- **1.** If $f(x) = (x-2)^2 + 5$, find f(2), f(a), and f(1/a).
- 2. Find the domain of the function.

$$f(x) = 0.5x - \frac{2}{\sqrt{x+1}}$$

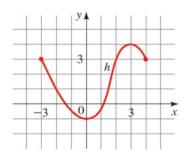
3. Find the range of the function.

$$f(x) = -x^2 - 2x + 3$$

- **4.** (a) Sketch the graph of the function $f(x) = x^2$.
 - (b) Use part (a) to graph the function $g(x) = (x-1)^2 + 1$.
- **5.** Describe how the graph of y = -f(2x) + 2 can be obtained from the graph of f.
- **6.** Sketch the graph of the function.

$$h(x) = x^3 - 4x^2$$

- 7. The graph of a function h is given.
 - (a) Find h(-3), h(-2), h(2), and h(4)
 - (b) Find the domain and range of h.
 - (c) Find the values of x for which h(x) = 3
 - (d) Find the values of x for which $h(x) \le 3$.



8. A function is given. Use a graphing calculator to draw the graph of f. Find the domain and range of f from the graph.

$$f(x) = x^2, \quad -3 \le x \le 5$$

9. A function is given. (a) Find all the local maximum and minimum values of the function and the value of x at which each occurs. (b) Find the intervals on which the function is increasing and on which the function is decreasing. State each answer correct to two decimal places.

$$G(x) = \frac{2}{x^2 + x + 1}$$

10. Evaluate f(-2), f(-1), f(0), f(1), and f(5) for the piecewise-defined function.

$$f(x) = \begin{cases} 3x^2 & \text{if } x < 0\\ 2x + 1 & \text{if } x \ge 0 \end{cases}$$

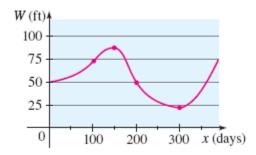
11. Sketch the graph of the function.

$$f(x) = \begin{cases} x^2 & \text{if } x < -3\\ x + 12 & \text{if } x \ge -3 \end{cases}$$

12. Draw the graph of the function in an appropriate viewing rectangle.

$$f(x) = 1.1x^3 - 8.6x^2 - 1.4x + 1.2$$

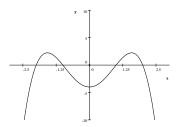
- 13. For the function $f(x) = 2x^2 x$ determine the average rate of change between the values x = -1 and x = 0.
- **14.** For the function $f(t) = 2t^2 t$ determine the average rate of change between the values t = 2 and t = 2 + h ($h \ne 0$).
- **15.** Use a graphing device to draw the graph of the function $f(x) = 144x^3 144x^2 + 36x$. State approximately the intervals on which the function is increasing and on which the function is decreasing.
- **16.** The graph shows the depth of water W in a reservoir over a one-year period as a function of the number of days x since the beginning of the year. What was the average rate of change of W between x = 0 and x = 100?



- 17. If an object is dropped from a high cliff or a tall building, then the distance it has fallen after t seconds is given by the function $f(t) = 16t^2$. Find its average speed (average rate of change) over the following intervals:
 - (i) Between 1 s and 6 s
 - (ii) Between t = c and t = c + h
- **18.** If $f(x) = 2x^2 + 1$ and g(x) = x 1, find f + g, fg, and their domains.
- **19.** Use f(x) = 3x 2 and $g(x) = 3 + 2x^2$ to evaluate the expression $(f \circ g)(2)$.

20. Given
$$f(x) = \frac{1}{x+2}$$
 and $g(x) = \frac{1}{x-2}$, find $f \circ g$, $g \circ f$.

21. Determine whether the function in the figure is even, odd, or neither.



- **22.** Determine whether or not the function $f(x) = x^2 3x + 2$ is one-to-one.
- 23. Use a graphing calculator or computer to determine whether or not the function $f(x) = 2x^3 x$ is one-to-one.
- **24.** Find the inverse of the function.

$$f(x) = \frac{1}{2}x + 1$$

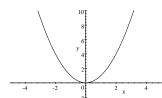
25. Find the inverse of the function.

$$f(x) = \sqrt{25 - x^2}$$
, $0 \le x \le 5$

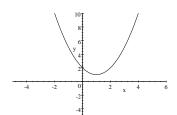
1.
$$f(2) = (2-2)^2 + 5 = 5$$

 $f(a) = (a-2)^2 + 5 = 9 - 4a + a^2$
 $f(\frac{1}{a}) = (\frac{1}{a} - 2)^2 + 5 = \frac{1 - 4a + 9a^2}{a^2}$

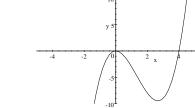
- 2. Domain: $(-1, \infty)$
- 3. Range: $(-\infty, 4]$
- **4.** (a)



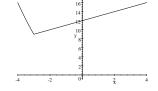
(b)

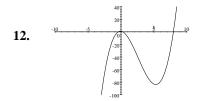


- 5. By shrinking horizontally by a factor of 1/2, then reflecting about the x-axis, then shifting 2 units up.
- 6



- 7. (a) h(-3) = 3; h(-2) = 1; h(2) = 3; h(4) = 3 (b) Domain [-3,4], Range [-1,4] (c) -3,2,4
 - (d) $-3 \le x \le 2$
- **8.** Domain: [-3,5], Range [0,25]
- 9. (a) local maximum ≈ 2.67 when $x \approx -0.50$; no local minimum (b) increasing on $(-\infty, -0.50]$; decreasing on $[-0.50, \infty)$
- **10.** f(-2) = 12, f(-1) = 3, f(0) = 1, f(1) = 3, f(5) = 11
- 11.

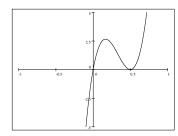




13. Average rate of change
$$= \frac{f(0) - f(-1)}{0 - (-1)} = -3$$

14. Average rate of change
$$=\frac{f(2+h)-f(2)}{2+h-2}=\frac{2(2+h)^2-8-h}{h}=7+2h$$

15.
$$f$$
 is increasing on $\left(-\infty, \frac{1}{6}\right)$ and $\left(\frac{1}{2}, \infty\right)$, and decreasing on $\left(\frac{1}{6}, \frac{1}{2}\right)$.



16.
$$\approx \frac{1}{4}$$
 ft/day

17. (i)
$$\frac{f(6) - f(1)}{6 - 1} = 112 \text{ ft/s}$$
, (ii) $\frac{f(c+h) - f(c)}{c + h - c} = \frac{16(c+h)^2 - 16c^2}{h} = 32c + 16h$

18.
$$f + g = 2x^2 + x$$
 domain : $(-\infty, \infty)$; $(fg)(x) = 2x^3 - 2x^2 + x - 1$, domain: $(-\infty, \infty)$.

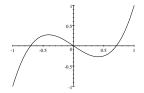
19.
$$(f \circ g)(2) = 31$$

20.
$$(f \circ g)(x) = f\left(\frac{1}{x-2}\right) = \frac{1}{\frac{1}{x-2} + 2} = \frac{x-2}{2x-3}$$

$$(g \circ f)(x) = g\left(\frac{1}{x+2}\right) = \frac{1}{\frac{1}{x+2}-2} = \frac{x+2}{-2x-3}$$

22.
$$f(x) = x^2 - 3x + 2 = (x - 2)(x - 1)$$
, so $f(2) = 0 = f(1)$, so f is not one-to-one.

23. Using a graphing calculator and the horizontal line test we see that $f(x) = 2x^3 - x$ is not one-to-one.



24.
$$g(x) = 2x - 2$$

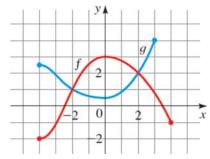
24.
$$g(x) = 2x - 2$$

25. $g(x) = \sqrt{25 - x^2}$, $0 \le x \le 5$

1. For the function given, find g(-1), g(3), and $g(a^2)$.

$$g(x) = \left(1/x\right) + x^2$$

- **2.** Graphs of the functions f and g are given.
 - (a) Which is larger, f(0) or g(0)?
 - **(b)** Which is larger, f(-1) or g(-1)?
 - (c) For which values of x is f(x) = g(x)?



3. Find the domain of the function.

$$f(x) = \frac{x+3}{x^2 - 4}$$

4. A function is given. Use a graphing calculator to draw the graph of f. Find the domain and range of f from the graph.

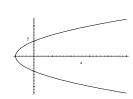
$$f(x) = -\sqrt{16 - x^2}$$

- 5. Sketch the graph of the function $f(x) = 2 + \sqrt{x}$.
- **6.** Determine if the equation $x^2 + y^2 25 = 0$ defines y as a function of x. Explain your answer.
- 7. Determine whether each curve represents a graph of a function.

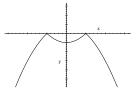




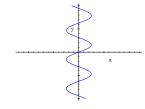
b.)



c.)



d.)



8. A function *f* is given, and the indicated transformations are applied to its graph (in the given order). Write the equation for the final transformed graph.

f(x) = |x|; shift to the left 1/2 unit, shrink vertically by a factor of 0.2, and shift downward 2 units.

9. Sketch the graph of the piecewise defined function.

$$f(x) = \begin{cases} x+2 & \text{if } x < 0 \\ 2 & \text{if } 0 \le x \le 1 \\ 3-x & \text{if } 1 < x \end{cases}$$

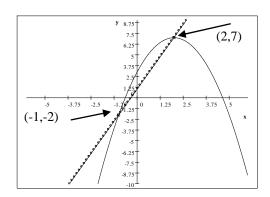
10. Sketch the graph of the function.

$$h(x) = \frac{1}{\left(x-2\right)^2}$$

11. Use a graphing calculator to estimate the range of the function.

$$f(x) = x^4 - x^3 + x^2 + 2x - 15$$

12. For the given graph of a function, determine the average rate of change between the indicated values.



- 13. For the function $g(t) = \frac{1}{3t-2}$ determine the average rate of change between the values t = 0 and t = a+1.
- 14. Use a graphing calculator to determine approximately the intervals on which the function is increasing, and on which f is decreasing.

$$f(x) = x^4 + 6x^3 + x^2 - 24x + 16$$

- **15.** Describe how the graph of y = -f(3x) + 4 can be obtained from the graph of f.
- **16.** Determine whether $f(x) = x^2 x^6$ is even, odd, or neither.

- 17. If an object is dropped from a high cliff or a tall building, then the distance it has fallen after t seconds is given by the function $f(t) = 16t^2$. Find its average speed (average rate of change) over the following intervals:
 - (i) Between 2 s and 7 s
 - (ii) Between t = c and t = c + h
- **18.** A function is given. (a) Find all the local maximum and minimum values of the function and the value of *x* at which each occurs. (b) Find the intervals on which the function is increasing and on which the function is decreasing. State each answer correct to two decimal places.

$$U(x) = 4\left(x^3 - x\right)$$

- 19. Use a graphing device to draw the graph of the function $f(x) = -3 3x^2$. State approximately the intervals on which the function is increasing and on which the function is decreasing.
- **20.** If f(x) = 3x 2 and $g(x) = 3 + 2x^2$, find fg and $(f \circ g)(x)$.
- **21.** Given $f(x) = 2 + x^2$ and $g(x) = \sqrt{x-1}$, find $(f \circ g)(2)$, $(f \circ f)(2)$.
- **22.** Determine whether or not the function $f(x) = -2x^2 + 18x 16$ is one-to-one.
- 23. Use a graphing calculator or computer to determine whether or not the function f(x) = -|x| |5-x| is one-to-one.
- **24.** Find the inverse of the function.

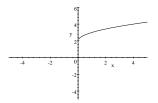
$$f(x) = 3x + 2$$

25. Find the inverse of the function.

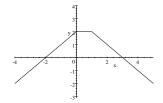
$$g(x) = x^2 - 9, x \ge 0$$

1.
$$g(-1) = \frac{1}{-1} + (-1)^2 = 0$$
, $g(3) = \frac{1}{3} + 3^2 = \frac{28}{3}$, $g(a^2) = \frac{1}{a^2} + (a^2)^2 = \frac{1}{a^2} + a^4 = \frac{1 + a^6}{a^2}$

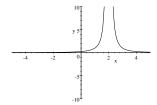
- **2.** (a) f(0) (b) f(-1) (c) -2,2
- 3. Domain: $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$
- **4.** Domain: [-4,4], Range [-4,0]
- 5.



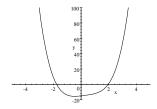
- **6.** $x^2 + y^2 25 = 0 \iff y^2 = 25 x^2 \iff y = \pm \sqrt{25 x^2}$. No, this equation gives two values of y for a given value of x.
- 7. (a) no (b) no (c) yes (d) no
- 8. $f(x) = 0.2 \left| x + \frac{1}{2} \right| 2$
- 9.



10.



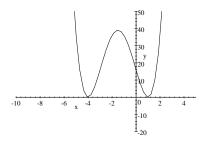
11. Range $[-15, \infty)$



12. The average rate of change for the function between the points (-1,-2) and (2,7) is $\frac{7-(-2)}{2-(-1)}=3$.

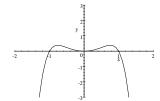
13.
$$\frac{3}{2(3a+1)}$$

14. The function is increasing on [-4, -1.5], $[1, \infty)$. Decreasing on $(-\infty, -4]$, [-1.5, 1).



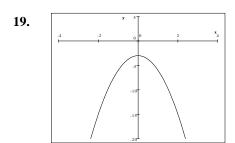
15. By shrinking horizontally by a factor of $\frac{1}{3}$, then reflecting about the x-axis, then shifting 4 units up.

16. Since f(x) = f(-x), f is even.



17. (i) $\frac{f(7) - f(2)}{7 - 2} = 144 \text{ ft/s}$, (ii) $\frac{f(c+h) - f(c)}{c+h-c} = \frac{16(c+h)^2 - 16c^2}{h} = 32c + 16h$

18. (a) local maximum ≈ 1.54 when $x \approx -0.58$; local minimum ≈ -1.54 when $x \approx 0.58$ (b) increasing on $(-\infty, -0.58] \cup [0.58, \infty)$; decreasing on [-0.58, 0.58]



f is increasing on $(-\infty,0]$ and decreasing on $[0,\infty)$.

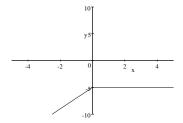
20.
$$fg = 6x^3 - 4x^2 + 9x - 6$$

 $(f \circ g)(x) = 7 + 6x^2$

21.
$$(f \circ g)(2) = 3$$
 $(f \circ f)(2) = 38$

22.
$$f(x) = -2x^2 + 18x - 16 = -2(x-8)(x-1)$$
, so $f(8) = 0 = f(1)$, so f is not one-to-one.

23.



Using a graphing calculator and the horizontal line test we see that f(x) = -|x| - |5-x| is not one-to-one.

24.
$$f^{-1}(x) = \frac{x-2}{3}$$

25.
$$g^{-1}(x) = \sqrt{x+9}$$

- 1. If $g(x) = \frac{4}{x} + x^2$, find g(-4).
 - (a) 4
 - (b) 6
 - (c) 1
 - (d) 15
 - (e) 21
- **2.** A function is given. Use a graphing calculator to draw the graph of f. Find the domain and range of f from the graph.

$$f(x) = \sqrt{9 - x^2}$$

- (a) Domain: [-3,3], Range: [-3,0]
- (b) Domain: [-9,9], Range: [-9,9]
- (c) Domain: [-3,3], Range: [0,3]
- (d) Domain: [-3,3], Range: all real numbers
- (e) Domain: all real numbers, Range: [0,3]
- **3.** Find the domain of the function.

$$f(x) = \frac{x}{x^2 - 25}$$

- (a) $(-\infty, 5)$
- (b) $(-\infty, -5) \cup (5, \infty)$
- (c) $(-5,\infty)$
- (d) $(-\infty,0)\cup(25,\infty)$
- (e) none of these
- **4.** Evaluate f(-1), f(0), f(1), for the piecewise-defined function.

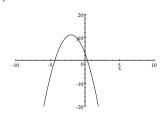
$$f(x) = \begin{cases} x^2 & \text{if } x < 0\\ 2x - 1 & \text{if } x \ge 0 \end{cases}$$

- (a) f(-1) = 1, f(0) = -1, f(1) = 1
- (b) f(-1) = -3, f(0) = 0, f(1) = 1
- (c) f(-1) = -1, f(0) = 0, f(1) = 1
- (d) f(-1) = 3, f(0) = 1, f(1) = -3
- (e) none of these
- **5.** Determine if the equation $x^2 + y^2 = 49$ defines y as a function of x.
 - (a) The equation represents a function because it's a circle.
 - (b) The equation represents a function because for each value of x there is always two values of y.
 - (c) Not a function because the equation gives two values of y for a given value of x.
 - (d) The equation represents a function because it passes the vertical line test.
 - (e) Not a function because the equation passes the vertical line test.

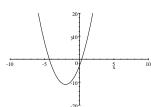
6. Sketch the graph of the function.

$$h(x) = 3 - 8x - 2x^2$$

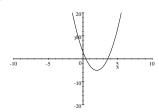
(a)



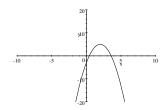
(b)



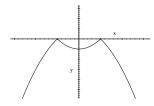
(c)



(d)



- (e) none
- 7. Determine whether the curve represents a graph of a function.



- (a) Function; the graph passes the horizontal line test.
- (b) Function; the graph passes the vertical line test.
- (c) Not a function; the graph passes the vertical line test
- (d) Not a function; the graph passes the horizontal line test
- (e) none
- 8. A function f is given, and the indicated transformations are applied to its graph (in the given order). Find the equation for the final transformed graph.

 $f(x) = \sqrt{x}$; shift 5 units to the left, stretch vertically by a factor of 2, and reflect in the x-axis.

(a)
$$f(x) = -2\sqrt{x} + 5$$

(b)
$$f(x) = -\frac{1}{2}\sqrt{x} - 5$$

(c)
$$f(x) = -5\sqrt{x-2}$$

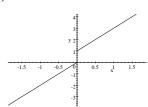
(d)
$$f(x) = -\sqrt{5x-2}$$

(e)
$$f(x) = -2\sqrt{x+5}$$

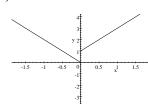
9. Sketch the graph of the function.

$$f(x) = \begin{cases} -2x & \text{if } x < 0\\ 1 - 2x & \text{if } x \ge 0 \end{cases}$$

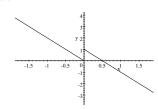
(a)



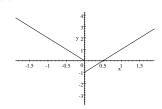
(b)



(c)



(d)



- (e) none
- 10. Determine which viewing rectangle produces the most appropriate graph of the function.

$$g(x) = 6x^3 - 15x^2 + 4x - 1$$

(a)
$$[-2,2]$$
 by $[-2,2]$

(b)
$$[-8,8]$$
 by $[-8,8]$

(c)
$$[-4,4]$$
 by $[-12,12]$

(d)
$$[-100,100]$$
 by $[-100,100]$

(e)
$$[-10,10]$$
 by $[-100,100]$

11. Use a graphing calculator to find, approximately the range of the function.

$$f(x) = 2x^4 - x^3 + x^2 + 2x - 7$$

(a)
$$[-2,7)$$

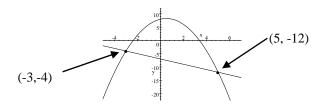
(b)
$$(-\infty, \infty)$$

(c)
$$[-14, \infty)$$

(d)
$$[-7,\infty)$$

(e)
$$[-\infty, 7)$$

12. For the given graph of a function, determine the average rate of change between the indicated values.

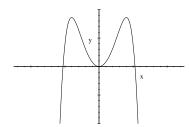


- (a) 0
- (b) 1
- (c) 2
- (d) -
- (e) -1
- 13. For the function $f(t) = \frac{1}{3t-2}$ determine the average rate of change between the values t = 0 and t = b+1.
 - (a) $\frac{3}{(3b-1)}$
 - (b) $\frac{2}{3(b+1)}$
 - (c) 3(3b+1)
 - (d) $\frac{-1}{(2b-3)}$
 - (e) $\frac{3}{2(3b+1)}$
- **14.** Use a graphing calculator to determine approximately the internals on which the function f is decreasing.

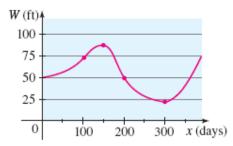
$$f(x) = x^4 + 6x^3 + x^2 - 24x + 16$$

- (a) $[-4, -1.5], [1, \infty)$
- (b) $(-\infty, -4]$, [-1.5, 1)
- (c) $(0,\infty)$
- (d) (0,-16)
- (e) $(-\infty, -16]$
- **15.** Describe how the graph of y = -f(3x) + 4 can be obtained from the graph of f.
 - (a) Shrink horizontally by a factor of 1/3, then reflecting about the x axis, then shifting 4 units up.
 - (b) Shrink horizontally by a factor of 4, then reflecting about the x axis, then shifting 3 units up.
 - (c) Shrink horizontally by a factor of 1/3, then reflecting about the y axis, then shifting 4 units right.
 - (d) Shrink horizontally by a factor of 1/3, then reflecting about the x axis, then shifting 3 units down.
 - (e) Shrink horizontally by a factor of 1/3, then reflecting about the y-axis, then shifting 4 units up.

16. Determine whether the function in the figure is even, odd, or neither.



- (a) even
- (b) odd
- (c) neither even or odd
- (d) both even and odd
- 17. The graph shows the depth of water W in a reservoir over a one-year period as a function of the number of days x since the beginning of the year. Estimate the average rate of change of W between x = 0 and x = 100?



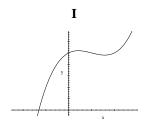
- (a) -2 ft/day
- (b) -4 ft/day

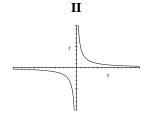
- (c) 4 ft/day (d) $\frac{1}{4} \text{ ft/day}$ (e) none of these
- **18.** If an object is dropped from a high cliff or a tall building, then the distance it has fallen after t seconds is given by the function $f(t) = 16t^2$. Find its average speed (average rate of change) over the interval between t = c and t = c + h.

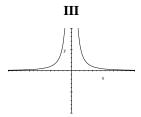
- (a) -16h (b) 32c+16h (c) 32c-h (d) 16c-h (e) none of these
- 19. Use a graphing device to draw the graph of the function $f(x) = -3 3x^2$. State approximately the interval(s) on which the function is increasing and on which the function is decreasing.
 - (a) f is increasing on $(-\infty,0]$ and decreasing on $[0,\infty)$
 - (b) f is increasing on $(-\infty, -3)$ and decreasing on $[3, \infty)$
 - (c) f is increasing on $(-\infty, \infty)$
 - (d) f is decreasing on $[0, \infty)$ only
 - (e) none of these
- **20.** If f(x) = 3x 2 and $g(x) = 3 + 2x^2$, find fg and $(g \circ f)(x)$.
 - (a) $fg = x^3 4x^2 + 9x 1$; $(g \circ f)(x) = 18x^2 24x + 11$
 - (b) $fg = 6x^3 4x^2 + 9x 6$; $(g \circ f)(x) = 18x^2 24x + 11$
- - (c) $fg = 2x^2 + 3x + 1$; $(g \circ f)(x) = 6x^2 + 7$
 - (d) $fg = 6x^2 + 7$;
- $(g \circ f)(x) = 6x^3 4x^2 + 9x 6$
- (e) none of these

- **21.** Given $f(x) = 2 + x^2$ and $g(x) = \sqrt{x-4}$, find $(f \circ g)(4)$
 - (a) $(f \circ g)(4) = 2$
 - (b) $(f \circ g)(4) = 4$
 - (c) $(f \circ g)(4) = -2$
 - (d) $(f \circ g)(4) = 0$
 - (e) $(f \circ g)(4) = 1$
- **22.** Find $g \circ g \circ g$, where $g(x) = x^2$.

- (a) x^6 (b) $6x^6$ (c) $8x^8$ (d) x^8 (e) $x^8 + 8$
- **23.** Determine which functions are one-to-one.







- (a) I only
- (b) I, II
- (c) I, II, III
- (d) II only
- (e) III only

24. Find the inverse of the function.

$$f(x) = 3x + 2$$

- (a) $f^{-1}(x) = x 2$ (b) $f^{-1}(x) = 2x$ (c) $f^{-1}(x) = \frac{x + 2}{3}$ (d) $f^{-1}(x) = \frac{x 2}{3}$ (e) none of these

25. Find the inverse of the function.

$$g(x) = x^2 - 9, x \ge 0$$

- (a) $g^{-1}(x) = -\sqrt{x+9}$
- (b) $g^{-1}(x) = \sqrt{x+9}$
- (c) $g^{-1}(x) = 9 + \sqrt{x}$
- (d) $g^{-1}(x) = 9 \sqrt{x}$
- (e) none of these

ANSWER KEY

Stewart/Redlin/Watson - Precalculus 7e Chapter 2 Form C

- **1.** d
- **2.** c
- **3.** e
- **4.** a
- **5.** c
- **6.** a
- **7.** b
- **8.** e
- **9.** c
- **10.** c
- 11. d 12. e
- **13.** e
- **14.** b
- **15.** a
- **16.** a
- **17.** d
- **18.** b
- **19.** a
- **20.** b
- **21.** a
- **22.** d
- **23.** d
- **24.** d
- **25.** b

- 1. If $g(x) = 3 \sqrt{2x 6}$, find g(5).
 - (a) 4
- (b) 3
- (c) 1
- (d) 5 (e) $3-\sqrt{10}$
- **2.** Find the range of the function.

$$f(x) = \sqrt{x+4}$$

- (a) [0,-2)
- (b) $(2, \infty)$
- (c) [-2,2)
- (d) $[0,\infty)$
- (e) all real numbers
- **3.** Find the domain of the function.

$$f(x) = \frac{1}{x} + \frac{1}{x+1}$$

- (a) $(-\infty, 0)$
- (b) $(-\infty, -1) \cup (-1, 0) \cup (0, \infty)$
- (c) $(-\infty, -1) \cup (-1, 0)$
- (d) $(-\infty,0)\cup(0,\infty)$
- (e) none of these
- **4.** Evaluate f(-1), f(0), f(1), for the piecewise-defined function.

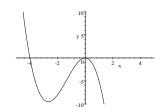
$$f(x) = \begin{cases} x^2 & \text{if } x < 0\\ x - 1 & \text{if } x \ge 0 \end{cases}$$

- (a) f(-1) = 1, f(0) = -1, f(1) = 0
- (b) f(-1) = -2, f(0) = 0, f(1) = 1
- (c) f(-1) = -1, f(0) = 0, f(1) = 1
- (d) f(-1) = 2, f(0) = 1, f(1) = -3
- (e) none of these
- 5. Determine if the equation $x^2 + (y-1)^2 = 36$ defines y as a function of x.
 - (a) The equation represents a function because it's a circle.
 - (b) The equation represents a function because for each value of x there is always two values of y.
 - (c) Not a function because the equation gives two values of y for a given value of x.
 - (d) The equation represents a function because it passes the vertical line test.
 - (e) Not a function because the equation passes the vertical line test.

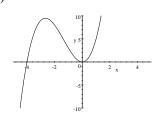
6. Sketch the graph of the function.

$$h(x) = x^3 - 4x^2$$

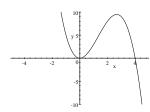
(a)



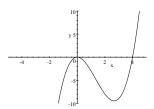
(b)



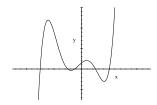
(c)



(d)



- (e) none
- 7. Determine whether the curve represents a graph of a function.



- (a) Function; the graph passes the horizontal line test.
- (b) Function; the graph passes the vertical line test.
- (c) Not a function; the graph passes the vertical line test
- (d) Not a function; the graph passes the horizontal line test
- (e) none
- **8.** A function f is given, and the indicated transformations are applied to its graph (in the given order). Find the equation for the final transformed graph.

 $f(x) = \sqrt{x}$; shift 5 units to the left, stretch vertically by a factor of 2, and reflect in the x-axis.

(a)
$$f(x) = -2\sqrt{x} + 5$$

(b)
$$f(x) = -\frac{1}{2}\sqrt{x} - 5$$

(c)
$$f(x) = -5\sqrt{x-2}$$

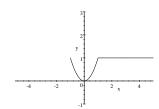
(d)
$$f(x) = -\sqrt{5x-2}$$

(e)
$$f(x) = -2\sqrt{x+5}$$

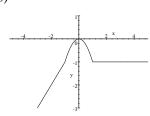
9. Sketch the graph of the function.

$$f(x) = \begin{cases} -x & \text{if } x < -1 \\ x^2 & \text{if } -1 \le x \le 1 \\ 1 & \text{if } x > 1 \end{cases}$$

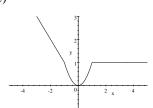
(a)



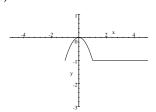
(b)



(c)



(d)



(e) none

10. Determine which viewing rectangle produces the most appropriate graph of the function.

$$g(x) = 6x^3 - 15x^2 + 4x - 1$$

(a)
$$[-2,2]$$
 by $[-2,2]$

(b)
$$[-8,8]$$
 by $[-8,8]$

(c)
$$[-4,4]$$
 by $[-12,12]$

(d)
$$[-100,100]$$
 by $[-100,100]$

(e)
$$[-10,10]$$
 by $[-100,100]$

11. Use a graphing calculator to find, approximately the range of the function.

$$f(x) = x^4 - x^3 + 3x^2 + 2x - 10$$

(a)
$$[0,\infty)$$

(b)
$$(-\infty,\infty)$$

(a)
$$[0,\infty)$$
 (b) $(-\infty,\infty)$ (c) $[-10,10)$ (d) $[-\infty,5)$ (e) $[-10,\infty)$

(d)
$$[-\infty, 5]$$

12. Find the average rate of change of the function f between the points given.

$$f(x) = \frac{1}{x-3}$$
; $x = 2$, $x = 7$

(b)
$$1/5$$

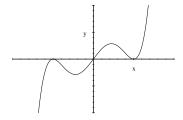
(b)
$$1/5$$
 (c) $-1/5$

(e)
$$-1$$

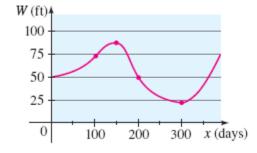
- 13. For the function $f(t) = \frac{1}{t}$ determine the average rate of change between the values t = a and t = a + h.
 - (a) $\frac{-1}{a(a+h)}$ (b) $\frac{-2}{h}$ (c) (3h+1) (d) $\frac{-1}{(2h-1)}$ (e) $\frac{1}{a(a+h)}$
- **14.** Use a graphing calculator to determine approximately the internals on which the function f is decreasing.

$$f(x) = x^4 + 6x^3 + x^2 - 24x + 16$$

- (a) [-4, -1.5], $[1, \infty)$ (b) $(-\infty, -4]$, [-1.5, 1) (c) $(0, \infty)$ (d) (0, -16) (e) $(-\infty, -16]$
- **15.** Describe how the graph of y = -f(x) 4 can be obtained from the graph of f.
 - (a) Shrink horizontally by a factor of 4, then reflecting about the x axis, then shifting 4 units up.
 - (b) Reflect about the x axis, shift 4 units up.
 - (c) Reflect about the y axis, shift 4 units down.
 - (d) Reflect about the x axis, shift 1 unit up.
 - (e) Reflect about the x axis, shift 4 units down.
- **16.** Determine whether the function in the figure is even, odd, or neither.



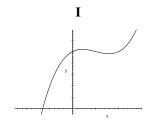
- (a) even
- (b) odd
- (c) neither even or odd
- (d) both even and odd
- (e) not enough information to determine
- 17. The graph shows the depth of water W in a reservoir over a one-year period as a function of the number of days x since the beginning of the year. Estimate the average rate of change of W between x = 0 and x = 100?

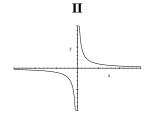


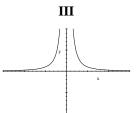
- (a) -2 ft/day
- (b) -4 ft/day
- (c) 4ft/day
- (d) 1/4 ft/day
- (e) none of these

- **18.** If an object is dropped from a high cliff or a tall building, then the distance it has fallen after t seconds is given by the function $f(t) = 16t^2$. Find its average speed (average rate of change) over the interval between t = c and t = c + h.
 - (a) -16h
 - (b) 32c+16
 - (c) 32c h
 - (d) 16c h
 - (e) none of these
- 19. Use a graphing device to draw the graph of the function $f(x) = -3 3x^2$. State approximately the interval(s) on which the function is increasing and on which the function is decreasing.
 - (a) f is increasing on $(-\infty,0]$ and decreasing on $[0,\infty)$
 - (b) f is increasing on $(-\infty, -3)$ and decreasing on $[3, \infty)$
 - (c) f is increasing on $(-\infty, \infty)$
 - (d) f is decreasing on $[0, \infty)$ only
 - (e) none of these
- **20.** If f(x) = 3x 2 and $g(x) = 3 + 2x^2$, find fg and $(g \circ f)(x)$.
 - (a) $fg = x^3 4x^2 + 9x 1$; $(g \circ f)(x) = 18x^2 24x + 11$
 - (b) $fg = 6x^3 4x^2 + 9x 6$; $(g \circ f)(x) = 18x^2 24x + 11$
 - (c) $fg = 2x^2 + 3x + 1$; $(g \circ f)(x) = 6x^2 + 7$
 - (d) $fg = 6x^2 + 7$; $(g \circ f)(x) = 6x^3 4x^2 + 9x 6$
 - (e) none of these
- **21.** Given $f(x) = 1 x^2$ and $g(x) = \sqrt{x-1}$, find $(f \circ g)(5)$
 - (a) $(f \circ g)(5) = -2$
 - (b) $(f \circ g)(5) = 5$
 - (c) $(f \circ g)(5) = -3$
 - (d) $(f \circ g)(5) = 1$
 - (e) $(f \circ g)(5) = -1$
- **22.** Find $f \circ g \circ h$, where $f(x) = \sqrt{1-x}$, $g(x) = 1-x^2$, $h(x) = 1+\sqrt{x}$.
 - (a) $\sqrt{1+\sqrt{x}}$
 - (b) $1 + \sqrt{x}$
 - (c) $\sqrt{1+x^2}$
 - (d) $\sqrt{1-x}$
 - (e) $1+x^2$

23. Determine which functions are one-to-one.







- (a) I only
- (b) I, II
- (c) I, II, III
- (d) II only
- (e) III only
- **24.** Find the inverse of the function.

$$f\left(x\right) = \frac{x - 7}{4}$$

(a)
$$f^{-1}(x) = x + 7$$

(b)
$$f^{-1}(x) = \frac{4x}{7}$$

(c)
$$f^{-1}(x) = \frac{x+7}{4}$$

(d)
$$f^{-1}(x) = 4x + 7$$

- (e) none of these
- **25.** Find the inverse of the function.

$$g(x) = x^2 - 16, x \ge 0$$

(a)
$$g^{-1}(x) = -\sqrt{x+16}$$

(b)
$$g^{-1}(x) = \sqrt{x+16}$$

(c)
$$g^{-1}(x) = 4 + \sqrt{x}$$

(d)
$$g^{-1}(x) = 4 - \sqrt{x}$$

(e) none of these

ANSWER KEY

Stewart/Redlin/Watson - Precalculus 7e Chapter 2 Form D

- **1.** c
- **2.** d
- **3.** b
- **4.** a
- **5.** c
- **6.** d
- **7.** b
- **8.** e
- **9.** c
- **10.** c
- **11.** e
- **12.** a
- **13.** a
- **14.** b
- **15.** e
- **16.** b
- **17.** d
- 18. e
- **19.** a
- **20.** b
- **21.** c
- **22.** b
- **23.** d
- **24.** d
- **25.** b

d) 17

1. If
$$g(x) = \frac{4}{x} + x^2$$
, find $g(4)$.

- a) 4
- b) 6
- c) 1
- e) 21
- **2.** Find the domain of the function.

$$f(x) = 2x^2 - 3$$
, $0 \le x < 5$

- a) [0,6]
- b) $(-\infty,\infty)$
- c) $(3/2, \infty)$
- d) $(-\infty,5) \cup (5,\infty)$
- e) [0,5)
- 3. Find the domain of the function.

$$f(x) = \frac{x-1}{x^2 - 4}$$

- a) (-4,4)
- b) $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$
- c) $(2,\infty)$
- d) $(-\infty, -2) \cup (2, \infty)$
- e) none of these
- **4.** Evaluate f(-1), f(0), f(1), for the piecewise-defined function.

$$f(x) = \begin{cases} 3x^2 & \text{if } x < 0\\ 2x + 1 & \text{if } x \ge 0 \end{cases}$$

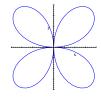
- a) f(-1) = 3, f(0) = 1, f(1) = 3
- b) f(-1) = 0, f(0) = 3, f(1) = -3
- c) f(-1) = -1, f(0) = 0, f(1) = 1
- d) f(-1) = 3, f(0) = 1, f(1) = -3
- e) none of these
- **5.** Sketch the graph of the piecewise defined function.

$$f(x) = \begin{cases} x+2 & \text{if } x < 0 \\ 2 & \text{if } 0 \le x \le 1 \\ 3-x & \text{if } 1 < x \end{cases}$$

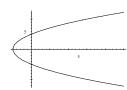
6. Determine if the equation $x^2 + y^2 - 25 = 0$ defines y as a function of x. Explain your answer.

7. Determine whether each curve represents a graph of a function.

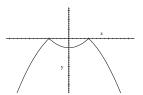
a.)



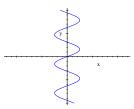
b.)



c.)



d.)



8. A function f is given, and the indicated transformations are applied to its graph (in the given order). Write the equation for the final transformed graph.

f(x) = |x|; shift to the left $\frac{1}{2}$ unit, shrink vertically by a factor of 0.2, and shift downward 2 units.

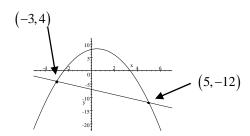
- **9.** Sketch the graph of the function $f(x) = 2 + \sqrt{x}$.
- **10.** Sketch the graph of the function.

$$h(x) = \frac{1}{\left(x - 2\right)^2}$$

11. Use a graphing calculator to find, approximately the range of the function.

$$f(x) = x^4 - x^3 + x^2 + 2x - 15$$

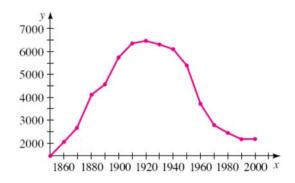
12. For the given graph of a function, determine the average rate of change between the indicated values.



- 13. For the function $g(t) = \frac{1}{3t-2}$ determine the average rate of change between the values t = 0 and t = a+1.
- **14.** Use a graphing calculator to determine approximately the intervals on which the function is increasing, and on which f is decreasing.

$$f(x) = x^4 + 6x^3 + x^2 - 24x + 16$$

- **15.** Describe how the graph of y = -f(3x) + 4 can be obtained from the graph of f.
- **16.** Determine whether $f(x) = x^2 x^6$ is even, odd, or neither.
 - a) even
- b) odd
- c) neither even nor odd d) both even and odd
- 17. The graph gives the number of farms in the United States from 1850 to 2000. Estimate the average rate of change in the number of farms between the following years.
 - 1860 and 1890 (i)
 - (ii) 1920 and 1980



18. A man is running around a circular track that is 200 m in circumference. An observer uses a stopwatch to record the runner's time at the end of each lap, obtaining the data in the following table.

What was the man's average speed (rate) between 108 s and 203 s? Round the answer to two decimal places.

Time (s)	Distance (m)
32	200
68	400
108	600
152	800
203	1000
263	1200
335	1400
412	1600

- 19. Use a graphing device to draw the graph of the function $f(x) = -3 3x^2$. State approximately the interval(s) on which the function is increasing and on which the function is decreasing.
 - a) f is increasing on $(-\infty, 0]$ and decreasing on $[0, \infty)$
 - b) f is increasing on $(-\infty, -3)$ and decreasing on $[3, \infty)$
 - c) f is increasing on $(-\infty, \infty)$
 - d) f is and decreasing on $[0, \infty)$ only
 - none of these

20. If
$$f(x) = 3x - 2$$
 and $g(x) = 3 + 2x^2$, find fg and $(f \circ g)(x)$.

21. Given
$$f(x) = 2 + x^2$$
 and $g(x) = \sqrt{x-1}$, find $(f \circ g)(2)$, $(f \circ f)(2)$.

22. Determine whether the function
$$f(x) = -2x^2 + 18x - 16$$
 is one-to-one.

23. Use a graphing calculator or computer to determine whether the function
$$f(x) = -|x| - |5-x|$$
 is one-to-one.

$$f(x) = \frac{x-2}{3}$$

a)
$$f^{-1}(x) = 2x - 3$$

b)
$$f^{-1}(x) = 2x$$

c)
$$f^{-1}(x) = \frac{x+2}{3}$$

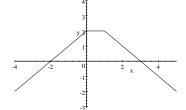
d)
$$f^{-1}(x) = 3x + 2$$

25. Find the inverse of the function.

$$g(x) = x^2 - 9, x \ge 0$$

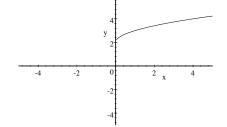
- **1.** d
- **2.** e
- **3.** b
- **4.** a



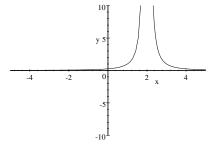


- **6.** $x^2 + y^2 25 = 0 \iff y^2 = 25 x^2 \iff y = \pm \sqrt{25 x^2}$. No. This equation gives two values of y for a given value of x.
- 7. (a) no (b) no (c) yes (d) no
- 8. $f(x) = 0.2 \left| x + \frac{1}{2} \right| 2$





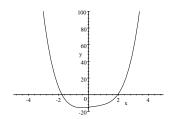




ANSWER KEY

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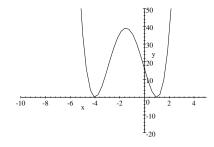
11. Range $[-15, \infty)$



12. The average rate of change for the function between the points (-3,-4) and (5,-12) is

$$\frac{-12 - \left(-4\right)}{5 - \left(-3\right)} = \frac{-8}{8} = -1.$$

- 13. Average rate of change $=\frac{g(a+1)-g(0)}{a+1-0} = \frac{\frac{1}{3a+1}+\frac{1}{2}}{a+1} = \frac{\frac{3}{2}\frac{a+1}{3a+1}}{a+1} = \frac{3}{2(3a+1)}$
- **14.** The function is increasing on [-4,-1.5], $[1,\infty)$. Decreasing on $(-\infty,-4]$, [-1.5,1)



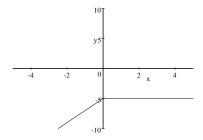
- 15. By shrinking horizontally by a factor of $\frac{1}{3}$, then reflecting about the x axis, then shifting 4 units up. Determine whether the function in the figure is even, odd, or neither.
- **16.** a
- 17. (i) ≈ 83 farms/yr (ii) ≈ -67 farms/yr
- **18.** 4.21 m/s
- **19.** a
- **20.** $fg = 6x^3 4x^2 + 9x 6$ $(f \circ g)(x) = 7 + 6x^2$
- **21.** $(f \circ g)(2) = 3$ $(f \circ f)(2) = 38$

ANSWER KEY

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22.
$$f(x) = -2x^2 + 18x - 16 = -2(x - 8)(x - 1)$$
, so $f(8) = 0 = f(1)$, so f is not one-to-one.

23. Using a graphing calculator and the horizontal line test we see that f(x) = -|x| - |5-x| is not one-to-one.



25.
$$g^{-1}(x) = \sqrt{x+9}$$

- **1.** If $f(x) = x^3 + 2x 1$, find f(a).
 - (a) $a^3 + 2a 1$
- (b) $2a^3 + a 16$ (c) $2a^3 + 3a$ (d) $4a^3$ (e) $2a^3 a + 1$

2. Find the range of the function.

$$f(x) = 2x^2 - 3$$

- $(a) \quad [0,\infty) \qquad (b) \ \left(-\infty,\infty\right) \qquad (c) \ \left(-3/2,\infty\right) \qquad \quad (d) \ \left(-\infty,-3\right) \cup (3,\infty) \qquad \quad (e) \ \left[-3,\infty\right)$

3. Find the domain of the function.

$$f(x) = 3x - \frac{2}{\sqrt{x+1}}$$

- (a) (-1,1) (b) $(-\infty,-1) \cup (1,\infty)$ (c) $(-1,\infty)$ (d) $(-\infty,-1] \cup [1,\infty)$ (e) none of these
- **4.** Evaluate f(-1), f(0), f(1), for the piecewise-defined function.

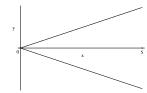
$$f(x) = \begin{cases} 1 - 2x & \text{if } x \le 0 \\ 2x - 1 & \text{if } x > 0 \end{cases}$$

- (a) f(-1) = 3, f(0) = -1, f(1) = 2
- (b) f(-1) = 0, f(0) = 3, f(1) = -3
- (c) f(-1) = -1, f(0) = 0, f(1) = 1
- (d) f(-1) = -1, f(0) = 1, f(1) = 1
- (e) none of these
- **5.** Sketch the graph of the function.

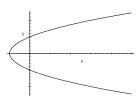
$$G(x) = x^3 - 3x^2$$

- Determine if the equation $x^2 + (y-1)^2 4 = 0$ defines y as a function of x. Explain your answer.
- 7. Determine whether each curve represents a graph of a function.

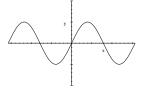


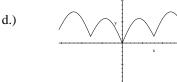


b.)



c.)





- **8.** Suppose the graph of f is given. Describe how the graph of the function y = f(x-3) 3 can be obtained from the graph of f.
- 9. Sketch the graph of the function $f(x) = 2 + \sqrt{x}$.
- 10. A function f is given, and the indicated transformations are applied to its graph (in the given order). Find the equation for the final transformed graph.

 $f(x) = \sqrt{x}$; shift 5 units to the left, stretch vertically by a factor of 2, and reflect in the x-axis.

- (a) $f(x) = -2\sqrt{x} + 5$
- (b) $f(x) = -\frac{1}{2}\sqrt{x} 5$
- (c) $f(x) = -5\sqrt{x-2}$
- (d) $f(x) = -\sqrt{5x-2}$
- (e) $f(x) = -2\sqrt{x+5}$
- 11. Use a graphing calculator to find, approximately the range of the function.

$$f(x) = 2x^4 - x^3 + x^2 + 2x - 7$$

- (a) [-2,7)
- (b) $(-\infty,\infty)$
- (c) $[-14, \infty)$
- (d) $[-7,\infty)$
- (e) $[-\infty, 7)$
- 12. Find the average rate of change of the function between the given points

$$f(x) = 2x^2 + x$$
; $x = 0, x = 2$

- 13. For the function $g(t) = \frac{1}{3t-2}$ determine the average rate of change between the values t = 0 and t = c+1.
- **14.** Use a graphing calculator to determine approximately the intervals on which the function is increasing, and on which *f* is decreasing.

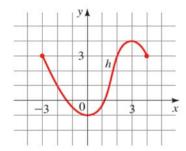
$$f(x) = x^4 + 6x^3 + x^2 - 24x + 16$$

- **15.** Describe how the graph of y = -f(2x) 4 can be obtained from the graph of f.
 - (a) Shrink horizontally by a factor of 1/2, then reflecting about the x axis, then shifting 4 units down.
 - (b) Shrink horizontally by a factor of 4, then reflecting about the x axis, then shifting 2 units up.
 - (c) Shrink horizontally by a factor of 1/2, then reflecting about the y axis, then shifting 4 units right.
 - (d) Shrink horizontally by a factor of 1/2, then reflecting about the x axis, then shifting 2 units down.
 - (e) Shrink horizontally by a factor of 1/2, then reflecting about the y axis, then shifting 4 units up.

- **16.** Determine whether $f(x) = x^2 x^4$ is even, odd, or neither.
 - (a) even
 - (b) odd
 - (c) neither even nor odd
 - (d) both even and odd
 - (e) not enough information to determine
- 17. A function is given. (a) Find all the local maximum and minimum values of the function and the value of x at which each occurs. (b) Find the intervals on which the function is increasing and on which the function is decreasing. State all answers correct to two decimal places.

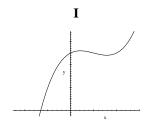
$$G(x) = \frac{2}{x^2 + x + 1}$$

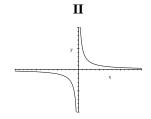
- **18.** The graph of a function h is given.
 - (a) Find h(-3), h(-2), h(0), and h(3)
 - **(b)** Find the domain and range of *h*.
 - (c) Find the values of x for which h(x) = 3
 - (d) Find the values of x for which $h(x) \le 3$.

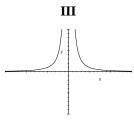


- 19. Use a graphing device to draw the graph of the function $f(x) = -3 3x^2$. State approximately the interval(s) on which the function is increasing and on which the function is decreasing.
 - (a) f is increasing on $(-\infty,0]$ and decreasing on $[0,\infty)$
 - (b) f is increasing on $(-\infty, -3)$ and decreasing on $[3, \infty)$
 - (c) f is increasing on $(-\infty, \infty)$
 - (d) f is decreasing on $[0, \infty)$ only
 - (e) none of these
- **20.** If f(x) = 3x 2 and $g(x) = 3 + 2x^2$, find fg and $(g \circ f)(x)$.
 - (a) $fg = x^3 4x^2 + 9x 1$; $(g \circ f)(x) = 18x^2 24x + 11$
 - (b) $fg = 6x^3 4x^2 + 9x 6$; $(g \circ f)(x) = 18x^2 24x + 11$
 - (c) $fg = 2x^2 + 3x + 1$; $(g \circ f)(x) = 6x^2 + 7$
 - (d) $fg = 6x^2 + 7$; $(g \circ f)(x) = 6x^3 4x^2 + 9x 6$
 - (e) none of these

- **21.** Given $f(x) = 2 + x^2$ and $g(x) = \sqrt{x-1}$, find $(f \circ g)(2)$, $(f \circ f)(2)$.
- 22. Determine which functions are one-to-one.







- (a) I only
- (b) I, II
- (c) I, II, III
- (d) II only
- (e) III only
- 23. Use a graphing calculator or computer to determine whether the function f(x) = -|x| |5-x| is one-to-one.
- **24.** Find the inverse of the function.

$$f(x) = 3x + 2$$

(a)
$$f^{-1}(x) = x - 2$$

(b)
$$f^{-1}(x) = 2x$$

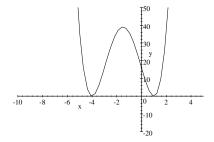
(c)
$$f^{-1}(x) = \frac{x+2}{3}$$

(d)
$$f^{-1}(x) = \frac{x-2}{3}$$

- (e) none of these
- **25.** Find the inverse of the function.

$$g(x) = x^2 - 16, x \ge 0$$

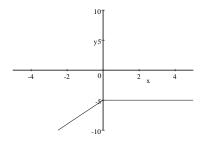
- **1.** a
- **2.** e
- **3.** c
- **4.** e
- **6.** $x^2 + (y-1)^2 4 = 0 \iff y = 1 \pm \sqrt{4 x^2}$. No. This equation gives two values of y for a given value of x.
- 7. (a) no, (b) no, (c) yes, (d) yes
- **8.** Shift the graph of f 3 units to the right then 3 units down
- 9. -4 -2 0 2 x 4
- **10.** e
- **11.** d
- **12.** 5
- 13. Average rate of change: $\frac{3}{2(3c+1)}$
- **14.** The function is increasing on [-4,-1.5], $[1,\infty)$. Decreasing on $(-\infty,-4]$, [-1.5,1)



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- **15.** a
- **16.** a
- 17. (a) local maximum ≈ 2.67 when $x \approx -0.50$; no local minimum (b) increasing on $(-\infty, -0.50]$; decreasing on $[-0.50, \infty)$
- **18.** (a) h(-3) = 3; h(-2) = 1; h(0) = -1; h(3) = 4; (b) Domain [-3, 4], Range [-1, 4]; (c) -3, 2, 4; (d) $-3 \le x \le 2$
- **19.** a
- **20.** b
- **21.** $(f \circ g)(2) = 3$ $(f \circ f)(2) = 38$
- **22.** d
- 23. Using a graphing calculator and the horizontal line test we see that f(x) = -|x| |5-x| is not one-to-one.



- **24.** d
- **25.** $g^{-1}(x) = \sqrt{x+16}$