

# MINI LECTURE NOTES

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## PRECALCULUS: CONCEPTS THROUGH FUNCTIONS, A UNIT CIRCLE APPROACH TO TRIGONOMETRY FOURTH EDITION

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