

Solutions Manual
DISCRETE-EVENT SYSTEM SIMULATION
Fifth Edition

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Foreword

There are over three hundred exercises for solution in the text. These exercises emphasize principles of discrete-event simulation and provide practice in utilizing concepts found in the text.

Answers provided here are selective, in that not every problem in every chapter is solved. Answers in some instances are suggestive rather than complete. These two caveats hold particularly in chapters where building of computer simulation models is required. The solutions manual will give the instructor a basis for assisting the student and judging the student's progress. Some instructors may interpret an exercise differently than we do, or utilize an alternate solution method; they are at liberty to do so. We have provided solutions that our students have found to be understandable.

When computer solutions are provided they will be found on the text web site, www.bcnn.net, rather than here. Solutions in addition to those noted below may be developed and added to the book's web site.

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Chapter 1

Introduction to Simulation

1.1

	SYSTEM	ENTITIES	ATTRIBUTES	ACTIVITIES	EVENTS	STATE VARIABLES
	Small appliance repair shop	Appliances	Type of appliance Age of appliance Nature of problem	Repairing the appliance	Arrival of a job Completion of a job	Number of appliances waiting to be repaired Status of repair person busy or idle
a.	Cafeteria	Diners	Size of appetite Entree preference	Selecting food Paying for food	Arrival at service line Departures from service line	Number of diners in waiting line Number of servers working
b.	Grocery store	Shoppers	Length of grocery list	Checking out	Arrival at checkout counters Departure from checkout counter	Number of shoppers in line Number of checkout lanes in operation
c.	Laundromat	Washing machine	Breakdown rate	Repairing a machine	Occurrence of breakdowns Completion of service	Number of machines running Number of machines in repair Number of Machines waiting for repair

	SYSTEM	ENTITIES	ATTRIBUTES	ACTIVITIES	EVENTS	STATE VARIABLES
d.	Fast food restaurant	Customers	Size of order desired	Placing the order Paying for the order	Arrival at the counter Completion of purchase	Number of customers waiting Number of positions operating
e.	Hospital emergency room	Patients	Attention level required	Providing service required	Arrival of the patient Departure of the patient	Number of patients waiting Number of physicians working
f.	Taxicab company	Fares	Origination Destination	Traveling	Pick-up of fare Drop-off of fare	Number of busy taxi cabs Number of fares waiting to be picked up
g.	Automobile assembly line	Robot welders	Speed Breakdown rate	Spot welding	Breaking down	Availability of machines

1.3 Abbreviated solution:

Iteration	Problem Formulation	Setting of Objectives and Overall Project Plan
1	Cars arriving at the intersection are controlled by a traffic light. The cars may go straight, turn left, or turn right.	How should the traffic light be sequenced? Criterion for evaluating effectiveness: average delay time of cars. Resources required: 2 people for 5 days for data collection, 1 person for 2 days for data analysis, 1 person for 3 days for model building, 1 person for 2 days for running the model, 1 person for 3 days for implementation.
2	Same as 1 above plus the following: Right on red is allowed after full stop provided no pedestrians are crossing and no vehicle is approaching the intersection.	How should the traffic light be sequenced? Criterion for evaluating effectiveness: average delay time of cars. Resources required: 2 people for 8 days for data collection, 1 person for 3 days for data analysis, 1 person for 4 days for model building, 1 person for 2 days for running the model, 1 person for 3 days for implementation.
3	Same as 2 above plus the following: Trucks arrive at the intersection. Vehicles break down in the intersection making one lane impassable. Accidents occur blocking traffic for varying amounts of time.	How should the traffic light be sequenced? Should the road be widened to 4 lanes? Method of evaluating effectiveness: average delay time of all vehicles. Resources required: 2 people for 10 days for data collection, 1 person for 5 days for data analysis, 1 person for 5 days for model building, 1 person for 3 days for running the model, 1 person for 4 days for implementation.

1.4 Data Needed

Number of guests attending
 Time required for boiling water
 Time required to cook pasta
 Time required to dice onions, bell peppers, mushrooms
 Time required to saute onions, bell peppers, mushrooms, ground beef
 Time required to add necessary condiments and spices
 Time required to add tomato sauce, tomatoes, tomato paste
 Time required to simmer sauce
 Time required to set the table
 Time required to drain pasta
 Time required to dish out the pasta and sauce

Events

Begin cooking
 Complete pasta cooking } Simultaneous
 Complete sauce cooking }
 Arrival of dinner guests
 Begin eating

Activities

Boiling the water
 Cooking the pasta
 Cooking sauce
 Serving the guests

State variables

Number of dinner guests
 Status of the water (boiling or not boiling)
 Status of the pasta (done or not done)
 Status of the sauce (done or not done)

1.5 Event

Deposit
 Withdrawal

Activities

Writing a check
 Cashing a check
 Making a deposit
 Verifying the account balance
 Reconciling the checkbook with the bank statement

- 1.12 (a) 1971 with 1200 attendees
 (b) 1972
 (c) From Dec. 8, 1971 to Jan. 17, 1973, 1.11 years

(d) DC, Southeast, West

- 1.15 The pupose of the WSC Foundation is to develop and manage a fund to help insure the continuance and high quality of the WSC.

Chapter 2

Simulation Examples in a Spreadsheet

For additional solutions check the course web site at www.bcnn.net. The numbers resulting from a student's spreadsheet simulation may differ from the results here, depending on the random numbers used.

In the spreadsheet solutions, the columns labeled "RD Assignment" are for manual solutions using the random digits in Table A. 1. You can ignore these columns when solving the problem in Excel, and instead use the methods in the textbook.

2.1

Clock			Clock			Clock		
Interarrival			Service	Time	Waiting		Time	
	Time	Arrival	Time	Service	Time	Time	Customer	
Customer	(Minutes)	Time	(Minutes)	Begins	in Queue	Service	Spends in	Idle Time
					(Minutes)	Ends	System	of Server
							(Minutes)	(Minutes)
1		0	25	0	0	25	25	
2	0	0	50	25	25	75	75	0
3	60	60	37	75	15	112	52	0
4	60	120	45	120	0	165	45	8
5	120	240	50	240	0	290	50	75
6	0	240	62	290	50	352	112	0
7	60	300	43	352	52	395	95	0
8	120	420	48	420	0	468	48	25
9	0	420	52	468	48	519	99	0
10	120	540	38	540	0	578	38	21
Average			45		19		112	

- (a) The average time in the queue for the 10 new jobs is 19 minutes.
 (b) The average processing time of the 10 new jobs is 45 minutes.
 (c) The maximum time in the system for the 10 new jobs is 112 minutes.

2.2 Profit = Revenue from retail sales - Cost of bagels made + Revenue from grocery store sales - Lost profit.

Let Q = number of dozens baked/day

$S = \sum_i 0_i$, where 0_i = Order quantity in dozens for the i th customer

$Q - S$ = grocery store sales in dozens, $Q > S$

$S - Q$ = dozens of excess demand, $S > Q$

Profit = $\$5.40 \min(S, Q) - \$3.80Q + \$2.70(Q - S) - \$1.60(S - Q)$

Number of Customers	Probability	Cumulative Probability	RD Assignment
8	.35	.35	01-35
10	.30	.65	36-65
12	.25	.90	66-90
14	.10	1.00	91-100

Dozens Ordered	Probability	Cumulative Probability	RD Assignment
1	.4	.4	1-4
2	.3	.7	5-7
3	.2	.9	8-9
4	.1	1.0	0

Pre-analysis

$$\begin{aligned}
 E(\text{Number of Customers}) &= .35(8) + .30(10) + .25(12) + .10(14) \\
 &= 10.20
 \end{aligned}$$

$$E(\text{Dozens ordered}) = .4(1) + .3(2) + .2(3) + .1(4) = 2$$

$$E(\text{Dozens sold}) = \bar{S} = (10.20)(2) = 20.4$$

$$\begin{aligned}
 E(\text{Profit}) &= \$5.40\text{Min}(\bar{S}, Q) - \$3.80Q + \$2.70(Q - \bar{S}) - \$1.60(\bar{S} - Q) \\
 &= \$5.40\text{Min}(20.4, Q) - \$3.80Q + \$2.70(Q - 20.4) \\
 &\quad - \$0.67(20.4 - Q)
 \end{aligned}$$

$$E(\text{Profit}|Q = 0) = 0 - 0 + \$1.60(20.4) = -\$32.64$$

$$\begin{aligned}
 E(\text{Profit}|Q = 10) &= \$5.40(10) - \$3.80(10) + 0 - \$1.60(20.4 - 10) \\
 &= -\$0.64
 \end{aligned}$$

$$\begin{aligned}
 E(\text{Profit}|Q = 20) &= \$5.40(20) - \$3.80(20) + 0 - \$1.60(20.4 - 20) \\
 &= \$15.36
 \end{aligned}$$

$$\begin{aligned}
 E(\text{Profit}|Q = 30) &= \$5.40(20.4) - \$3.80(30) + \$2.70(30 - 20.4) - 0 \\
 &= \$22.08
 \end{aligned}$$

$$\begin{aligned}
 E(\text{Profit}|Q = 40) &= \$5.40(20.4) - \$3.80(40) + \$2.70(40 - 20.4) - 0 \\
 &= \$11.08
 \end{aligned}$$

The pre-analysis, based on expectation only, indicates that simulation of the policies $Q = 20, 30$, and 40 should be sufficient to determine the policy. The simulation should begin with $Q = 30$, then proceed to $Q = 40$, then, most likely to $Q = 20$.

Initially, conduct a simulation for $Q = 20, 30$ and 40 . If the profit is maximized when $Q = 30$, it will become the policy recommendation.

The problem requests that the simulation for each policy should run for 5 days. This is a very short run length to make a policy decision.

$Q = 30$