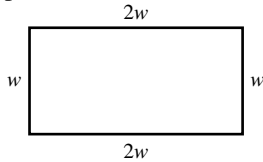


## Chapter 1

### Problems 1.1

1. Let  $w$  be the width and  $2w$  be the length of the plot.



Then area = 800.

$$(2w)w = 800$$

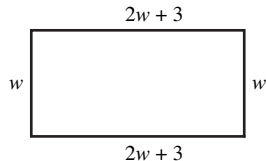
$$2w^2 = 800$$

$$w^2 = 400$$

$$w = 20 \text{ ft}$$

Thus the length is 40 ft, so the amount of fencing needed is  $2(40) + 2(20) = 120$  ft.

2. Let  $w$  be the width and  $2w + 3$  be the length.



Then perimeter = 300.

$$2w + 2(2w + 3) = 300$$

$$6w + 6 = 300$$

$$6w = 294$$

$$w = 49 \text{ ft}$$

Thus the length is  $2(49) + 3 = 101$  ft.

The dimensions are 49 ft by 101 ft.

3. Let  $n$  = number of ounces in each part. Then we have

$$4n + 5n = 145$$

$$9n = 145$$

$$n = 16\frac{1}{9}$$

Thus there should be  $4\left(16\frac{1}{9}\right) = 64\frac{4}{9}$  ounces of

A and  $5\left(16\frac{1}{9}\right) = 80\frac{5}{9}$  ounces of B.

4. Let  $n$  = number of cubic feet in each part.

Then we have

$$1n + 3n + 5n = 765$$

$$9n = 765$$

$$n = 85$$

Thus he needs  $1n = 1(85) = 85 \text{ ft}^3$  of portland

cement,  $3n = 3(85) = 255 \text{ ft}^3$  of sand, and

$5n = 5(85) = 425 \text{ ft}^3$  of crushed stone.

5. Let  $n$  = number of ounces in each part. Then we have

$$2n + 1n = 16$$

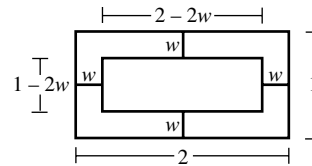
$$3n = 16$$

$$n = \frac{16}{3}$$

Thus the turpentine needed is

$$(1)n = \frac{16}{3} = 5\frac{1}{3} \text{ ounces.}$$

6. Let  $w$  = width (in miles) of strip to be cut. Then the remaining forest has dimensions  $2 - 2w$  by  $1 - 2w$ .



Considering the area of the remaining forest, we have

$$(2 - 2w)(1 - 2w) = \frac{3}{4}$$

$$2 - 6w + 4w^2 = \frac{3}{4}$$

$$8 - 24w + 16w^2 = 3$$

$$16w^2 - 24w + 5 = 0$$

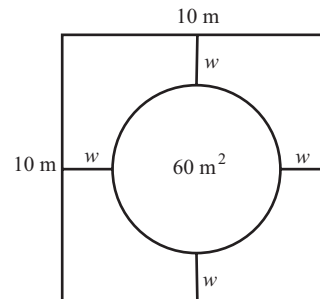
$$(4w - 1)(4w - 5) = 0$$

Hence  $w = \frac{1}{4}, \frac{5}{4}$ . But  $w = \frac{5}{4}$  is impossible since

one dimension of original forest is 1 mi. Thus

the width of the strip should be  $\frac{1}{4}$  mi.

7. Let  $w$  = "width" (in meters) of the pavement. Then  $5 - w$  is the radius of the circular flower bed.



Thus

$$\begin{aligned}\pi r^2 &= A \\ \pi(5-w)^2 &= 60 \\ w^2 - 10w + 25 &= \frac{60}{\pi} \\ w^2 - 10w + \left(25 - \frac{60}{\pi}\right) &= 0 \\ a = 1, b = -10, c = 25 - \frac{60}{\pi} \\ w &= \frac{-b \pm \sqrt{100 - 4\left(1\right)\left(25 - \frac{60}{\pi}\right)}}{2} \approx 9.37, 0.63\end{aligned}$$

Since  $0 < w < 5$ ,  $w \approx 0.63$  m.

8. Since diameter of circular end is 140 mm, the radius is 70 mm. Area of circular end is  $\pi(\text{radius})^2 = \pi(70)^2$ . Area of square end is  $x^2$ .

Equating areas, we have  $x^2 = \pi(70)^2$ .

Thus  $x = \pm\sqrt{\pi(70)^2} = \pm 70\sqrt{\pi}$ . Since  $x$  must be positive,  $x = 70\sqrt{\pi} \approx 124$  mm.

9. Let  $q$  = number of tons for \$560,000 profit.

Profit = Total Revenue - Total Cost

$$560,000 = 134q - (82q + 120,000)$$

$$560,000 = 52q - 120,000$$

$$680,000 = 52q$$

$$\frac{680,000}{52} = q$$

$$q \approx 13,076.9 \approx 13,077 \text{ tons.}$$

10. Let  $q$  = required number of units.

Profit = Total Revenue - Total Cost

$$150,000 = 50q - (25q + 500,000)$$

$$150,000 = 25q - 500,000$$

$$650,000 = 25q, \text{ from which}$$

$$q = 26,000$$

11. Let  $x$  = amount at 6% and

$$20,000 - x = \text{amount at } 7\frac{1}{2}\%.$$

$$x(0.06) + (20,000 - x)(0.075) = 1440$$

$$-0.015x + 1500 = 1440$$

$$-0.015x = -60$$

$x = 4000$ , so  $20,000 - x = 16,000$ . Thus the investment should be \$4000 at 6% and \$16,000

at  $7\frac{1}{2}\%$ .

12. Let  $x$  = amount at 4% and

$120,000 - x$  = amount at 5%.

$$0.04x + 0.05(120,000 - x) = 0.045(120,000)$$

$$-0.01x + 6000 = 5400$$

$$-0.01x = -600$$

$$x = 60,000$$

The investment consisted of \$60,000 at 5% and \$60,000 at 4%.

13. Let  $p$  = selling price. Then profit =  $0.2p$ .

selling price = cost + profit

$$p = 3.40 + 0.2p$$

$$0.8p = 3.40$$

$$p = \frac{3.40}{0.8} = \$4.25$$

14. Following the procedure in Example 6 we obtain the total value at the end of the second year to be  $1,000,000(1+r)^2$ .

So at the end of the third year, the accumulated

amount will be  $1,000,000(1+r)^2$  plus the

interest on this, which is  $1,000,000(1+r)^2 r$ .

Thus the total value at the end of the third year

will be  $1,000,000(1+r)^2 + 1,000,000(1+r)^2 r$

$$= 1,000,000(1+r)^3.$$

This must equal \$1,125,800.

$$1,000,000(1+r)^3 = 1,125,800$$

$$(1+r)^3 = \frac{1,125,800}{1,000,000} = 1.1258$$

$$1+r \approx 1.04029$$

$$r \approx 0.04029$$

Thus  $r \approx 0.04029 \approx 4\%$ .

15. Following the procedure in Example 6 we obtain

$$3,000,000(1+r)^2 = 3,245,000$$

$$(1+r)^2 = \frac{649}{600}$$

$$1+r = \pm\sqrt{\frac{649}{600}}$$

$$r = -1 \pm \sqrt{\frac{649}{600}}$$

$$r \approx -2.04 \text{ or } 0.04$$

We choose  $r \approx 0.04 = 4\%$ .

16. Total revenue = variable cost + fixed cost

$$100\sqrt{q} = 2q + 1200$$

$$50\sqrt{q} = q + 600$$

$$2500q = q^2 + 1200q + 360,000$$

$$0 = q^2 - 1300q + 360,000$$

$$0 = (q - 400)(q - 900)$$

$$q = 400 \text{ or } q = 900$$

17. Let  $n$  = number of bookings.

$$0.90n = 81$$

$$n = 90 \text{ seats booked}$$

18. Let  $n$  = number of people polled.

$$0.20p = 700$$

$$p = \frac{700}{0.20} = 3500$$

19. Let  $s$  = monthly salary of deputy sheriff.

$$0.30s = 200$$

$$s = \frac{200}{0.30}$$

$$\text{Yearly salary} = 12s = 12\left(\frac{200}{0.30}\right) = \$8000$$

20. Yearly salary before strike =  $(7.50)(8)(260)$   
= \$15,600

$$\text{Lost wages} = (7.50)(8)(46) = \$2760$$

Let  $P$  be the required percentage increase (as a decimal).

$$P(15,600) = 2760$$

$$P = \frac{2760}{15,600} \approx 0.177 = 17.7\%$$

21. Let  $q$  = number of cartridges sold to break even.

total revenue = total cost

$$21.95q = 14.92q + 8500$$

$$7.03q = 8500$$

$$q \approx 1209.10$$

1209 cartridges must be sold to approximately break even.

22. Let  $n$  = number of shares.

$$\text{total investment} = 5000 + 20n$$

$$0.04(5000) + 0.50n = 0.03(5000 + 20n)$$

$$200 + 0.50n = 150 + 0.60n$$

$$-0.10n = -50$$

$$n = 500$$

500 shares should be bought.

23. Let  $v$  = total annual vision-care expenses (in dollars) covered by program. Then

$$35 + 0.80(v - 35) = 100$$

$$0.80v + 7 = 100$$

$$0.80v = 93$$

$$v = \$116.25$$

24. a.  $0.031c$

b.  $c - 0.031c = 600,000,000$

$$0.969c = 600,000,000$$

$$c \approx 619,195,046$$

Approximately 619,195,046 bars will have to be made.

25. Revenue = (number of units sold)(price per unit)  
Thus

$$400 = q \left[ \frac{80 - q}{4} \right]$$

$$1600 = 80q - q^2$$

$$q^2 - 80q + 1600 = 0$$

$$(q - 40)^2 = 0$$

$$q = 40 \text{ units}$$

26. If  $I$  = interest,  $P$  = principal,  $r$  = rate, and  $t$  = time, then  $I = Prt$ . To triple an investment of  $P$  at the end of  $t$  years, the interest earned during that time must equal  $2P$ . Thus

$$2P = P(0.045)t$$

$$2 = 0.045t$$

$$t = \frac{2}{0.045} \approx 44.4 \text{ years}$$

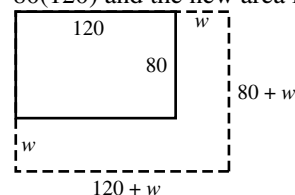
27. Let  $q$  = required number of units. Equate the incomes of each proposal.

$$5000 + 0.50q = 50,000$$

$$0.50q = 45,000$$

$$q = 90,000 \text{ units}$$

28. Let  $w$  = width of strip. The original area is  $80(120)$  and the new area is  $(120 + w)(80 + w)$ .



Thus

$$(120 + w)(80 + w) = 2(80)(120)$$

$$9600 + 200w + w^2 = 19,200$$

$$w^2 + 200w - 9600 = 0$$

$$(w + 240)(w - 40) = 0$$

$$w = -240 \text{ or } w = 40$$

We choose  $w = 40$  ft.

- 29.** Let  $n$  = number of \$20 increases. Then at the rental charge of  $400 + 20n$  dollars per unit, the number of units that can be rented is  $50 - 2n$ . The total of all monthly rents is  $(400 + 20n)(50 - 2n)$ , which must equal 20,240.  
 $20,240 = (400 + 20n)(50 - 2n)$   
 $20,240 = 20,000 + 200n - 40n^2$   
 $40n^2 - 200n + 240 = 0$   
 $n^2 - 5n + 6 = 0$   
 $(n - 2)(n - 3) = 0$   
 $n = 2, 3$   
 Thus the rent should be either  
 $\$400 + 2(\$20) = \$440$  or  $\$400 + 3(\$20) = \$460$ .

- 30.** Let  $x$  = original value of the blue-chip investment, then  $3,100,000 - x$  is the original value of the glamour stocks. Then the current value of the blue-chip stock is  $x + \frac{1}{10}x$ , or  $\frac{11}{10}x$ .

For the glamour stocks the current value is

$$(3,100,000 - x) - \frac{1}{10}(3,100,000 - x), \text{ which}$$

$$\text{simplifies to } \frac{9}{10}(3,100,000 - x).$$

Thus for the current value of the portfolio,

$$\frac{11}{10}x + \frac{9}{10}(3,100,000 - x) = 3,240,000$$

$$11x + 27,900,000 - 9x = 32,400,000$$

$$2x = 4,500,000$$

$$x = 2,250,000$$

Thus the current value of the blue chip

$$\text{investment is } \frac{11}{10}(2,250,000) \text{ or } \$2,475,000.$$

- 31.**  $10,000 = 800p - 7p^2$

$$7p^2 - 800p + 10,000 = 0$$

$$p = \frac{800 \pm \sqrt{640,000 - 280,000}}{14}$$

$$= \frac{800 \pm \sqrt{360,000}}{14} = \frac{800 \pm 600}{14}$$

$$\text{For } p > 50 \text{ we choose } p = \frac{800 + 600}{14} = \$100.$$

- 32.** Let  $p$  be the percentage change in market value.

$$(1 + 0.15)\left(\frac{P}{E}\right) = \frac{(1 + p)P}{(1 - 0.10)E}$$

$$1.15 = \frac{1 + p}{0.90}$$

$$1.035 = 1 + p$$

$$p = 0.035 = 3.5\%$$

The market value increased by 3.5%.

- 33.** To have supply = demand,

$$2p - 10 = 200 - 3p$$

$$5p = 210$$

$$p = 42$$

- 34.**  $2p^2 - 3p = 20 - p^2$

$$3p^2 - 3p - 20 = 0$$

$$a = 3, b = -3, c = -20$$

$$p = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-3) \pm \sqrt{(-3)^2 - 4(3)(-20)}}{2(3)}$$

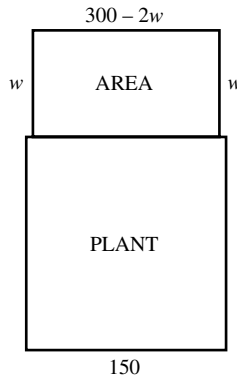
$$= \frac{3 \pm \sqrt{249}}{6}$$

$$p \approx 3.130 \text{ or } p \approx -2.130$$

The equilibrium price is  $p \approx 3.13$ .

- 35.** Let  $w$  = width (in ft) of enclosed area. Then length of enclosed area is

$$300 - w - w = 300 - 2w.$$



Thus

$$w(300 - 2w) = 11,200$$

$$2w(150 - w) = 11,200$$

$$w(150 - w) = 5600$$

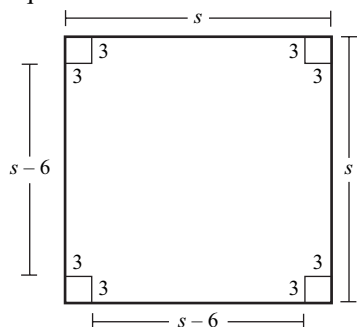
$$0 = w^2 - 150w + 5600$$

$$0 = (w - 80)(w - 70)$$

Hence  $w = 80, 70$ . If  $w = 70$ , then length is  $300 - 2w = 300 - 2(70) = 160$ . Since the building has length of only 150 ft, we reject

$w = 70$ . If  $w = 80$ , then length is  $300 - 2w = 300 - 2(80) = 140$ . Thus the dimensions are 80 ft by 140 ft.

36. Let  $s$  = length in inches of side of original square.



Considering the volume of the box, we have  
 (length)(width)(height) = volume  
 $(s - 4)(s - 4)(2) = 50$   
 $(s - 4)^2 = 25$   
 $s - 4 = \pm\sqrt{25} = \pm 5$   
 $s = 4 \pm 5$   
 Hence  $s = -1, 9$ . We reject  $s = -1$  and choose  $s = 9$ . The dimensions are 9 in. by 9 in.

37. Original volume =  $(10)(5)(2) = 100 \text{ cm}^3$   
 Volume increase =  $0.50(100) = 50 \text{ cm}^3$   
 Volume of new bar =  $100 + 50 = 150 \text{ cm}^3$   
 Let  $x$  = number of centimeters that the length and width are each increased. Then  
 $2(x + 10)(x + 5) = 150$   
 $x^2 + 15x + 50 = 75$   
 $x^2 + 15x - 25 = 0$   
 $a = 1, b = 15, c = -25$   
 $x = \frac{-15 \pm \sqrt{15^2 - 4(1)(-25)}}{2} \approx 1.51, -16.51$

We reject  $-16.51$  as impossible. The new length is approximately 11.51 cm, and the new width is approximately 6.51 cm.

38. Volume of old style candy  
 $= \pi(7.1)^2(2.1) - \pi(2)^2(2.1)$   
 $= 97.461\pi \text{ mm}^3$   
 Let  $r$  = inner radius (in millimeters) of new style candy. Considering the volume of the new style candy, we have

$$\begin{aligned}\pi(7.1)^2(2.1) - \pi r^2(2.1) &= 0.78(97.461\pi) \\ 29.84142\pi &= 2.1\pi r^2 \\ 14.2102 &= r^2 \\ r &\approx \pm 3.7696\end{aligned}$$

Since  $r$  is a radius, we choose  $r = 3.77 \text{ mm}$ .

39. Let  $x$  = amount of loan. Then the amount actually received is  $x - 0.16x$ . Hence,  
 $x - 0.16x = 195,000$   
 $0.84x = 195,000$   
 $x \approx 232,142.86$   
 To the nearest thousand, the loan amount is \$232,000. In the general case, the amount received from a loan of  $L$  with a compensating balance of  $p\%$  is  $L - \frac{p}{100}L$ .

$$\begin{aligned}L - \frac{p}{100}L &= E \\ \frac{100 - p}{100}L &= E \\ L &= \frac{100E}{100 - p}\end{aligned}$$

40. Let  $n$  = number of machines sold over 600. Then the commission on each of  $600 + n$  machines is  $40 + 0.04n$ . Equating total commissions to 30,800 we obtain  
 $(600 + n)(40 + 0.04n) = 30,800$   
 $24,000 + 24n + 40n + 0.04n^2 = 30,800$   
 $0.02n^2 + 32n - 3400 = 0$   
 $n = \frac{-32 \pm \sqrt{1024 + 272}}{0.04} = \frac{-32 \pm 36}{0.04}$   
 We choose  $n = \frac{-32 + 36}{0.04} = 100$ . Thus the number of machines that must be sold is  $600 + 100 = 700$ .

41. Let  $n$  = number of acres sold. Then  $n + 20$  acres were originally purchased at a cost of  $\frac{7200}{n + 20}$  each. The price of each acre sold was  $30 + \left[ \frac{7200}{n + 20} \right]$ . Since the revenue from selling  $n$  acres is \$7200 (the original cost of the parcel), we have

$$n \left[ 30 + \frac{7200}{n+20} \right] = 7200$$

$$n \left[ \frac{30n + 600 + 7200}{n+20} \right] = 7200$$

$$n(30n + 600 + 7200) = 7200(n + 20)$$

$$30n^2 + 7800n = 7200n + 144,000$$

$$30n^2 + 600n - 144,000 = 0$$

$$n^2 + 20n - 4800 = 0$$

$$(n + 80)(n - 60) = 0$$

$n = 60$  acres (since  $n > 0$ ), so 60 acres were sold.

42. Let  $q$  = number of units of product sold last year and  $q + 2000$  = the number sold this year. Then the revenue last year was  $3q$  and this year it is  $3.5(q + 2000)$ . By the definition of margin of profit, it follows that

$$\frac{7140}{3.5(q + 2000)} = \frac{4500}{3q} + 0.02$$

$$\frac{2040}{q + 2000} = \frac{1500}{q} + 0.02$$

$$2040q = 1500(q + 2000) + 0.02q(q + 2000)$$

$$2040q = 1500q + 3,000,000 + 0.02q^2 + 40q$$

$$0 = 0.02q^2 - 500q + 3,000,000$$

$$q = \frac{500 \pm \sqrt{250,000 - 240,000}}{0.04}$$

$$= \frac{500 \pm \sqrt{10,000}}{0.04}$$

$$= \frac{500 \pm 100}{0.04}$$

$$= 10,000 \text{ or } 15,000$$

So that the margin of profit this year is not greater than 0.15, we choose  $q = 15,000$ . Thus 15,000 units were sold last year and 17,000 this year.

43. Let  $q$  = number of units of  $B$  and  $q + 25$  = number of units of  $A$  produced.

Each unit of  $B$  costs  $\frac{1000}{q}$ , and each unit of  $A$

costs  $\frac{1500}{q + 25}$ . Therefore,

$$\frac{1500}{q + 25} = \frac{1000}{q} + 2$$

$$1500q = 1000(q + 25) + 2(q)(q + 25)$$

$$0 = 2q^2 - 450q + 25,000$$

$$0 = q^2 - 225q + 12,500$$

$$0 = (q - 100)(q - 125)$$

$$q = 100 \text{ or } q = 125$$

If  $q = 100$ , then  $q + 25 = 125$ ; if  $q = 125$ ,  $q + 25 = 150$ . Thus the company produces either 125 units of  $A$  and 100 units of  $B$ , or 150 units of  $A$  and 125 units of  $B$ .

### Apply It 1.2

1.  $200 + 0.8S \geq 4500$

$$0.8S \geq 4300$$

$$S \geq 5375$$

He must sell at least 5375 products per month.

2. Since  $x_1 \geq 0$ ,  $x_2 \geq 0$ ,  $x_3 \geq 0$ , and  $x_4 \geq 0$ , we have the inequalities

$$150 - x_4 \geq 0$$

$$3x_4 - 210 \geq 0$$

$$x_4 + 60 \geq 0$$

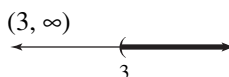
$$x_4 \geq 0$$

### Problems 1.2

1.  $5x > 15$

$$x > \frac{15}{5}$$

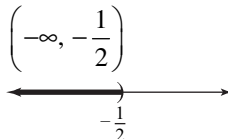
$$x > 3$$



2.  $4x < -2$

$$x < \frac{-2}{4}$$

$$x < -\frac{1}{2}$$

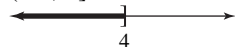


3.  $5x - 11 \leq 9$

$5x \leq 20$

$x \leq 4$

$(-\infty, 4]$



4.  $5x \leq 0$

$x \leq \frac{0}{5}$

$x \leq 0$

$(-\infty, 0]$

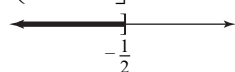


5.  $-4x \geq 2$

$x \leq \frac{2}{-4}$

$x \leq -\frac{1}{2}$

$\left(-\infty, -\frac{1}{2}\right]$

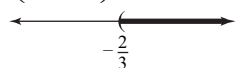


6.  $3z + 2 > 0$

$3z > -2$

$z > -\frac{2}{3}$

$\left(-\frac{2}{3}, \infty\right)$

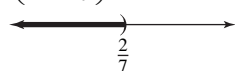


7.  $5 - 7s > 3$

$-7s > -2$

$s < \frac{2}{7}$

$\left(-\infty, \frac{2}{7}\right)$

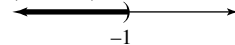


8.  $4s - 1 < -5$

$4s < -4$

$s < -1$

$(-\infty, -1)$



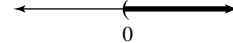
9.  $3 < 2y + 3$

$0 < 2y$

$0 < y$

$y > 0$

$(0, \infty)$



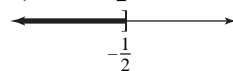
10.  $4 \leq 3 - 2y$

$1 \leq -2y$

$-\frac{1}{2} \geq y$

$y \leq -\frac{1}{2}$

$\left(-\infty, -\frac{1}{2}\right]$



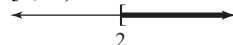
11.  $t + 6 \leq 2 + 3t$

$4 \leq 2t$

$2 \leq t$

$t \geq 2$

$[2, \infty)$



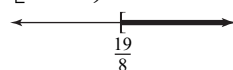
12.  $-3 \geq 8(2 - x)$

$-3 \geq 16 - 8x$

$8x \geq 19$

$x \geq \frac{19}{8}$

$\left[\frac{19}{8}, \infty\right)$



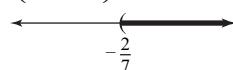
13.  $3(2 - 3x) > 4(1 - 4x)$

$6 - 9x > 4 - 16x$

$7x > -2$

$x > -\frac{2}{7}$

$\left(-\frac{2}{7}, \infty\right)$



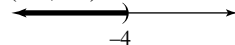
14.  $8(x+1)+1 < 3(2x)+1$

$8x+9 < 6x+1$

$2x < -8$

$x < -4$

$(-\infty, -4)$



15.  $2(4x-2) > 4(2x+1)$

$8x-4 > 8x+4$

$-4 > 4$ , which is false for all  $x$ .

Thus the solution set is  $\emptyset$ .

16.  $5-(x+2) \leq 2(2-x)$

$5-x-2 \leq 4-2x$

$x \leq 1$

$(-\infty, 1]$

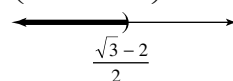


17.  $x+2 < \sqrt{3}-x$

$2x < \sqrt{3}-2$

$x < \frac{\sqrt{3}-2}{2}$

$\left(-\infty, \frac{\sqrt{3}-2}{2}\right)$



18.  $\sqrt{2}(x+2) > \sqrt{8}(3-x)$

$\sqrt{2}(x+2) > 2\sqrt{2}(3-x)$

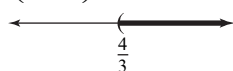
$x+2 > 2(3-x)$

$x+2 > 6-2x$

$3x > 4$

$x > \frac{4}{3}$

$\left(\frac{4}{3}, \infty\right)$

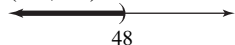


19.  $\frac{5}{6}x < 40$

$5x < 240$

$x < 48$

$(-\infty, 48)$

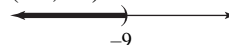


20.  $-\frac{2}{3}x > 6$

$-x > 9$

$x < -9$

$(-\infty, -9)$



21.  $\frac{5y+2}{4} \leq 2y-1$

$5y+2 \leq 8y-4$

$-3y \leq -6$

$y \geq 2$

$[2, \infty)$



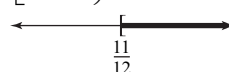
22.  $\frac{3y-2}{3} \geq \frac{1}{4}$

$12y-8 \geq 3$

$12y \geq 11$

$y \geq \frac{11}{12}$

$\left[\frac{11}{12}, \infty\right)$



23.  $-3x+1 \leq -3(x-2)+1$

$-3x+1 \leq -3x+7$

 $1 \leq 7$ , which is true for all  $x$ . The solution is

$-\infty < x < \infty$ .

$(-\infty, \infty)$



24.  $0x \leq 0$

 $0 \leq 0$ , which is true for all  $x$ . The solution is

$-\infty < x < \infty$ .

$(-\infty, \infty)$



25.  $\frac{1-t}{2} < \frac{3t-7}{3}$

$3(1-t) < 2(3t-7)$

$3-3t < 6t-14$

$-9t < -17$

$t > \frac{17}{9}$

$\left(\frac{17}{9}, \infty\right)$

