

Solutions Manual

INTRODUCTION TO HYDROLOGY

FIFTH EDITION

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CHAPTER 1

- 1.1 $100 \times 10^6 \times 0.02 = 2 \times 10^6 \text{ m}^3$
1 acre-ft = 43,560 cubic feet
cubic meters $\times 35.31 =$ cubic feet
 $(2 \times 10^6 \times 35.31) / 43,560 = 1,612.2 \text{ acre-ft}$
- 1.2 volume/volume per unit time = time
 $(500,000 \times 0.3) / (0.5) = 300,000 \text{ sec.}$
 $300,000 / 3,600 = 83.3 \text{ hours}$
- 1.3 $(450 + 500) / 2 - (500 + 530) / 2 = \text{avg. inflow} - \text{avg. outflow}$
the change in storage is thus - 40 cfs
 $-40 \times 3600 / 43560 = -3.31$, the change in storage in acre-ft.
The initial storage is thus depleted by 3.31 ac-ft
 $3.31 \times 43,560 / 35.31 = 4,083 \text{ cubic meters}$
- 1.4 $125 / 365 = 0.34 \text{ cm/day} = 0.035 \text{ cm/day}$
 $0.34 / 2.54 = 0.13 \text{ in./day}$
- 1.5 volume = $5280 \times 5280 \times 0.5 = 13,939,220 \text{ cubic feet}$
 $V/Q = \text{time}$
 $13,939,220 \times 3600 / 12 = 1,161,600 \text{ sec, or } 322.7 \text{ hr, or } 13.4 \text{ days}$
- 1.6 $ET = P - R$
 $R = (140 \times 3600 \times 24 \times 365) / (10,000 \times 1000^2) =$
0.44 m/yr or 44 cm/yr
 $ET = 105 - 44 = 61 \text{ cm/yr}$
This is a crude estimate.
- 1.7 equivalent depth = vol/area
inflow = $25 \times 3600 \times 24 \times 365 = 788,400 \text{ cubic feet/yr}$
inflow / $(3650 \times 43560) = 4.96 \text{ ft/yr}$
 $E = 100 \times 365 / 3650 = 10.0 \text{ ft/yr}$
Hence there is a drop in level of 5.04 ft
- 1.8 $I_{\text{avg.}} - O_{\text{avg.}} = \text{change in storage per unit time}$
 $(20 - 18) \times 3600 = 7,200 \text{ cubic meters}$
The storage is thus increased by 7,200 cubic meters
resulting in a final storage of 27,200 cubic meters

CHAPTER 2

Problems in this chapter are to be developed by the instructor.

CHAPTER 3

3.1 – 3.4 To be assigned by instructor.

3.5 For the James River rainfall:

<u>Interval in.</u>	<u>f</u>	<u>Σf</u>	<u>P(x)</u>	<u>F(x)</u>
(36-37)	2	2	0.057	0.057
(38-39)	4	6	0.114	0.171
(40-41)	7	13	0.200	0.371
(42-43)	9	22	0.257	0.628
(44-45)	5	27	0.143	0.771
(46-47)	4	31	0.114	0.885
(48-49)	2	33	0.057	0.942
(50-51)	2	35	0.057	0.999 1.000

- a) $P(\text{MAR} \geq 40) = 1.000 - 0.171 = 0.829 = 82.9\%$
- b) $P(\text{MAR} \geq 50) = 0.057 = 5.7\%$
- c) $P(40 \leq \text{MAR} \leq 50) = 0.942 - 0.171 = 0.771 = 77.1\%$

3.6 Using the curve data for a standard normal curve (Table B.1) requires standardization of the limits of the integral,

$$z = \frac{x - \bar{x}}{S} = \frac{8 - 4}{2} = 2$$

From Table B.1, the integral is the area to the right of $F(z = 2)$, or $0.5 - 0.4772 = 0.0228$.

3.7 For the data given:

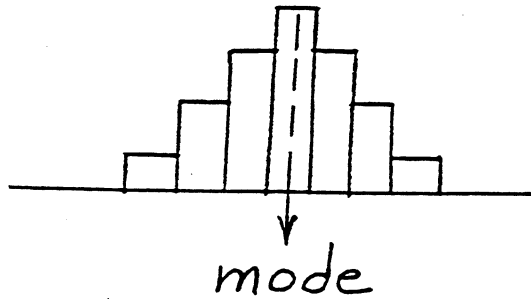
- a) The area under the curve must be 1.0 to qualify as a probability density function,

$$A = \int_0^b f(x)dx = \frac{b^3}{8} = 1.0$$

This gives $b = 2.0$

- b) This is the area between 0.0 and 0.5, or $0.5^3/8 = 0.016$

3.8 The histogram is symmetric, has zero skew, and mean = median = mode.



Sketch for Prob. 3.8

Since area to right of mode is 50%, $F(\text{mode}) = 50\%$ and $T = 2$ yr.

3.9 Given $\bar{x} = 10.3$, $s = 1.1$, $C_v = 0.11$, $n = 20$

$$S.E.(\bar{x}) = s/\sqrt{n} = 1.1/\sqrt{20} = 0.245$$

$$S.E.(s) = s/\sqrt{2n} = 1.1/\sqrt{40} = 0.0174$$

$$S.E.(C_v) = C_v\sqrt{1+2C_v^2}/\sqrt{2n} = 0.11\sqrt{1+2(0.11)^2}/\sqrt{40} = 0.017$$

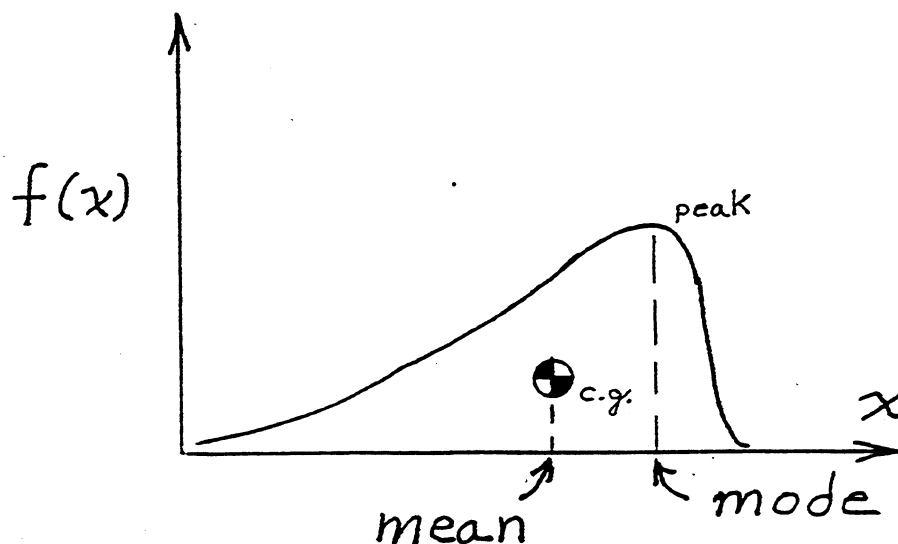
$$95\% \text{ C.L.: } z = \pm 1.96$$

$$\bar{x} \pm 1.96 (S.E._x) = 10.3 \pm 0.48$$

$$= \{10.78 \text{ to } 9.82\}$$

3.10 Because the median divides the area in half, most of the area would be to the right of the median. The distribution is probably skewed right.

3.11 Sketch:



Sketch of p.d.f. for Prob. 3.11

a) Left skewed

b) Negative because Pearson skew = (mean - mode)/s_x

3.12 For the 30,000 cfs value:

$$T_r = \frac{60 \text{ yrs}}{3 \text{ times}} = \underline{\underline{20 \text{ yrs}}}$$

3.13 Frequency analysis:

a)

<u>m</u> <u>rank</u>	<u>Peak</u> <u>value</u>	<u>F =</u> <u>$\frac{m}{10}$</u>	<u>$T_r = 1/F$</u>
1	1000	.1	10
2	900	.2	5
3	800	.3	3.33
4	700	.4	2.5
5	600	.	.
6	500	.	.
7	400	.	.
8	300		
9	200		
10	100		

By interpolation, 4-yr value is

$$800 + \frac{4 - 3.33}{5 - 3.33} (100)$$

$$= 840 \text{ cfs}$$

b) Using Table B.1,

$$Q_{4\text{-yr}} = \bar{Q} + K s_Q = 550 + .67(300) = 750 \text{ cfs}$$

3.14 For an annual precipitation of 30 in.

$$a) \quad P(x \geq 30) = G(30)$$

$$z = (30 - 27.6)/6.06 = 0.396$$

$$F(z) = 0.15392$$

$$G(30) = 0.5 - 0.15392 = 0.346$$

$$\begin{aligned} \text{b) Risk in 3 years} &= 1 - (1 - G(30))^3 \\ &= 0.720 \end{aligned}$$

$$\text{c) } P(\text{all three years}) = G(30)^3 = 0.041$$

$$3.15 \quad P(E_1 \cup E_2) = P(E_1) + P(E_2) - P(E_1 \cap E_2)$$

$$\begin{aligned} \text{a) If } E_1 \text{ and } E_2 \text{ are independent, } P(E_1|E_2) &= P(E_1) \\ \text{and } P(E_1 \cap E_2) &= P(E_1) \times P(E_2) \\ P(E_1 \cup E_2) &= 0.3 + 0.3 - 0.3 \times 0.3 = 0.51 \end{aligned}$$

$$\begin{aligned} \text{b) If dependent, with } P(E_1|E_2) &= 0.1, \\ P(E_1 \cap E_2) &= 0.1 \times 0.3 = 0.03 \\ \text{and } P(E_1 \cup E_2) &= 0.3 + 0.3 - 0.03 = 0.57 \end{aligned}$$

$$3.16 \quad P(A) = 0.4, P(\text{no } A) = P(\bar{A}) = 1 - 0.4 = 0.6$$

$$P(B) = 0.5, P(\text{no } B) = P(\bar{B}) = 1 - 0.5 = 0.5;$$

A and B independent

$$\text{a) } P(A \cap B) = P(A) \times P(B) = 0.4 \times 0.5 = 0.20$$

$$\text{b) } P(A \cap B) = P(\bar{A}) \times P(\bar{B}) = 0.6 \times 0.5 = 0.30$$

$$\begin{aligned} 3.17 \quad P(E_1|E_2) &= 0.9, P(E_2|E_1) = 0.2, P(E_1 \cap E_2) = 0.1 \\ P(E_1) &= P(E_1 \cap E_2)/P(E_2|E_1) = 0.1/0.2 = 0.5 \\ P(E_2) &= P(E_1 \cap E_2)/P(E_1|E_2) = 0.1/0.9 = 0.111 \end{aligned}$$

3.18 Two random events that are:

- a) Mutually exclusive:
 - A: Precipitation today exceeds 4 in.
 - B: Precipitation today does not exceed 3"
- b) Dependent:
 - A: Precipitation today exceeds 4 in.
 - B: Runoff today exceeds 1 in.
- c) Mutually exclusive and dependent:
 - A: Precipitation today does not exceed 4 in.
 - B: Runoff today exceeds 6 in.
- d) Neither mutually exclusive nor dependent:
 - A: Today's precipitation exceeds 4 in.

B: Groundwater pumpage this year will exceed 3 acre-feet per acre

3.19 $P(A) = 0.4, P(B) = 0.5$

a) $P(A \cap B) = P(A) P(B|A) = 0.4(0.5) = 0.20$

b) $P(\bar{A} \cap \bar{B}) = 0.6(0.5) = 0.30$

c) $P(\bar{A} \cap \bar{B}) = P(A) P(B) = 0.6(0.5) = 0.30$

3.20 For the given data:

a) Only if $P(B|A) = P(B)$

Now, $P(B) = 0.6$

$$P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$$

Since $P(A \text{ and } B) = 0.2$ and $P(A) = 0.4$

$P(B|A) = \frac{0.2}{0.4} = 0.5$, Dependent

b) No, mutually exclusive if $P(A \text{ and } B) = 0$, but $P(A \text{ and } B) = 0.2$

c) $P(B) = 0.6$

d) $P(\bar{A}) = 1 - 0.4 = 0.6$

e) $P(\bar{A} \text{ and } \bar{B}) = P(\bar{B}|\bar{A}) P(\bar{A})$

From data, $P(\text{both}) = 0.2$

Check: $P(\bar{A} \text{ and } \bar{B}) = 1 - P(E_1) - P(E_2) - P(E_3)$

Possibles:	Warm Mar	Cold Mar	Warm Mar	Cold Mar
	Apr Flood	Apr Flood	Apr Dry	Apr Dry
	$P = 0.2$	$P = 0.4$	$P = 0.2$	$P = 0.2$

f) $P(B|A) = 0.5$

g) to make them independent,

$$P(B|A) = P(B)$$

Since $P(B) = 0.6$

$$P(B|A) = \frac{P(A \text{ and } B)}{P(A)} = \frac{0.2}{0.4} = 0.5$$

Change $P(B)$ to 0.5, without changing $P(A \text{ and } B)$

- 3.21 A: Flood
B: Ice-jam

$$P(A \text{ and } B) = P(A|B)P(B), \text{ thus } P(A \text{ and } B) < P(A|B)$$

$$\text{and } P(A \text{ and } B) < P(A)$$

$$\text{Also } P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\text{Also } P(A) < P(A|B) \text{ because } B < S$$

$$\text{Ranking: Largest} = P(A \text{ or } B)$$

$$\text{Second} = P(A|B)$$

$$\text{Third} = P(A)$$

$$\text{Fourth} = P(A \text{ and } B)$$

- 3.22 For the information given:

- a) Both statements say the same thing when $\underline{n} = \underline{t} = T_r$ years,
or $T_r = 1$ yr

- b) First:

$$\left(1 - \frac{1}{T}\right)^{t-1} = \left(1 - \frac{1}{3}\right)^{t-1} = \left(\frac{2}{3}\right)^2 = \frac{4}{9} = 0.444$$

Second: P = Probability annual precipitation value will not be equaled or exceeded in any single year,

$$P = 1 - F_x = 1 - \frac{1}{3} = \frac{2}{3}$$

$$\frac{n!}{r!(n-r)!} P^{n-r} (1-P)^r = \frac{3!}{1!(2)!} \left(\frac{2}{3}\right)^{3-1} \left(1 - \frac{2}{3}\right)^1 = \underline{\underline{4/9}}$$

- 3.23 For risk = 50%, $R = 0.5 = 1 - (1 - 1/T)^2$

for 2 consecutive yr

Solution gives $T = 3.41$ yr

For risk = 100%, $R = 1 = 1 - (1 - 1/T)^2$, $T = 1$ yr

- 3.24 For the temporary cofferdam:

- a) $P(\text{overtopping in any yr}) = P(F) = 1/T = 1/20 = 0.05$
- b) $P(\text{non-exceed in yr 1 and non-exceed in yr 2 and exceed in yr 3}) = P(F) \times P(F) \times P(F) = 0.95 \times 0.95 \times 0.5 = 0.451$
- c) $\text{Risk} = 1 - (1 - 1/T)^n$
 $1 - (1 - 1/20)^5 = 0.226$
- d) $P(\text{non-exceed in 5 consecutive yr})$
 $= (1 - 1/20)^5 = 0.774$

3.25 For $N = 33$, median = 17th largest flow.

Defining Q as the annual peak:

- a) $P(Q \text{ exceeds median}) = 17/33 = 0.515$
- b) $T_r = 1/G(Q) = 1/0.515 = 1.94 \text{ yrs.}$
- c) $G(Q) = 0.515 \text{ in any year.}$
- d) $1 - G(Q) = 0.485$
- e) $P(Q < \text{median in all 10 yrs})$
 $= P(Q \cap Q \cap Q \cap Q \dots) = (0.485)^{10} = 0.00072$
- f) $P(Q \geq \text{median at least once in 10 years})$
 $= 1 - (1 - G(Q))^{10} = 0.99928$
- g) $P(Q_1 \text{ and } Q_2 \text{ exceed median})$
 $= P(Q_1) P(Q_2)$
 $= G(Q) G(Q) = 0.265$
- h) $P(Q_1 \text{ exceeds median and } Q_2 \text{ does not})$
 $G(Q)(1 - G(Q)) = 0.250$

3.26 For the temporary floodwall:

- a) $P(\text{overtopping in any yr}) = P(F) = 1/T = 1/20 = 0.05$
- b) $P(\text{non-exceed in 3 consecutive yr}) = (1 - P(F))^3$
 $= P(\bar{F})^3 = 0.95^3 = 0.857$
- c) $\text{Risk} = 1 - (1 - 1/T)^N = 1 - (1 - 1/20)^3 = 0.143$
- d) $P(\text{exceed in 1st yr only or exceed in 2nd yr only or 3rd yr only})$
 $= P(\text{in 1st yr only}) + P(\text{in 2nd yr only}) + P(\text{in 3rd yr only})$
 $= P(F) \times P(\bar{F}) \times P(\bar{F}) + P(\bar{F}) \times P(F) \times P(\bar{F}) + P(\bar{F}) \times P(\bar{F}) \times P(F)$
 $= (0.05)(0.95)(0.95) + (0.95)(0.05)(0.95) + (0.95)(0.95)(0.05) = 0.135$
- e) $P(\text{exceed in 3rd yr exactly}) = P(\bar{F}) \times P(\bar{F}) \times P(F)$
 $= (0.95)(0.95)(0.05) = 0.045$

3.27 The owner's acceptance level is:

$$\text{Risk} = 1 - (1 - 1/T_r)^n = 0.25$$

Substitution of $n = 20$ gives $T_r = 70$ yrs, thus the wall should be between 8.5 and 10.0 ft, or interpolating, 9.1 ft.

3.28 For Oak Creek:

a) $\text{Freq.} = m/N = 3/60 = 0.05$

b) $P(F) = \text{freq.} = 0.05$

c) $T = 1/P(F) = 1/0.05 = 20 \text{ yr}$

d) $P(\bar{F}) = 1 - P(F) = 1 - 0.05 = 0.95$

e) $P(\text{non-exceed in two consecutive yr}) = P(\bar{F}) \times P(\bar{F}) = 0.95 \times 0.95 = 0.9025$

f) $P(\text{one or more exceed in 20 yr}) = \text{Risk}$
 $= 1 - (1 - 1/T)^N$
 $= 1 - (1 - 0.05)^{20} = 0.642$

g) $P(\text{non-exceed in one yr and exceed in next yr})$
 $= P(\bar{F}) \times P(F)$
 $= 0.95 \times 0.05 = 0.0475$

h) Using Binomial Theorem, $P(3 \text{ occurrences in } 60 \text{ yr})$
 $= P(x \text{ in } n)$
 $= [n!/x!(n-x)!] p^x (1-p)^{n-x}$
 $= [60!/3! 57!](0.05)^3 (0.95)^{57} = 0.230$

i) Same as part f).

3.29 For Anniston, Alabama,

Mean rain = 57.2 in.

Standard deviation = 15.5 in.

100-yr $X = 57.2 + K(15.5)$

From Appendix B, K for 0.01 = 2.326,

$$X_{100} = 93.2 \text{ in.}$$

The 1988 depth of 99 inches was the greatest depth of record. It has an apparent recurrence interval of 23 years. If the rain is normally distributed,

$$99 = 57.2 + K_{99}(15.5)$$

$$K_{99} = 2.697$$

The area to the right of 2.697 is .49647, giving a recurrence interval of $1/.00353 = 283$ years.

$$3.30 \quad P(\mu < x < \mu + \sigma) = \text{area from } z = 0 \text{ to } z = 1 = 0.3413 = 34.13\%$$

$$3.31 \quad P(\mu - 3\sigma \leq X \leq \mu + 3\sigma) = \text{area under standard normal from } -3 \text{ to } +3$$

From Appendix C.1:

$$P(\mu - 3\sigma \leq x \leq \mu + 3\sigma) = 2(.4987) = 0.997 \text{ or } = 99.74 \%$$

3.32 For Normal distribution of runoff:

$$x = \bar{x} + zs, \quad s = \sqrt{9} = 3$$

$$11 = 14 + 3z, \quad z = -1.0, \quad F(z) = 0.3413$$

$$P(x \leq 11) = 0.5000 - 0.3413 = 0.1583 \text{ in any yr}$$

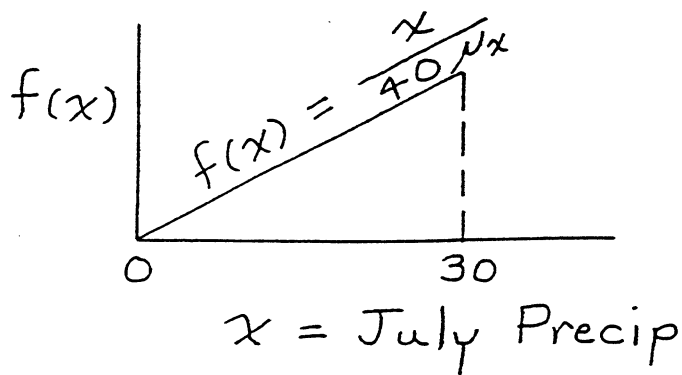
$$P(x \leq 11 \text{ in 3 consecutive yrs}) = 0.1588^3 = 0.004 = 0.4\%$$

3.33 From Table B.1, the standard variate, z , with area to the right of 0.330 is 0.44 (area left = $F(z) = 0.5 - 0.33 = 0.17$). Thus,

$$\begin{aligned} x &= \bar{x} + zs \\ &= 5 + 0.44(1.0) = 5.44 \end{aligned}$$

$$3.34 \quad \text{Since } \mu = 0, \sigma = 1, \text{ then } \int_{-2}^2 f(z) dz = 2(0.4772) = 0.9544$$

3.35 Given:



Prob. 3.35 Definition Sketch

$$\mu_x \approx 30 \text{ in.}$$

$$a) P(x \leq 20 \text{ in.}) = \text{area left of 20 in.} = 1/2bh = 0.1667$$

$$\begin{aligned} b) P(x \geq 30 \text{ in.}) &= \text{area right of 30 in.} \\ &= 1 - \text{area left of 30 in.} \\ &= 1 - 15/40 = 0.625 \end{aligned}$$

3.36 The function is a triangle. For this shape,

$$a) P(X < 20 \text{ in.}) = \text{area left of 20.0, or } 20^2/2400 = 0.167$$

$$\begin{aligned} b) P(X \geq 30 \text{ in.}) &= \text{area right of 30.0,} \\ &\text{or } 1.0 - \text{area left of 30.0, } = 1 - 30^2/2400 = 0.625 \end{aligned}$$

3.37 Using Table B.1:

$$\begin{array}{cccccccccc} \text{a.} & \text{b.} & \text{c.} & \text{d.} & \text{e.} & \text{f.} & \text{g.} & \text{h.} & \text{i.} & \text{j.} \\ 2 & 6 & 10 & 7 & 9 & 4 & 5 & 1 & 8 & 3 \end{array}$$

3.38 September precipitation statistics:

$$\bar{x} = 65.5^\circ, s = \sqrt{39.3} = 6.27^\circ$$

a) Approx. limits are $\bar{x} \pm s$. $F(z) = 0.33$,

$$z = \pm 0.9$$

$$\bar{x} \pm zs = 65.5 \pm 0.97(6.27) = 65.5 \pm 6.1$$

$$= \{71.6 \text{ and } 59.4\}$$

b) Middle 95% = 47.5% either side of mean

$$F(z) = 0.475, z = \pm 1.96$$

$$\begin{aligned} \bar{x} \pm s &= 65.5 \pm 1.96(6.27) = 65.5 \pm 12.3 \\ &= \{77.8 \text{ and } 53.2\} \end{aligned}$$

c) $F(z) = 0.80 - 0.50 = 0.30$; $z = 0.84$

$$\begin{aligned} x_{80} &= \bar{x} + zs = 65.5 + 0.84(6.27) \\ &= 65.5 + 5.3 = 70.8^\circ \end{aligned}$$

d) 10-yr $F(z) = 0.50 - 0.10 = 0.40$, $z = 1.28$

$$x_{90} = \bar{x} + zs = 65.5 + 1.28(6.27) = 73.5^\circ$$

100-yr $F(z) = 0.50 - 0.01 = 0.49$, $z = 2.33$

$$x_{99} = \bar{x} + zs = 65.5 + 2.33(6.27) = 8.01^{\circ}$$

3.39 $\bar{x} = 3275$; s (computed) = 442, graphical est. at $(x_{84.1} - x_{15.9})/2$

3.40 30-min intensity from 60 yrs record

45 values ≥ 2.5 in./hr

5-yrs, none > 2.5 in./hr

a) T_r of 2.5 in./hr by P-D series:

$$= \frac{100}{F_{\text{Kimball}}} = \frac{100}{m/N+1} = \frac{100(61)}{85} = \underline{0.72 \text{ yrs}}$$

b) T_r of 2.5 in./hr by annual series:

$$= \frac{100}{F} = \frac{100(61)}{55} = \underline{1.11 \text{ yrs}}$$

3.41 For the peaks given:

Order (m)	Annual Series (Q)	Partial Series (Q)	$T =$ $(n+1)/m$
1	800	800	11.0
2	700	700	5.50
3	400	700	3.67
4	300	400	2.75
5	100	300	2.20
6	80	100	1.83
7	80	90	1.57
8	60	90	1.37
9	40	90	1.22
10(=n)	30	80	1.10

Q_{100} (Annual Series): $T = 2.20$ yrs

Q_{100} (Partial Series): $T = 1.83$ yrs

3.42 For the data given:

a) Annual series:

<u>Yr</u>	<u>Value</u>	<u>$T_r = N/m = 10/m$</u>
69	6"	10
71	5"	5
68	4"	3.33
66	3"	2.5
63	2"	2

Thus, 2" value has $T_r = 2$ years

b) Partial-Duration series:

<u>Value</u>	<u>$T_r = 10/m$</u>
6	10
5	3.33
5	3.33
4	2.5
3	2
2	10/6

Thus, 2" value has $T_r = 10/6$ yrs = 1.67 yrs

c)

<u>Value</u>	<u>T_r</u>
6"	10
5"	3.333

Interpolating, $X_8 = 6 \text{ in.} - 2/6.67 (1 \text{ in.}) = 5.70 \text{ in.}$

If interpolate by frequency:

<u>X</u>	<u>F_x</u>
6"	.1
x	.125
5	.3

Giving,

$$X_8 = 5 + 0.175/0.2 (1) = 5.875 \text{ in.}$$

(Either answer OK)

3.43 For the data given:

a) For partial series, the 30-min value was equaled or exceeded 85 times, thus

$$T = n+1/m = 61/85 = 0.72$$

b) For annual series, $m = 55$ and

$$T = 61/55 = 1.109$$

3.44 The function would be linear on:

a) Probability (Normal) paper

- b) Extreme-value (Gumbel) paper
- c) Rectangular coordinate paper ($Y = 3X+4$)
- d) Log-probability paper (Lognormal)
- e) Probability (A Pearson III with $g = 0$ is normal) paper
- f) Log-Log ($\bar{Q} = 43 A^{0.7}$)
- g) Log-probability paper (same as log-normal = Log-Pearson III with $g_{\log s} = 0$)
- h) None (Pearson III with $g = 3$)

3.45 $C_{s_x} = 0.879$ $C_{s_y} = 0.2775$

<u>Log normal Est.</u>	<u>50-yr</u>	<u>100-yr</u>
$K(C_s = 0)$	2.054	2.326
$y = \bar{y} + K_{s_y}$	3.490	3.531
$x = \log^{-1}y$	3171 cfs	3483 cfs

Log Pearson III

$K(C_s = 0.28)$	2.201	2.530
$y = \bar{y} + K_{s_y}$	3.5119	3.5611
$x = \log^{-1}y$	3250 cfs	3640 cfs

Gumbel

$K(n = 20) =$	3.179	3.836
$x = \bar{x} + K_{s_x} =$	3453 cfs	3832 cfs

3.46 $\bar{R} = 14$ in.

$s = 3$ in.

$P(R < 8 \text{ in. in yr 2 of 3 yrs})$

$= P(R > 8 \cap R < 8 \cap R > 8) = P(\bar{E}) P(E) P(\bar{E})$

$P(R < 8 \text{ in.}) = F(R)$

$8 \text{ in.} = 14 \text{ in.} + K(3 \text{ in.})$

$K = (8-14)/3 = -2.0$

Thus $F(8 \text{ in.}) = P(E) = 0.5 - 0.4772 = 0.0228$

Thus $P(2\text{nd yr only}) = (0.9772)(0.0228)(0.9772) = 0.022$

3.47 $Q = \bar{Q} + K_s$

$$32,000 = 30,000 + K(1,000)$$

$$K = 2.0$$

$$\text{Thus } F(Q) = 0.5 + 0.4772 = 0.9772$$

$$G(Q) = 0.0228$$

$$T_r = 43.9 \text{ yrs}$$

3.48 For the precipitation data given:

- a) The graph would plot as a straight line on probability paper, with the mean of 27.6 having a 50% exceedance probability. A second point, or any number of points, can be generated from

$$x_T = \bar{x} + z_T s$$

Where z_T is the standard normal variate (Table B.1) corresponding to the value $T = 1/G(x)$ where $G(x)$ is the exceedance probability. For example, an exceedance of $G(x) = 0.33$ corresponds to $z = 0.44$ from Table B.1. The corresponding T is $1/0.33 = 3.03$, and $x = 27.6 + 0.44(6.06) = \underline{30.27}$

- b) Assuming the 1972 drought was the smallest value in 80 years, it has an apparent frequency of $80/81 = 0.988$. For a value of 14 in., the corresponding z is -2.24. From Table B.1, $F(z) = 0.4875$. Thus the probability of exceedance is $.4875 + 0.50 = 0.9875$.
- c) The apparent recurrence interval for the highest value is 81 years, using $T = N+1/m$, where m is the rank. The normal distribution gives $z = (42 - 27.6)/6.06 = 2.376$. This gives $F(z) = 0.49122$, and $G(x) = 0.00878$. Because $T = 1/G(x)$, $T = 114$ years.

3.49 For normal distribution, $T = 2$ and $P = 1/2 = 0.5$ occurs at mean: $X = 40,000$ cfs

$$\text{For } T = 10 \text{ and } P = 1/10 = 0.10, F(z) = 0.50 - 0.10 = 0.40: z = 1.282$$

$$\text{Therefore, } X = \bar{X} + zs$$

$$52820 = 40000 + 1.28s, s = 10,000 \text{ cfs}$$

$$\text{For } T = 25 \text{ and } P = 1/25 = 0.04, F(z) = 0.50 - 0.04 = 0.46, \text{ thus } z = 1.75$$

$$X_{25} = \bar{X} + zs = 4000 + 1.75(10000) = 57,500 \text{ cfs}$$

3.50 Find 25-yr flood: