Solutions to Practice Problems in the Text

Chapter One: Fundamentals of Mathematical Modeling

Practice Set 1-2

1.
$$d = rt$$

 $125 = 50t$ [Divide both sides by 50.]
 $t = 2.5$ hours

2.
$$d = rt$$

 $170 = r(2.5)$ [Divide both sides by 2.5.]
 $68 \text{ mph} = r$

3.
$$I = Prt$$

 $I = (\$5000)(0.05)(2) = \500

4.
$$I = Prt$$

 $616 = (2800)r(4)$
 $616 = 11200r$
 $0.055 = r$

5.
$$A = \pi r^2$$

 $A = \pi (3)^2 = (3.14)(9) = 28.26 \text{ in}^2$

6.
$$A = \pi r^2$$

 $12.56 = (3.14)r^2$
 $4 = r^2$
 $\sqrt{4} = 2 \text{ ft} = r$

7.
$$A = \frac{1}{2}bh$$

 $36 = \frac{1}{2}(8)h$
 $36 = 4h$
9 in = h

8.
$$A = \frac{1}{2}bh$$

 $150 = \frac{1}{2}b(40)$
 $150 = 20b$
7.5 cm = b

9.
$$A = \sqrt{s(s-a)(s-b)(s-c)} = \sqrt{15(15-5)(15-12)(15-13)} = \sqrt{15(10)(3)(2)} = \sqrt{900} = 30 \text{ in}^2$$

10.
$$A = \sqrt{s(s-a)(s-b)(s-c)} = \sqrt{6(6-3)(6-4)(6-5)} = \sqrt{6(3)(2)(1)} = \sqrt{36} = 6 \text{ in}^2$$

11.
$$C = \frac{5}{9}(F - 32) = \frac{5}{9}(68 - 32) = \frac{5}{9}(36) = 20^{\circ} C$$

12.
$$C = \frac{5}{9}(F - 32) = \frac{5}{9}(-4 - 32) = \frac{5}{9}(-36) = -20^{\circ} C$$

13.
$$F = \frac{9}{5}C + 32 = \frac{9}{5}(-10) + 32 = -18 + 32 = 14^{\circ} F$$

14.
$$F = \frac{9}{5}C + 32 = \frac{9}{5}(100) + 32 = 180 + 32 = 212^{\circ} F$$

15.
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-3 - (-4)}{-1 - 2} = \frac{-3 + 4}{-1 - 2} = \frac{1}{-3} = -\frac{1}{3}$$

16.
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 0}{-3 - (-1)} = \frac{-2}{-3 + 1} = \frac{-2}{-2} = 1$$

17.
$$z = \frac{x - \overline{x}}{s} = \frac{95 - 100}{15} = \frac{-5}{15} = -\frac{1}{3}$$

18.
$$z = \frac{x - \overline{x}}{s} = \frac{25.2 - 17.3}{7.9} = \frac{7.9}{7.9} = 1$$

19.
$$a^2 + b^2 = c^2$$

$$3^2 + 4^2 = c^2$$

$$9 + 16 = c^2$$

$$25 = c^2$$

$$\sqrt{25} = 5 = c$$

20.
$$a^2 + b^2 = c^2$$

$$12^2 + 5^2 = c^2$$

$$144 + 25 = c^2$$

$$169 = c^2$$

$$\sqrt{169} = 13 = c$$

21.
$$M = P\left(1 + \frac{r}{n}\right)^{nt} = 5000\left(1 + \frac{0.045}{12}\right)^{12*10} = 5000\left(1 + \frac{0.045}{12}\right)^{120} = $7834.96$$

22.
$$M = P\left(1 + \frac{r}{n}\right)^{nt} = 12,000\left(1 + \frac{0.0325}{12}\right)^{12*5} = 12,000\left(1 + \frac{0.0325}{12}\right)^{60} = \$14,114.28$$

23.
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-5 \pm \sqrt{(5)^2 - 4(1)(-6)}}{2(1)} = \frac{-5 \pm \sqrt{25 + 24}}{2} = \frac{-5 \pm \sqrt{49}}{2} = \frac{-12}{2} = -6$$

24.
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-9) \pm \sqrt{(-9)^2 - 4(2)(-5)}}{2(2)} = \frac{9 \pm \sqrt{81 + 40}}{4} = \frac{9 + \sqrt{121}}{4} = \frac{9 + 11}{4} = \frac{20}{4} = 5 \quad or \quad \frac{9 - \sqrt{121}}{4} = \frac{9 - 11}{4} = \frac{-2}{4} = -0.5$$

25.
$$y = Ae^{rn} = 1,500,000e^{0.055*7} = 1,500,000e^{0.385} = 2,204,421$$
 bacteria

26.
$$y = Ae^{rn} = 45,000e^{0.015*10} = 45,000e^{0.15} = 52,282.5 = 52,283$$
 people

$$\frac{I}{Pt} = \frac{Prt}{Pt}$$

[Divide both sides by *Pt.*]

$$\frac{I}{Pt} = r$$

28.
$$V = lwh$$

$$\frac{V}{lh} = \frac{lwh}{lh}$$

[Divide both sides by *lh*.]

$$\frac{V}{lh} = w$$

29.
$$A = \frac{1}{2}bh$$

$$2A = bh$$

[Multiply both sides by 2.]

$$\frac{2A}{h} = b$$

[Divide both sides by h to solve for b.]

30.
$$V = \frac{1}{3}Bh$$

$$3V = Bh$$

[Multiply both sides by 3.]

$$\frac{3V}{B} = h$$

[Divide both sides by B to solve for h.]

31.
$$P = 2L + 2W$$

$$P - 2W = 2L + 2W - 2W$$

[Subtract 2W from both sides.]

$$P-2W=2L$$

$$\frac{P-2W}{2}=L$$

[Divide both sides by 2.]

$$32. \qquad P = 2L + 2W$$

$$P - 2L = 2L + 2W - 2L$$

[Subtract 2L from both sides.]

$$P-2L=2W$$

$$\frac{P-2L}{2} = W$$

[Divide both sides by 2.]

33.
$$A = \frac{1}{2}(B + b)h$$

$$2(A) = 2[\frac{1}{2}(B+b)h]$$

[Multiply both sides by 2.]

$$2A = (B+b)h$$

$$2A = Bh + bh$$

[Use the Distributive Property.]

$$2A - bh = Bh + bh - bh$$

[Subtract bh from both sides.]

$$2A - bh = Bh$$

$$\frac{2A - bh}{h} = B$$

[Divide both sides by *h* to solve for *B*.]

34.
$$A = \frac{1}{2}(B + b)h$$

$$2(A) = 2[\frac{1}{2}(B+b)h]$$

$$2A = (B+b)h$$

$$\frac{2A}{B+b} = h$$

[Multiply both sides by 2.]

[Divide both sides by (B + b) to solve for h.]

35.
$$2x + 3y = 6$$

$$2x + 3y - 2x = 6 - 2x$$

$$3y = 6 - 2x$$

$$y = 2 - \frac{2}{3}x$$

[Subtract 2x from both sides.]

[Divide both sides by 3 to solve for y.]

36.
$$2x - y = 10$$

$$2x - y - 2x = 10 - 2x$$

-y = 10 - 2x

$$y = -10 + 2x$$

[Subtract 2x from both sides.]

[Divide both sides by -1.]

$$37. \qquad A = \frac{x+y}{2}$$

$$2A = x + y$$

$$2A - y = x + y - y$$

$$2A - y = x$$

[Multiply both sides by 2.]

[Subtract y from both sides.]

$$A = \frac{x+y}{2}$$

$$2A = x + y$$

[Multiply both sides by 2.]

$$2A - x = x + y - x$$

[Subtract *x* from both sides.]

$$2A - x = y$$

39.
$$F = \frac{9}{5}C + 32$$

$$5F = 9C + 160$$
 [Multiply through by 5.]
$$5F - 160 = 9C + 160 - 160$$
 [Subtract 160 from both sides.]
$$5F - 160 = 9C$$

$$\frac{5}{9}F - \frac{160}{9} = C$$
 [Divide both sides by 9.]
$$\frac{5}{9}(F - 32) = C$$
 [Factor out $\frac{5}{9}$.]

40.
$$C = \frac{5}{9}(F - 32)$$

$$C = \frac{5}{9}F - \frac{160}{9}$$
 [Use the distributive property.]
$$C + \frac{160}{9} = \frac{5}{9}F - \frac{160}{9} + \frac{160}{9}$$
 [Add $\frac{160}{9}$ to both sides.]
$$C + \frac{160}{9} = \frac{5}{9}F$$

$$\frac{9}{5}C + 32 = F$$
 [Multiply through by $\frac{9}{5}$.]

41. BMI =
$$\frac{W}{H^2} \cdot 703 = \frac{140}{73^2} \cdot 703 = 18.4687... = 18.5$$
, Normal

42. BMI =
$$\frac{W}{H^2} \cdot 703 = \frac{160}{60^2} \cdot 703 = 31.2444... = 31.2$$
, Obese

Practice Set 1-3

1.
$$\frac{45 \, min}{2 \, hr} = \frac{45 \, min}{120 \, min} = \frac{3}{8}$$

2.
$$\frac{1 \, hr}{35 \, \text{min}} = \frac{60 \, \text{min}}{35 \, \text{min}} = \frac{12}{7}$$

3.
$$\frac{4 in}{4 ft} = \frac{4 in}{48 in} = \frac{1}{12}$$

4.
$$\frac{3 \text{ ft}}{60 \text{ in}} = \frac{36 \text{ in}}{60 \text{ in}} = \frac{3}{5}$$

5.
$$\frac{6 \text{ ft}}{3 \text{ yd}} = \frac{6 \text{ ft}}{9 \text{ ft}} = \frac{2}{3}$$

6.
$$\frac{2 \ yd}{12 \ ft} = \frac{6 \ ft}{12 \ ft} = \frac{1}{2}$$

7.
$$\frac{8 \text{ weeks}}{16 \text{ days}} = \frac{56 \text{ days}}{16 \text{ days}} = \frac{7}{2}$$

8.
$$\frac{5 \, days}{1 \, week} = \frac{5 \, days}{7 \, days} = \frac{5}{7}$$

9.
$$\frac{25 \ mL}{1 \ L} = \frac{25 \ mL}{1000 \ mL} = \frac{1}{40}$$

10.
$$\frac{2400 \ mL}{2 \ L} = \frac{2400 \ mL}{2000 \ mL} = \frac{6}{5}$$

11.
$$\frac{304 \, miles}{9.5 \, gal} = 32 \, \text{mi./gal.}$$

12.
$$\frac{450 \, miles}{20 \, gal} = 22.5 \, \text{mi./gal.}$$

13.
$$\frac{\$3.50}{10 \,\text{min}} = \$0.35/\text{min}.$$

14.
$$\frac{\$86.40}{720 \, kWh} = \$0.12 / kWh$$

15.
$$\frac{$48}{10 \, days} = $4.80/day$$

16.
$$\frac{\$340}{40\,hr} = \$8.50/hr$$

17.
$$\frac{24lb}{15 people} = 1.6 \text{ lb./person}$$

18.
$$\frac{5.5 lb}{12 \ people} = 0.458\overline{3} \ lb./person$$

19.
$$\frac{x}{5} = \frac{3}{4}$$

$$4x = (3)(5)$$

$$4x = 15$$

$$x = \frac{15}{4}$$

[cross-multiplication property]

20.
$$\frac{9}{2x} = \frac{6}{4}$$

$$(4)(9) = (2x)(6)$$

$$36 = 12x$$

$$3 = x$$

[cross-multiplication property]

21.
$$\frac{30}{126} = \frac{5}{3x}$$
$$(3x)(30) = 5(126)$$
$$90x = 630$$
$$x = 7$$

[cross-multiplication property]

22.
$$\frac{2x}{7} = \frac{8}{14}$$
$$(2x)(14) = (7)(8)$$
$$28x = 56$$
$$x = 2$$

[cross-multiplication property]

23.
$$\frac{3x+6}{35} = \frac{2x-18}{5}$$

$$5(3x+6) = 35(2x-18)$$

$$15x+30 = 70x-630$$

$$15x+30-70x = 70x-630-70x$$

$$-55x+30=-630$$

$$-55x+30-30=-630-30$$

$$-55x=-660$$

$$x = 12$$

[cross-multiplication property] [distributive property]

24.
$$\frac{x-2}{7} = \frac{2x+2}{28}$$

$$28(x-2) = 7(2x+2)$$

$$28x - 56 = 14x + 14$$

$$28x - 56 - 14x = 14x + 14 - 14x$$

$$14x - 56 = 14$$

$$14x - 56 + 56 = 14 + 56$$

[cross-multiplication property] [distributive property]

$$14x = 70$$
$$x = 5$$

25.
$$\frac{15}{18} = \frac{x-1}{x}$$

$$(15)(x) = 18(x-1)$$

$$15x = 18x - 18$$

$$15x - 18x = 18x - 18 - 18x$$

$$-3x = -18$$

$$x = 6$$

[cross-multiplication property] [distributive property]

26.
$$\frac{3}{x+4} = \frac{5}{2x+3}$$
$$3(2x+3) = 5(x+4)$$
$$6x+9 = 5x+20$$
$$6x+9-5x = 5x+20-5x$$
$$x+9 = 20$$
$$x+9-9 = 20-9$$
$$x = 11$$

[cross-multiplication property] [distributive property]

27.
$$\frac{3}{x+1} = \frac{18}{9x-3}$$

$$3(9x-3) = 18(x+1)$$

$$27x-9 = 18x+18$$

$$27x-9-18x = 18x+18-18x$$

$$9x-9=18$$

$$9x-9+9=18+9$$

$$9x = 27$$

$$x = 3$$

$$x+8 = 2x-8$$

[cross-multiplication property] [distributive property]

28. $\frac{x+8}{6} = \frac{2x-8}{3}$ 3(x+8) = 6(2x-8) 3x + 24 = 12x - 48 3x + 24 - 12x = 12x - 48 - 12x -9x + 24 = -48 -9x + 24 - 24 = -48 - 24 -9x = -72 x = 8

[cross-multiplication property] [distributive property]

- 29. Unit rate equals cost divided by the number of square feet. $$2235 \div 1500 \text{ ft}^2 = $1.49/\text{ft}^2$$
- 30. Unit rate equals cost divided by the number of yards. $$47.80 \div 4 \text{ yd} = $11.95/\text{yd}$
- 31. Cost per ounce = $\$8.99 \div 16$ oz = \$0.561875 per ounce

- 32. Cost per can = $\$7.14 \div 6$ cans = \$1.19 per can
- 33. Brand X: $$1.49 \div 8 \text{ oz} = $0.18625/ \text{ ounce}$ Brand Z: $$2.12 \div 12 \text{ oz} = $0.1766.../ \text{ounce}$ Brand Z is the better buy because it costs less per ounce.
- 34. five 2-L colas: $\$4.95 \div 5 = \0.99 /bottle three 2-L colas: $\$2.99 \div 3 = \0.99666 ../bottle Purchasing five 2-L colas for \$4.95 is a better buy.
- 35. Let $\frac{120 \ cal}{\frac{3}{4} \ cup} = \frac{x}{1 \ cup}$ $(1)(120) = \frac{3}{4}x$ $120 = \frac{3}{4}x$ $160 \ calories = x$ [Cross multiply.]
 [Multiply both sides by 4/3.]
- 36. Let $\frac{8 oz}{90 cal} = \frac{28 oz}{x}$. 8x = (90)(28) [Cross multiply.] 8x = 2520x = 315 calories
- 37. Let $\frac{2.5 dozen}{1.25 cups} = \frac{x dozen}{3 cups}.$ (3)(2.5) = 1.25x 7.5 = 1.25x 6 = xAnswer is 6 dozen or 72 muffins.
- 38. If each of 30 students has 2 cookies, then 60 cookies are needed. $60 \div 12 = 5$ doz.

Let
$$\frac{3 dozen}{2.5 cups} = \frac{5 dozen}{x}$$

$$3x = (5)(2.5)$$

$$3x = 12.5$$

$$x = 4.16666... = 4\frac{1}{6} cups$$
[Cross multiply.]

- 39. Let $\frac{5 \text{ ft 4 in}}{10.5 \text{ ft}} = \frac{x}{20 \text{ ft}}$. Convert the measurements to inches as follows: 5 ft 4 in = 5(12)
 - +4 = 64 inches; 10.5 ft $= 10.5 \times 12$ in = 126 inches; 20 ft $= 20 \times 12$ in = 240 inches. Now substitute:

$$\frac{64 \text{ in}}{126 \text{ in}} = \frac{x}{240 \text{ in}}$$
$$(64)(240) = 126x$$

15360 = 126x

121.9 inches = x

Converting to feet and inches: 121.9 inches $\div 12$ in/ft = 10 ft. 1.9 in.

40. Let $\frac{5 \text{ ft } 10 \text{ in}}{8 \text{ ft } 9 \text{ in}} = \frac{x}{14 \text{ ft}}$. Convert the measurements to inches as follows: 5 ft 10 in = 5(12)

+10 = 70 inches, 8 ft 9 in = 8(12) + 9 = 105 inches, and 14 ft = 14(12) = 168 inches.

Now substitute:

$$\frac{70 \ in}{105 \ in} = \frac{x}{168 \ in}$$

(70)(168) = 105x [Cross multiply.]

11760 = 105x

112 inches = x

(112 inches = 9 feet 4 inches)

41. Let
$$\frac{1.8A}{18V} = \frac{5.4A}{x}$$
.

(18)(5.4) = 1.8A [Cross multiply.]

97.2 = 1.8A

54 V = A

42. Let
$$\frac{10 A}{50 V} = \frac{25 A}{x}$$

10x = (25)(50) [Cross multiply.]

10x = 1250

x = 125 V

43. Let $\frac{110 \, lb}{19.4 \, lb} = \frac{200 \, lb}{x}$

110x = (19.4)(200) [Cross multiply.]

110x = 3880

x = 35.2727... or approximately 35.3 lb.

44. Let $\frac{110 lb}{19.4 lb} = \frac{155 lb}{x}$

110x = (19.4)(155)

[Cross multiply.]

110x = 3007

x = 27.336363... or approximately 27.3 lb.

45. Let $\frac{10 lb}{400 ft^2} = \frac{x}{500 ft^2}$

(10)(500) = 400x5000 = 400x

[Cross multiply.]

$$12.5 lb = x$$

46. Let
$$\frac{20}{1} = \frac{256 \text{ oz}}{x}$$
 [2 gallons = 256 oz.]
 $20x = (256)(1)$ [Cross multiply.]
 $20x = 256$
 $x = 12.8 \text{ oz.}$

47. Let
$$\frac{\$240}{1200 \, words} = \frac{x}{1500 \, words}$$
.
$$(240)(1500) = 1200x$$

$$360,000 = 1200x$$

$$\$300 = x$$

[Cross multiply.]

48. Let
$$\frac{1500 \ doughnuts}{9 \ hours} = \frac{300 \ doughnuts}{x}$$

$$1500x = (9)(300)$$

$$1500x = 2700$$

$$x = 1.8 \ hr.$$
[Cross multiply.]

49. Let
$$\frac{1 \text{ adult}}{15 \text{ children}} = \frac{3 \text{ adults}}{x}$$

$$x = (3)(15)$$

$$x = 45 \text{ children}$$
[Cross multiply.]

50. Let
$$\frac{1 \text{ adult}}{6 \text{ infants}} = \frac{x}{15 \text{ infants}}$$

$$15 = 6x$$

$$2.5 \text{ adults} = x$$
[Cross multiply.]

Therefore, 3 adults are needed for 15 infants.

51. Let
$$\frac{1 inch}{8 feet} = \frac{2.75 inches}{x}$$

$$x = (8)(2.75)$$

$$x = 22 feet [Cross multiply.]$$

Let
$$\frac{1 inch}{8 feet} = \frac{1.9375 inches}{x}$$

 $x = (8)(1.9375)$ [Cross multiply.]
 $x = 15.5 \text{ feet}$
Dimensions are 22 ft × 15.5 ft

52. Let
$$\frac{1 inch}{10 miles} = \frac{x}{185 miles}$$

$$(1)(185) = 10x$$

$$18.5 in = x$$
[Cross multiply.]

53. Let
$$\frac{Mach 1}{761.2 \, mph} = \frac{Mach \, 3.1}{x}$$

$$1x = (3.1)(761.2)$$

$$x = 2359.72 \, mph$$
[Cross multiply.]

54. Let
$$\frac{Mach 1}{761.2 \, mph} = \frac{x}{1903 \, mph}$$

 $761.2x = (1)(1903)$ [Cross multiply.]
 $x = 2.5$ (Mach 2.5)

55. Let
$$\frac{400 ft}{1 day} = \frac{1000 ft}{x}$$

(1)(1000) = 400x
 $1000 = 400x$
2.5 days = x [Cross multiply.]

56. Let
$$\frac{8 \text{ sq/day}}{1 \text{ roofer}} = \frac{x}{2 \text{ roofers}}$$

$$(2)(8 \text{ sq/day}) = x$$

$$16 \text{ sq/day} = x$$
[Cross multiply.]

Since 2 roofers can do 16 squares per day, they can do 32 squares in 2 days.

57. Let
$$\frac{40 \, mg}{1 \, mL} = \frac{60 \, mg}{x}$$
.
 $40x = (1)(60)$ [Cross multiply.]
 $40x = 60$
 $x = 1.5 \, \text{mL}$

58. Let
$$\frac{100 \, mg}{1 \, kg} = \frac{x}{9.3 \, kg}$$
.
 $(100)(9.3) = 1x$ [Cross multiply.]
 $930 \, \text{mg} = x$

59. Let
$$\frac{1.8 \, mi}{30 \, \text{min}} = \frac{x}{45 \, \text{min}}$$

$$(1.8)(45) = 30x$$

$$81 = 30x$$

$$2.7 \, \text{miles} = x$$
[Cross multiply.]

60. Let
$$\frac{1mph}{1.609 \, kph} = \frac{x}{98 \, kph}$$
$$(1)(98) = 1.609x$$
$$98 = 1.609x$$
$$60.9 \, \text{mph} = x$$

Practice Set 1-.4

1.
$$2x + 6$$

3.
$$7x - 2$$

4.
$$3 + 4x$$

5.
$$3(4+x)$$

6.
$$2(x-6)$$

7.
$$\frac{1}{3}x-5$$

8.
$$x - \frac{3}{4}x$$

9. Let Bill's salary =
$$x$$
. Then, Ann's salary = $x + 5000

10. Let Monday's attendance = x. Then, Friday's is
$$\frac{1}{2}x + 3$$

11. Let the width =
$$x$$
. Then, the length = $2x + 5$.

12. Let the short rod =
$$x$$
. Then, each subsequent rod is 1 inch longer: $x + 1$ and $x + 2$.

13.
$$5x + 5 = 2x - 10$$
$$5x + 5 - 2x = 2x - 10 - 2x$$
$$3x + 5 = -10$$
$$3x + 5 - 5 = -10 - 5$$
$$3x = -15$$
$$x = -5$$

14.
$$8x - 16 = 80$$

 $8x - 16 + 16 = 80 + 16$
 $8x = 96$
 $x = 12$

15. Emily has saved x. Elena has saved 2x (twice as much).

$$x + 2x = 72$$
$$3x = 72$$

x = 24 so Emily has saved \$24 and Elena has saved 2(\$24) = \$48.

16. Let the lower grade = x. The higher grade is x + 56.

$$x + (x + 56) = 128$$
$$2x + 56 = 128$$
$$2x + 56 - 56 = 128 - 56$$
$$2x = 72$$

x = 36 so the lower grade is 36 and the higher is 36 + 56 = 92.

17. Let x = the shorter piece. The longer piece will be 2x.

$$x + 2x = 60$$
 meters
 $3x = 60$ meters
 $x = 20$ meters

The shorter piece is 20 meters long and the longer piece is 2(20) = 40 meters long.

18. Let Joshua's age = x and Mario's age be x + 18.

$$x + (x + 18) = 46$$

$$2x + 18 = 46$$

$$2x + 18 - 18 = 46 - 18$$

$$2x = 28$$

$$x = 14$$

So, Joshua is 14 years old and Mario is 14 + 18 = 32 years old.

19. Using the definition of an average, let x equal the missing grade.

$$\frac{88+91+95+x}{4} = 90$$

$$88+91+95+x=4(90)$$

$$274+x=360$$

$$274-274+x=360-274$$

$$x=86$$

In order to have a 90 average, she must make 86 on the last test.

20. Using the definition of an average, let x equal the missing grade.

$$\frac{60+92+78+89+x}{5} = 84$$

$$60+92+78+89+x=5(84)$$

$$319+x=420$$

$$319-319+x=420-319$$

$$x=101$$

In order to have a B average, she must make 101 on the last test. On a normal grading scale, this will be impossible.

21. Let x = the number of kilowatt-hours. Write the equation and solve.

$$$20.00 + $0.14x = $85.78$$

 $20.00 - 20.00 + 0.14x = 85.78 - 20.00$
 $0.14x = 65.78$

$$x = \frac{65.78}{0.14} = 470 \, kWh$$
 (rounded)

22. Let x = number of "out of area" minutes.

$$$29.95 + $9.95 + $0.40x = $69.90$$

 $39.90 + 0.40x = 69.90$
 $39.90 - 39.90 + 0.40x = 69.90 - 39.90$
 $0.40x = 30$
 $x = 75$

She was charged for 75 "out of area" minutes.

23. Let x = the taxi fare. Since 1/11 of a mile costs \$0.20, the cost of one mile = $$0.20 \times 11 = 2.20 .

$$x = \$3.20 + 18(\$2.20/\text{mile}) + \$1.20 = \$44.00$$

24. Let x = the taxi fare. Since 1/5 of a mile costs \$0.40, the cost of one mile = $$0.40 \times 5 = 2.00 .

$$x = $2.50 + 16($2.00/mile) = $34.50$$

25. The opponent scored x points in the game. Mighty Mites scored 39 points. This amount (39) is 2x - 1.

$$2x - 1 = 39$$

$$2x - 1 + 1 = 39 + 1$$

$$2x = 40$$

$$x = 20$$

The opponent scored 20 points.

26. Let the number of games Jim won = x and the number that Gaylord won = x + 99.

$$x + (x + 99) = 529$$

 $2x + 99 = 529$
 $2x + 99 - 99 = 529 - 99$
 $2x = 430$
 $x = 215$

Jim won 215 games and Gaylord won 215 + 99 = 314 games.

27. Let the integers be x, x + 1 and x + 2. Write the equation for the sum and solve.

$$x + (x + 1) + (x + 2) = 87$$

 $3x + 3 = 87$
 $3x + 3 - 3 = 87 - 3$
 $3x = 84$
 $x = 28$

The integers are x = 28, x + 1 = 29 and x + 2 = 30.

28. Let the integers be x, x + 1 and x + 2. Write the equation for the sum and solve.

$$x + (x + 1) + (x + 2) = 100$$

$$3x + 3 = 100$$

 $3x + 3 - 3 = 100 - 3$
 $3x = 97$
 $x = 32.333...$

Since this number is not an integer, there is not a set of consecutive integers that satisfies the requirements of this problem.

29. Let the odd integers be x, x + 2, and x + 4. Write the equation for the sum and solve.

$$x + (x + 2) + (x + 4) = -273$$

$$3x + 6 = -273$$

$$3x + 6 - 6 = -273 - 6$$

$$3x = -279$$

$$x = -93$$

The three integers are x = -93, x + 2 = -91, and x + 4 = -89.

30. Let the odd integers be x, x + 2, and x + 4. Write the equation for the sum and solve.

$$x + (x + 2) + (x + 4) = 1503$$
$$3x + 6 = 1503$$
$$3x + 6 - 6 = 1503 - 6$$
$$3x = 1497$$
$$x = 499$$

The three integers are x = 499, x + 2 = 501, and x + 4 = 503.

31. Let x = the value of the lot. Then, 6.5x = the value of the house.

$$x + 6.5x = $175,000$$

 $7.5x = $175,000$
 $x = $23,333.33$

So, the lot is worth approximately \$23,333 and the house is worth about \$151,667.

32. Let x = the value of the lot. Then, 7x = the value of the house.

$$x + 7x = $164,000$$

 $8x = $164,000$
 $x = $20,500$

So, the lot is worth approximately \$22,500 and the house is worth about \$143,500.

33.
$$x = \frac{949 \text{ yen}}{146 \text{ yen/dollar}} = $6.50.$$

34.
$$x = \frac{65 \ pounds}{0.549 \ pounds / dollar} = $118.40$$

35.
$$time = \frac{distance}{speed} = \frac{500mi}{170.265mi/hr} = 2.936598831hr = about 2 hr 56 min$$

- 36. $x = 500 \text{ miles} \div 74.602 \text{ mph} = 6.702 \text{ hours}$. Convert 0.702 to minutes by multiplying 0.702(60) = 42.12 to give the answer of approximately 3 hours and 42 minutes.
- 37. Let the number of males and females at the beginning of the semester = x. If 8 males drop the class, there are x 8 males remaining. Now the number of females is twice the number of males remaining.

$$x = 2(x - 8)$$

$$x = 2x - 16$$

$$x - 2x = 2x - 16 - 2x$$

$$-x = -16$$

$$x = 16$$

There were 16 males and 16 females at the beginning of the semester.

38. Let x = the number of Democrats and the number of Republicans in the Senate.

$$x + x + 2 = 100$$

$$2x + 2 = 100$$

$$2x + 2 - 2 = 100 - 2$$

$$2x = 98$$

$$x = 49$$

There were 49 Democrats and 49 Republicans in the Senate.

39. Let x = the number of bags of apples.

$$5x + 2x = 252$$
$$7x = 252$$
$$x = 36$$

There are 36 bags containing 5 lb. of apples and 36 bags containing 2 lb. of apples.

40. Let x = the number of seats in Theater B, x + 150 = the number of seats in Theater A.

$$(x + 150) + x + 270 = 800$$
$$2x + 420 = 800$$
$$2x + 420 - 420 = 800 - 420$$
$$2x = 380$$
$$x = 190$$

The number of seats in Theater A is x + 150 = 190 + 150 = 340.

41. Let x = profit from the automotive division. Then x - 273 represents the profit from financial services.

$$x + (x - 273 \text{ million}) = 483 \text{ million}$$

 $2x - 273 \text{ million} = 483 \text{ million}$
 $2x - 273 \text{ million} + 273 \text{ million} = 483 \text{ million} + 273 \text{ million}$
 $2x = 756 \text{ million}$
 $x = 378 \text{ million}$

The profit from the automotive division was 378 million and from financial services

was 378 million - 273 million = 105 million.

42. Let x = salary of Palmisano and x - \$3.91 million = Moonvie's salary.

$$x+x-3.91 \ million = 56.73 \ million$$

$$2x-3.91 \ million + 3.91 \ million = 56.73 \ million + 3.91 \ million$$

$$2x=60.64 \ million$$

$$x=30.32 \ million$$

Therefore, Palmisano made \$30.32 million and Moonvie made \$26.41 million in 2010.

43. Let x = attendance at the Ohio State game and x - 1044 = attendance at the Penn State game. Total attendance for the two teams in 2010 was 209,512.

$$x + x - 1044 = 209,512$$

 $2x - 1044 = 209,512$
 $2x - 1044 + 1044 = 209,512 + 1044$
 $2x = 210,556$
 $x = 105,278$

Therefore, the attendance at the Ohio State game was 105,278 and the attendance at the Penn State game was 105,278 - 1044 = 104,234.

44. Let x = the middle-sized piece. The longest is 3x and the shortest is 3x - 23.

The total length of the pipe is 40 inches. Therefore,

$$3x + x + 3x - 23 = 40$$

 $7x - 23 = 40$
 $7x - 23 + 23 = 40 + 23$
 $7x = 63$
 $x = 9$

Therefore, the middle sized piece is 9 in., the longest is 3(9) = 27 in. and the shortest is 3x - 23 = 3(9) - 23 = 4 in.

45. Let x = the original price of the radio. Savings = 15% of retail price or 0.15x.

$$x - 0.15x = $127.46$$

 $0.85x = 127.46
 $x = 149.95

The original price of the radio was \$149.95.

46. Let x = the original price of the watch. Savings = 25% of retail price or 0.25x.

$$x - 0.25x = $168.75$$

 $0.75x = 168.75
 $x = 225

The original price of the watch was \$225.00.

47. Let x = the wholesale price of the shoes. The markup amount is 65% times x.

$$x + 0.65x = $125.40$$

 $1.65x = 125.40
 $x = 76

The wholesale price of the shoes was \$76.00.

48. Let x = the wholesale price of the shoes. The markup amount is 40% times x.

$$x + 0.40x = $63$$

$$1.4x = $63$$

$$x = $45$$

The wholesale price of the shoes was \$45.00.

49. Let x = Drema's contributions. The company's contributions = 20% of x.

$$x + 0.20x = $1200$$

$$1.2x = $1200$$

$$x = $1000$$

Drema deposited \$1000 into the account.

50. Let x = the population four years ago. The growth of the population is 5% of x.

$$x + 0.05x = 882$$

$$1.05x = 882$$

$$x = 840$$

There were 840 people in the town four years ago.

51. BMI =
$$\frac{W}{H^2} \cdot 703 = \frac{120}{60^2} \cdot 703 = 23.4333... = 23.4$$
, Normal

52. BMI =
$$\frac{W}{H^2} \cdot 703 = \frac{195}{67^2} \cdot 703 = 30.53798... = 30.5$$
, Obese

Chapter 1 Review Problems

1..
$$I = Prt$$

$$t = \frac{I}{Pr}$$

[Divide both sides by Pr.]

2. 2x + 3y = 9

$$3y = -2x + 9$$

$$y = -\frac{2}{3}x + 3$$

[Divide all terms by 3.]

3. $C = \pi d$

$$d = \frac{C}{\pi}$$

[Divide both sides by π .]

4. a + b + c = P

$$c = P - a - b$$

[Subtract a and b from both sides.]

5. $\frac{27 \, min}{3 \, hr} = \frac{27 \, min}{180 \, min} = \frac{3}{20}$

$$6. \quad \frac{4 \text{ weeks}}{21 \text{ days}} = \frac{28 \text{ days}}{21 \text{ days}} = \frac{4}{3}$$

7.
$$\frac{6 in}{5 ft} = \frac{6 in}{60 in} = \frac{1}{10}$$

8.
$$\frac{$60}{5 hr} = $12/\text{hour}$$

9.
$$\frac{44 \text{ bushels}}{8 \text{ trees}} = 5.5 \text{ bushels/tree}$$

10.
$$\frac{$12.80}{3.5 lb} = $3.66/lb$$
.

11.
$$\frac{x}{3} = \frac{4}{7}$$
$$7x = 12$$
$$x = \frac{12}{7}$$

12.
$$\frac{2}{3} = \frac{8}{2x}$$
$$4x = 24$$
$$x = 6$$

13.
$$\frac{x-3}{8} = \frac{3}{4}$$

$$4x - 12 = 24$$

$$4x - 12 + 12 = 24 + 12$$

$$4x = 36$$

$$x = 9$$

14.
$$\frac{4x-3}{7} = \frac{2x-1}{3}$$

$$12x-9 = 14x-7$$

$$12x-9-14x = 14x-7-14x$$

$$-2x-9+9 = -7+9$$

$$-2x = 2$$

$$x = -1$$

15.
$$A = \frac{1}{2}bh$$
. Substitute: $A = \frac{1}{2}(3 \text{ in})(4 \text{ in}) = 6 \text{ in}^2$

- 16. Let $\frac{2400 L}{50 min} = \frac{x}{30 min}$. Cross multiply. 72000 = 50x 1440 liters = x
- 17. Let $\frac{3}{4} = \frac{x}{92}$. Cross multiply. 276 = 4x 69 dentists = x
- 18. Let x = total number of minutes that you talk. Then, \$1.24 + (x 4)(\$0.28) = \$3.76 1.24 + 0.28x - 1.12 = 3.76 0.12 + 0.28x = 3.76 0.12 + 0.28x - 0.12 = 3.76 - 0.12 0.28x = 3.64x = 13 The call was 13 minutes long.
- 19. Let x = number of minutes per month. Then, \$50 + \$0.36x = \$99.68. 0.36x = 99.68 50 0.36x = 49.68 x = 138 minutes
- 20. Let x = labor time (per hour). Then, \$40 + \$30x = \$115 40 + 30x - 40 = 115 - 40 30x = 75x = 2.5 hours
- 21. Let the shorter piece be x and the longer be x + 3. Then, x + (x + 3) = 33 2x + 3 = 33 2x + 3 3 = 33 3 2x = 30 $x = 15 \text{ in (short piece)} \quad \text{and} \quad x + 3 = 15 + 3 = 18 \text{ in (long piece)}$
- 22. Let the short piece = x, the middle-sized piece = x + 14, and the long piece = 3x.

Then,
$$x + (x + 14) + 3x = 79$$

 $5x + 14 = 79$
 $5x + 14 - 14 = 79 - 14$
 $5x = 65$
 $x = 13$ cm (short)
 $x + 14 = (13) + 14 = 27$ cm (middle)
 $3x = 3(13) = 39$ cm (long)

23. Let the calculator be x and the cassette player be x + 140.

Then,
$$x + (x + 140) = 208$$

 $2x + 140 = 208$

$$2x + 140 - 140 = 208 - 140$$

 $2x = 68$
 $x = 34.00 which is the cost of the calculator

24. Let n = the number of nickels and 2n - 2 = the number of dimes.

Then,
$$n + (2n - 2) = 52$$
.
 $3n - 2 = 52$
 $3n - 2 + 2 = 52 + 2$
 $3n = 54$

n = 18 There are 18 nickels and 34 dimes in the bank for a total of \$4.30.

25. Use the formula d = rt and substitute values.

182 mi =
$$(52 \text{ mph})(t)$$

t = 3.5 hours

26. T = UN + F Substitute the given values and solve.

$$$16,750 = $15N + $2500$$

 $16750 - 2500 = 15N + 2500 - 2500$
 $14250 = 15N$
 $N = 950$ units produced

26. First remove the parentheses by use of the distributive property, then add 2 to the 12.

$$2 + 3(2x + 4) = 2 + 6x + 12 = 6x + 14$$
.

28.
$$5x + 3 = 6x$$

 $5x + 3 - 5x = 6x - 5x$
 $3 = x$

29. for any triangle, $A + B + C = 180^{\circ}$

Let A =the first angle

The second angle, B = 3A

The third angle, $C = \frac{2}{3}(3A) = 2A$

$$A + 3A + 2A = 180^{\circ}$$

$$6A=180^{\text{o}}$$

$$A = 30^{\circ}, B = 3(30^{\circ}) = 90^{\circ}, C = 2(30^{\circ}) = 60^{\circ}$$

30. First convert all the measurements to the same units, like inches.

$$5 \text{ ft } 3 \text{ in} = 63 \text{ in}, \ 10 \text{ ft } 6 \text{ in} = 126 \text{ in}, \ \text{and } 52 \text{ ft} = 624 \text{ in}$$

Now set up a proportion like: $\frac{63in}{126in} = \frac{x}{624in}$

Cross multiply: (63in)(624in) = (126in)(x)

Divide by 126in: x = 312in = 26ft

Chapter 1 Test

1.
$$V = lwh$$

$$w = \frac{V}{lh}$$
[Divide both sides by lh .]

2.
$$h = vt - 16t^2$$

 $h + 16t^2 = vt$ [Add $16t^2$ to both sides.]

$$\frac{h+16t^2}{t} = v$$
 [Divide both sides by t .]

3.
$$\frac{4 \, hr}{1 \, day} = \frac{4 \, hr}{24 \, hr} = \frac{1}{6}$$

4.
$$\frac{10 \text{ ft}}{160 \text{ in}} = \frac{120 \text{ in}}{160 \text{ in}} = \frac{3}{4}$$

5.
$$\frac{\$413.20}{4 \ days} = \$103.30 / day$$

6.
$$\frac{7.5 lb}{6 people} = 1.25 lb/person$$

7.
$$\frac{50 \, eggs}{10 \, chickens} = 5 \, eggs / chicken$$

8.
$$\frac{7}{12} = \frac{3x}{10}$$

$$70 = 36x$$

$$\frac{70}{36} = \frac{35}{18} = x$$

9.
$$\frac{x-4}{8} = \frac{2x+3}{9}$$

$$9(x-4) = 8(2x+3)$$

$$9x - 36 = 16x + 24$$

$$9x - 36 - 16x = 16x + 24 - 16x$$

$$-7x - 36 = 24$$

$$-7x - 36 + 36 = 24 + 36$$

$$-7x = 60$$

$$x = -\frac{60}{7}$$

10. Let
$$x =$$
 defective bulbs. Then, $\frac{3}{85} = \frac{x}{510}$.
 $85x = 1530$
 $x = 18$ bulbs

11. Let
$$x = \text{parts produced}$$
. Then, $\frac{300 \text{ parts}}{20 \text{ min}} = \frac{x}{45 \text{ min}}$.

$$20x = 13500$$

$$x = 675 \text{ parts}$$

12. Given
$$P = 2L + 2W$$
. Substitute the given values into the formula. $P = 2(20 \text{ ft.}) + 2(12 \text{ ft.}) = 64 \text{ ft.}$

13. Company A Plan:
$$$20 + 0.10m$$
 (where $m = miles driven$) Company B Plan: $$10 + 0.30m$

To find the number of miles where the two costs are equal, set these two expressions equal.

$$\$20 + 0.10m = \$10 + 0.30m$$

$$20 + 0.10m - 0.10m = 10 + 0.30m - 0.10m$$

$$20 = 10 + 0.20m$$

$$20 - 10 = 10 + 0.20m - 10$$

$$10 = 0.20m$$

$$50 = m, \text{ so at 50 miles the costs are the same for both plans}$$

14. Let the number of passengers on one ship =
$$x$$
.
The second ship holds twice as many passengers = $2x$
Write the equation $x + 2x = 2250$ and solve.
 $3x = 2250$
 $x = 750$ so the smaller ship holds 750 passengers

15. Let Sarah's age be x. Then, Michelle's age is 5x - 10. Write the equation and solve.

$$x + 5x - 10 = 44$$

 $6x - 10 = 44$
 $6x - 10 + 10 = 44 + 10$
 $6x = 54$
 $x = 9$ so Sarah is 9 years and Michelle is 5(9)-10 = 35 years.

16. Let the short board = x and the longer one be 3x + 1. Write the equation.

$$x + 3x + 1 = 21$$

 $4x + 1 = 21$
 $4x + 1 - 1 = 21 - 1$
 $4x = 20$
 $x = 5$ so the short board is 5 ft. and the longer is $3(5) + 1 = 16$ ft.

17. x + 12.3% of x is now \$2.83 per gallon x + 0.123x = \$2.83

1.123x = \$2.83x = \$2.52 per gallon

18. P - 22% of P is now 28,000 people, after 8 years

P - 0.22P = 28,000

0.78P = 28,000

P = 35,897.4359 = 35,898 whole people 8 years ago

Now divide the amount of decrease in population by 8 years to get a rough average yearly decrease in population:

35,898 - 28,000 = 7898 people in 8 years

7898/8 = 987.25 or about 988 people per year decrease in population

19. The average of the four grades needs to equal at least 84 so:

$$(75 + 82 + 80 + x)/4 = 84$$

[multiply by 4]

$$75 + 82 + + 80 + x = 336$$

$$237 + x = 336$$

x = 99 is the least the student can make an have an overall average of 84

20. Let L = lot value, H = house value = 7.5L

L + 7.5L = \$152,000

8.5L = \$152,000

L = \$17,882.35294 or about \$17,882 for the lot

H = 7.5L = \$134,117.6471 or about \$138,118 for the house

Chapter 2

Practice Set 2-1

1. Let L = 360 ft and W = 160 ft.

$$P = 2L + 2W$$

$$P = 2(360 \text{ ft}) + 2(160 \text{ ft}) = 720 \text{ ft} + 320 \text{ ft} = 1040 \text{ ft}$$

2. Let d = 8 ft

$$C = \pi d$$

$$C = \pi(8) = (3.14159)(8) \approx 25.1 \text{ ft}$$

3. Let L = 15 ft and W = 11 ft.

$$A = LW = (15 \text{ ft})(11 \text{ ft}) = 165 \text{ ft}^2$$

 $1 \text{ yd}^2 = 9 \text{ ft}^2$ so divide by 9 to convert to square yards.

$$165 \text{ ft}^2 \div 9 \text{ ft}^2/\text{yd}^2 = 18.3 \text{ yd}^2$$

4. Let r = 10 ft.

$$A = \pi r^2 = \pi (10 \text{ ft})^2 \approx 314.159 \text{ ft}^2$$

Since this is half a circle, divide this answer by 2.

$$314.159 \text{ ft}^2 \div 2 \approx 157.1 \text{ ft}^2$$

- 5. A square has 4 equal sides. P = 4L = 54 in., so L = 13.5 in per side. The area of a square is given by the formula: $A = L^2 = (13.5 \text{ in})^2 = 182.25 \text{ in}^2$.
- 6. A = lw

$$65 \text{cm}^2 = (13 \text{cm})(\text{w})$$

$$5cm = w$$

$$P = 21 + 2w = 2(13cm) + 2(5cm) = 36cm$$

7. Use the formula for the area of a rectangle to calculate the size of the area to be planted.

$$A = lw = (8.75 \text{ ft})(4.5 \text{ ft}) = 39.375 \text{ ft}^2$$

Since she needs four plants for every square foot, you should multiply this answer by 4. This gives 39.375 * 4 = 157.5 plants. In a practical sense, using this answer means you should buy 158 plants. If you round the area off to 40 ft² and multiply by 4, you would get 160 plants.

8. Find the circumference of the circular walkway with a diameter = 50 ft.

 $C = \pi d$