Precalculus with Limits A Graphing Approach

SEVENTH EDITION

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1. Use function notation to write g in terms of $f(x) = x^3$.

$$g(x) = -\frac{1}{5}(x+4)^3$$

A)
$$g(x) = -\frac{1}{5} [f(x)]^3 + 4$$

B)
$$g(x) = -\frac{1}{5}[f(x) + 4]$$

C)
$$g(x) = -[f(x)]^3 + \frac{64}{5}$$

D)
$$g(x) = -\frac{1}{5} [f(x)]^3 + 64$$

E)
$$g(x) = -\frac{1}{5} [f(x+4)]$$

2. Hooke's Law states that the force F required to compress or stretch a spring (within its elastic limits) is proportional to the distance d that the spring is compressed or stretched from its original length. That is, F = kd, where k is the measure of the stiffness of the spring and is called the *spring constant*. The table below shows the elongation d in centimeters of a spring when a force of F kilograms is applied.

Force, F	Elongation, d
20	3.5
40	6.3
60	10.0
80	13.3
100	16.5

Find the equation of the line that seems to best fit the data.

- A) F = 12.098d
- B) F = 3.024d
- C) F = 6.049d
- D) F = 4.537d
- E) F = 7.561d

Larson's Precalculus with Limits: A Graphing Approach, 7e

3. Find (fg)(x).

Find
$$(fg)(x)$$
.
 $f(x) = \sqrt{-5x}$ $g(x) = \sqrt{-8x+6}$
A) $(fg)(x) = 2x\sqrt{10} - \sqrt{30x}$

A)
$$(fg)(x) = 2x\sqrt{10} - \sqrt{30x}$$

B)
$$(fg)(x) = 2x\sqrt{10-30x}$$

C)
$$(fg)(x) = \sqrt{-13x + 6}$$

D)
$$(fg)(x) = \sqrt{40x^2 + 6}$$

E)
$$(fg)(x) = \sqrt{40x^2 - 30x}$$

4. If f is an even function, determine if g is even, odd, or neither.

$$g(x) = -f(x-2)$$

- A) even
- B) odd
- C) cannot be determined
- D) neither

5. Given the following function, h(x), find two functions f and g such that

$$(f \circ g)(x) = h(x).$$

$$h(x) = \sqrt[3]{x^2 - 11}$$

A)
$$f(x) = \sqrt[3]{x^2}$$
, $g(x) = -11$

B)
$$f(x) = \sqrt[3]{x^2}$$
, $g(x) = x - 11$

C)
$$f(x) = \sqrt[3]{x}$$
, $g(x) = x - 11$

D)
$$f(x) = \sqrt[3]{x-11}$$
, $g(x) = x^2$

E)
$$f(x) = \sqrt[3]{x-11}$$
, $g(x) = x+11$

6. Evaluate the following function at the specified value of the independent variable and simplify.

$$f(w) = \frac{-7w^2 + 20}{w^2}; \qquad f(0)$$

- A) 20
- B) 0
- C) -7
- D) 13
- undefined E)

7. Determine algebraically whether the following function is one-to-one.

$$|x-5|, x \le 5$$

A)
$$|a-5| = |b-5|$$

 $5-a = 5-b$
 $-a = -b$; one-to-one

$$a = b$$

B)
$$|a-5| = |b-5|$$

 $|a|-5 = |b|-5$; one-to-one
 $|a| = |b|$
 $a = b$

C)
$$|a-5| = |b-5|$$

 $a+5 = 5-b$; not one-to-one
 $a = -b$

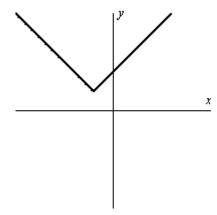
D)
$$|a-5| = |b-5|$$

 $|-5|-a = |-5|+b$; not one-to-one
 $-a = b$

E)
$$\begin{vmatrix} a-5 \end{vmatrix} = \begin{vmatrix} b-5 \end{vmatrix}$$

 $\begin{vmatrix} -5 \end{vmatrix} - a = \begin{vmatrix} -5 \end{vmatrix} - b$; one-to-one
 $-a = -b$
 $a = b$

8. Determine an equation that may represented by the graph shown below.



- A) f(x) = |x+1|-1
- B) f(x) = |x-1|+1
- C) f(x) = |x+1|+1
- D) f(x) = |x-1|-1
- E) f(x) = -|x-1|+1
- 9. Determine the domain and range of the inverse function f^{-1} of the following function f.

$$f(x) = -|x+6| + 2$$
, where $x > -6$

- A) Domain: $[-6, \infty)$; Range: $[2, \infty)$
- B) Domain: $(-\infty, 2]$; Range: $[-6, \infty)$
- C) Domain: [-6,2]; Range: $[-6,\infty)$
- D) Domain: $(-\infty, -6]$; Range: $[-2, \infty)$
- E) Domain: $(-\infty, \infty)$; Range: $(-\infty, \infty)$
- 10. Find the domain of the function.

$$f(y) = \sqrt{9 - y^2}$$

- A) $-3 \le y \le 3$
- B) $y \le -3$ or $y \ge 3$
- C) $y \ge 0$
- D) $y \le 3$
- E) all real numbers

11. Find the slope-intercept form of the line passing through the points.

$$(-1, -6), (0, -2)$$

A)
$$y = 4x + 23$$

B)
$$y = 4x - 2$$

C)
$$y = \frac{1}{4}x - \frac{23}{4}$$

D)
$$y = -\frac{1}{4}x + \frac{1}{2}$$

E)
$$y = -4x - 10$$

12. Write the slope-intercept form of the equation of the line through the given point perpendicular to the given line.

line:
$$-5x - 15y = -6$$

A)
$$y = \frac{1}{5}x + \frac{39}{5}$$

B)
$$y = -\frac{1}{3}x + \frac{17}{3}$$

C)
$$y = 3x + 19$$

C)
$$y = 3x + 19$$

D) $y = -5x + 27$

E)
$$y = 3x - \frac{5}{3}$$

13. Compare the graph of the following function with the graph of f(x) = |x|.

$$y = \left| \frac{4}{9} x \right|$$

A) vertical shift of
$$\frac{4}{9}$$
 units up

B) horizontal stretch of
$$\frac{9}{4}$$
 units

C) vertical shrink of
$$\frac{4}{9}$$
 units

D) horizontal shrink of
$$\frac{4}{9}$$
 units vertical shift of $\frac{9}{4}$ units

E) horizontal shrink of $\frac{4}{9}$ units

- 14. Which equation does not represent y as a function of x?
 - A) x = 2y + 5
 - B) x = 6

 - C) y = -5x 7D) $y = |6 + 9x^2|$ E) $y = \sqrt{-8 + 4x}$
- 15. Evaluate the function at the specified value of the independent variable and simplify.

$$q(p) = \frac{-2p}{5p - 2}$$

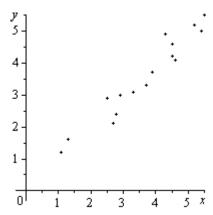
- q(x-9)
- A) $\frac{-2x+18}{5x-47}$
- B) $\frac{-2x-18}{5x-47}$
- C) $\frac{-2p+18}{5p-47}$
- D) $\frac{18}{43}$
- E) $-\frac{18}{47}$
- 16. Determine the domain of $g(x) = \frac{1}{x^2 49}$.
 - A) [-7,7]
 - B) $(-7,0] \cup [0,7)$
 - C) $\left(-\infty, -7\right) \cup \left(-7, 7\right) \cup \left(7, \infty\right)$
 - D) $\left(-\infty, -7\right] \cup \left[7, \infty\right)$
 - E) $\left(-\infty,\infty\right)$

17. Find the difference quotient and simplify your answer.

$$f(w) = -9w^2 + 2w,$$

$$\frac{f(4+h)-f(4)}{h}, h \neq 0$$

- A) 10 + h
- B) $-70 9w + \frac{16}{w}$
- C) $2-9w+\frac{16}{w}$
- D) 2 9h
- E) -70 9h
- 18. The scatter plots of different data are shown below. Determine whether there is a positive correlation, negative correlation, or no discernible correlation between the variables.



- A) positive correlation
- B) negative correlation
- C) no discernible correlation

19. Evaluate the following function for $f(x) = -2x^2 + 1$ and g(x) = x + 4 algebraically.

$$\left(\frac{f}{g}\right)(q-4)$$

$$A) \quad \frac{-2q^2 + 5}{q + 8}$$

B)
$$\frac{-2q^2 + 8q - 31}{q}$$

$$C) \quad \frac{-2q^2 + 5}{q}$$

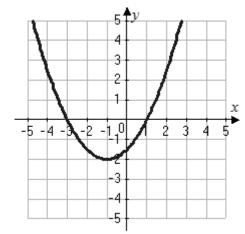
C)
$$\frac{-2q^2 + 5}{q}$$
D) $\frac{-2q^2 + 16q - 31}{q}$
E) $\frac{-2q^2 - 3}{q}$

E)
$$\frac{-2q^2 - 3}{q}$$

20. Use the graph of

$$f(x) = x^2$$

to write an equation for the function whose graph is shown.



- A) $f(x) = (x+1)^2 2$
- B) $f(x) = (x-1)^2 2$
- C) $f(x) = (x+1)^2 + 2$
- D) $f(x) = \frac{1}{2}(x-1)^2 2$
- E) $f(x) = \frac{1}{2}(x+1)^2 2$

Answer Key

- 1. E
- 2. C
- 3. E
- 4. C
- 5. D
- 6. E
- 7. A
- 8. C
- 9. B
- 10. A 11. B
- 12. C
- 13. B
- 14. B
- 15. A
- 16. C 17. E
- 18. A
- 19. D
- 20. E

Name: _____ Date: _____

- 1. Evaluate the indicated function for $f(x) = x^2 5$ and g(x) = x + 9.
 - (fg)(-1)
 - A) -32
 - B) -48 C) -46
 - D) 40
 - E) -50
- 2. Find the value(s) of x for which f(x) = g(x).

$$f(x) = x^2 - 7x + 3$$
 $g(x) = -3x + 8$

$$g(x) = -3x + 8$$

- A) 3, 10, $\frac{8}{3}$
- B) $3, -7, \frac{8}{3}$
- C) 5, -1
- D) -5, 1
- E) $4, \frac{8}{2}$
- 3. Find (f g)(x).

$$f(x) = -\frac{8x}{4x+7}$$

$$g(x) = -\frac{4}{x}$$

$$g(x) = -\frac{4}{x}$$

A)
$$(f-g)(x) = \frac{-8x+4}{3x+7}$$

B)
$$(f-g)(x) = \frac{-8x+23}{4x+7}$$

C)
$$(f-g)(x) = \frac{-8x+9}{4x+7}$$

D)
$$(f-g)(x) = \frac{-8x^2 + 16x - 28}{4x^2 + 7x}$$

E)
$$(f-g)(x) = \frac{-8x^2 + 16x + 28}{4x^2 + 7x}$$

4. If f is an even function, determine if g is even, odd, or neither.

$$g(x) = f(-x) + 1$$

- A) even
- B) odd
- C) cannot be determined
- D) neither
- 5. Evaluate the function at the specified value of the independent variable and simplify.

$$f(p) = \frac{-3p}{4p - 3}$$

$$f(s+8)$$

A)
$$\frac{-3s - 24}{4s + 29}$$

B)
$$\frac{-3s + 24}{4s + 29}$$

C)
$$\frac{-3p-24}{4p+29}$$

D)
$$\frac{24}{35}$$

E)
$$-\frac{24}{29}$$

6. Determine the domain of $g(x) = \frac{1}{x^2 - 81}$.

A)
$$[-9,9]$$

B)
$$(-9,0] \cup [0,9)$$

C)
$$(-\infty, -9) \cup (-9, 9) \cup (9, \infty)$$

D)
$$\left(-\infty, -9\right] \cup \left[9, \infty\right)$$

E)
$$\left(-\infty,\infty\right)$$

7. Determine whether lines L_1 and L_2 passing through the pairs of points are parallel, perpendicular, or neither.

$$L_1$$
: (7, -4), (-9, -1)

$$L_2$$
: (4, -6), (-3, 9)

- A) parallel
- B) perpendicular
- C) neither

8. Algebraically determine whether the function below is even, odd, or neither.

$$f(q) = 2q^{3/2}$$

- A) even
- B) odd
- C) cannot be determined
- D) neither
- 9. Find $f \circ g$.

$$f(x) = x + 2$$
 $g(x) = \frac{5}{x^2 - 4}$

A)
$$(f \circ g)(x) = \frac{5}{x^2}$$

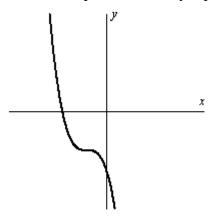
$$B) \quad (f \circ g)(x) = \frac{5}{x^2 + 4x}$$

C)
$$(f \circ g)(x) = \frac{2x^2 + 3}{x^2 - 4}$$

D)
$$(f \circ g)(x) = \frac{7}{x^2 - 4}$$

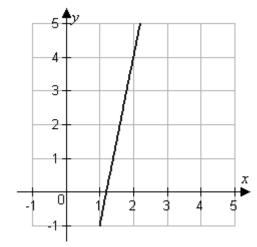
E)
$$(f \circ g)(x) = \frac{2x^2 - 3}{x^2 - 4}$$

10. Determine an equation that may represented by the graph shown below.



- A) $f(x) = (x-1)^3 + 2$
- B) $f(x) = -(x-1)^3 + 2$ C) $f(x) = -(x-1)^3 2$ D) $f(x) = -(x+1)^3 2$

- E) $f(x) = -(x+1)^3 + 2$
- 11. Estimate the slope of the line.



- A) -5
- B)
- C)
- D)

12. Compare the graph of the following function with the graph of f(x) = |x|.

$$y = \left| \frac{1}{9} x \right|$$

- A) vertical shift of $\frac{1}{9}$ unit up
- B) horizontal stretch of $\frac{9}{1}$ unit
- C) vertical shrink of $\frac{1}{9}$ unit
- D) horizontal shrink of $\frac{1}{9}$ unit vertical shift of $\frac{9}{1}$ unit
- E) horizontal shrink of $\frac{1}{9}$ unit
- 13. Use a graphing utility to graph the function and visually determine the intervals over which the function is increasing, decreasing, or constant.

$$f(x) = 2x^4 - 4x^2$$

- A) decreasing on (0,0)
 - increasing on $(0,\infty)$
- B) increasing on $(-\infty, -1)$
 - decreasing on (-1,0)
 - increasing on (0,1)
 - decreasing on (1,∞)
- C) decreasing on (-∞,-1)
 - increasing on (-1,1)
 - decreasing on $(1, \infty)$
- D) increasing on (-∞,0)
 - decreasing on $(0,\infty)$
- E) decreasing on $(-\infty, -1)$
 - increasing on (-1,0)
 - decreasing on (0,1)
 - increasing on (1,∞)

14. Hooke's Law states that the force F required to compress or stretch a spring (within its elastic limits) is proportional to the distance d that the spring is compressed or stretched from its original length. That is, F = kd, where k is the measure of the stiffness of the spring and is called the *spring constant*. The table below shows the elongation d in centimeters of a spring when a force of Fkilograms is applied.

Force, F	Elongation, d
20	2.8
40	5.0
60	8.0
80	10.6
100	13.2

Find the equation of the line that seems to best fit the data. Use the model to estimate the elongation of the spring when a force of 50 kilograms is applied. Round your answer to one decimal place.

- A) 13.2 centimeters
- B) 9.9 centimeters
- C) 3.3 centimeters
- D) 6.6 centimeters
- E) 5.0 centimeters
- 15. Find $f \circ g$.

Find
$$f \circ g$$
.
 $f(x) = 3x - 2$ $g(x) = x - 5$
A) $(f \circ g)(x) = 3x - 17$

A)
$$(f \circ g)(x) = 3x - 17$$

B)
$$(f \circ g)(x) = 3x - 7$$

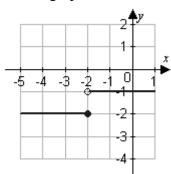
C)
$$(f \circ g)(x) = 3x^2 - 17x + 10$$

D)
$$(f \circ g)(x) = 2x + 3$$

E)
$$(f \circ g)(x) = 2x - 7$$

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16. Use the graph of the function to find the domain and range of f.



A) domain: $(-\infty, -2) \cup (-2, \infty)$

range: $(-\infty, -2) \cup (-1, \infty)$

B) domain: $(-\infty, -2) \cup (-2, \infty)$

range: {-2,-1}

C) domain: all real numbers

range: $\{-2, -1\}$

D) domain: $(-\infty, -2) \cup (-2, \infty)$

 $range: \begin{pmatrix} -1,1 \end{pmatrix}$

E) domain: $\{-2, -1\}$

range: all real numbers

17. Find the inverse function of *f*.

 $f(x) = x^5 + 5$

- A) $f^{-1}(x) = -\sqrt[5]{x} + 5$
- B) $f^{-1}(x) = \sqrt[5]{x} + 5$
- C) $f^{-1}(x) = -\sqrt[5]{x+5}$
- D) $f^{-1}(x) = \sqrt[5]{x-5}$
- E) $f^{-1}(x) = \sqrt[5]{x} 5$

18. Evaluate the following function at the specified value of the independent variable and simplify.

$$f(u) = \frac{4u^2 + 12}{u^2};$$
 $f(0)$

- A) 12
- B) 0
- C) 4
- D) 16
- E) undefined
- 19. Find $g \circ f$.

$$f(x) = x + 2$$

A) $(g \circ f)(x) = x^2 + 2$
 $g(x) = x^2$

- B) $(g \circ f)(x) = x^2 4$
- C) $(g \circ f)(x) = x^2 + 4$ D) $(g \circ f)(x) = x^2 + 2x + 4$
- E) $(g \circ f)(x) = x^2 + 4x + 4$
- 20. Find all real values of x such that f(x) = 0.

$$f(x) = \frac{-3x - 2}{5}$$

- A) $-\frac{2}{15}$
- B) $\pm \frac{2}{15}$
- C) $\pm \frac{2}{3}$ D) $-\frac{2}{3}$ E) $\frac{2}{3}$

Answer Key

- 1. A
- 2. C
- 3. E
- 4. A
- 5. A
- 6. C
- 7. C
- 8. D
- 9. E
- 10. D
- 11. C
- 12. B
- 13. E
- 14. D
- 15. A
- 16. C
- 17. D
- 18. E
- 19. E
- 20. D

Name: _____ Date: _____

1. Find the difference quotient and simplify your answer.

$$f(s) = -2s^2 - 2s,$$

$$f(s) = -2s^2 - 2s,$$
 $\frac{f(4+h) - f(4)}{h}, h \neq 0$

A) 6 + h

B)
$$-18 - 2s - \frac{16}{s}$$

C)
$$-2 - 2s - \frac{16}{s}$$

D)
$$-2 - 2h$$

E)
$$-18 - 2h$$

2. Determine whether the function has an inverse function. If it does, find the inverse function.

$$f(x) = x^2 + 5$$

A) No inverse function exists.

B)
$$f^{-1}(x) = \sqrt{x} + 5, x \ge 0$$

C)
$$f^{-1}(x) = \sqrt{x} - 5$$

D)
$$f^{-1}(x) = \sqrt{x+5}, x \ge -6$$

E)
$$f^{-1}(x) = \sqrt{x-5}$$

3. Which equation does not represent y as a function of x?

A)
$$x = -9y + 2$$

B)
$$x = -1$$

C)
$$y = 7x - 9$$

C)
$$y = 7x - 9$$

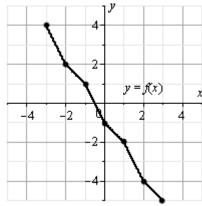
D) $y = |6 - x^2|$

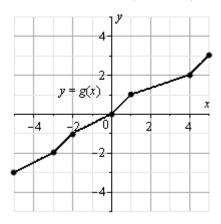
E)
$$y = \sqrt{-9 + 6x}$$

4. Determine the domain and range of the inverse function f^{-1} of the following function f.

$$f(x) = -|x+7|-1$$
, where $x > -7$

- A) Domain: $[-7,\infty)$; Range: $[-1,\infty)$
- B) Domain: $(-\infty, -1]$; Range: $[-7, \infty)$
- C) Domain: $\begin{bmatrix} -7, -1 \end{bmatrix}$; Range: $\begin{bmatrix} -7, \infty \end{bmatrix}$
- D) Domain: $(-\infty, -7]$; Range: $[1, \infty)$
- E) Domain: $(-\infty, \infty)$; Range: $(-\infty, \infty)$
- 5. Use the graphs of y = f(x) and y = g(x) to evaluate $(g^{-1} \circ f^{-1})(-4)$.





- A) 4
- B) 1.3
- C) 0
- D) –2
- E) -2.5

6. Compare the graph of the following function with the graph of $f(x) = x^3$.

$$y = \left[5(x+10)\right]^3$$

- A) vertical shift of 10 units up
- B) vertical shift of 10 units up horizontal shrink of $\frac{1}{5}$ units
- C) horizontal shift of 10 units to the left horizontal shrink of $\frac{1}{125}$ units
- D) horizontal shift of 10 units to the left horizontal stretch of $\frac{1}{5}$ units
- horizontal shift of 10 units to the left vertical shift of 5 units up
- 7. Find $f \circ g$.

$$f(x) = \left| x^2 - 6 \right| \qquad g(x) = -9 - x$$

$$g(x) = -9 - x$$

A)
$$(f \circ g)(x) = |x^2 + 18x + 75|$$

B)
$$(f \circ g)(x) = |x^2 + 75|$$

C)
$$(f \circ g)(x) = \left| -3 - x^2 \right|$$

C)
$$(f \circ g)(x) = \begin{vmatrix} -3 - x^2 \end{vmatrix}$$

D) $(f \circ g)(x) = \begin{vmatrix} -15 - x^2 \end{vmatrix}$

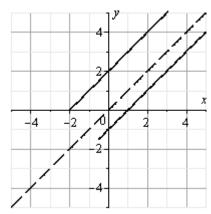
E)
$$(f \circ g)(x) = -9 - |x^2 - 6|$$

8. The average lengths *L* of cellular phone calls in minutes from 1999 to 2004 are shown in the table below.

6	<u>a</u>		
	Year	Average length, L (in minutes)	
	1999	2.38	
	2000	2.56	
	2001	2.74	
	2002	2.73	
	2003	2.87	
	2004	3.05	

Use the *regression* feature of a graphing utility to find a linear model for the data. Let t represent the year, with t = 9 corresponding to 1999. Use the model to predict the average lengths of cellular phone calls for the year 2015. Round your answer to two decimal places.

- A) 4.37 minutes
- B) 8.74 minutes
- C) 5.37 minutes
- D) 3.37 minutes
- E) 2.19 minutes
- 9. Decide whether the two functions shown in the graph below appear to be inverse functions of each other.



- A) yes
- B) no
- C) not enough information

10. Use a graphing utility to graph the function and visually determine the intervals over which the function is increasing, decreasing, or constant.

$$f(x) = -x^3 + 3x + 1$$

- A) increasing on (-∞,-1)
 - decreasing on (-1,1)
 - increasing on (1, ∞)
- B) decreasing on $(-\infty, 0)$
 - increasing on (0,∞)
- C) decreasing on $(-\infty, \infty)$
- D) increasing on $(-\infty, \infty)$
- E) decreasing on $(-\infty, -1)$
 - increasing on (-1,1)
 - decreasing on $(1, \infty)$
- 11. Find the value(s) of x for which f(x) = g(x).

$$f(x) = x^2 - 13x + 5$$
 $g(x) = -9x + 2$

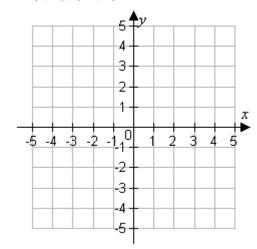
$$g(x) = -9x + 2$$

- A) 5, 18, $\frac{2}{9}$
- B) 5, -13, $\frac{2}{9}$
- C) 3, 1
- D) -3, -1
- E) $8, \frac{2}{9}$

12. Use function notation to write g in terms of $f(x) = x^3$.

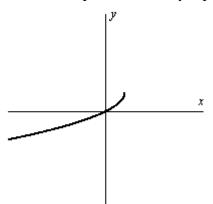
$$g(x) = -\frac{1}{4}(x+9)^3$$

- A) $g(x) = -\frac{1}{4} [f(x)]^3 + 9$
- B) $g(x) = -\frac{1}{4}[f(x) + 9]$
- C) $g(x) = -[f(x)]^3 + \frac{729}{4}$
- D) $g(x) = -\frac{1}{4} [f(x)]^3 + 729$
- E) $g(x) = -\frac{1}{4} [f(x+9)]$
- 13. Plot the points and find the slope of the line passing through the pair of points. (3, 4), (-2, 4)



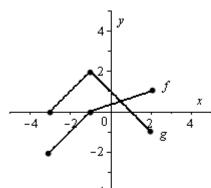
- A) slope: 0
- B) slope: 1
- C) slope: -5
- D) slope: $-\frac{1}{5}$
- E) slope: undefined

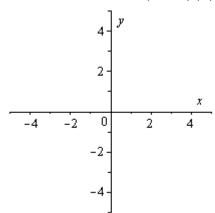
14. Determine an equation that may represented by the graph shown below.



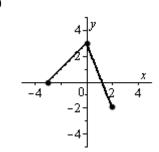
- A) $f(x) = 1 \sqrt{1-x}$
- B) $f(x) = -1 \sqrt{1 x}$ C) $f(x) = -1 + \sqrt{1 x}$ D) $f(x) = -1 \sqrt{1 + x}$
- E) $f(x) = -1 + \sqrt{1+x}$

15. Use the graphs of f and g, shown below, to graph h(x) = (f + g)(x).

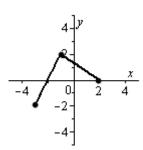




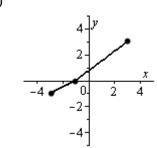
A)



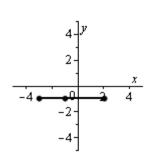
B)



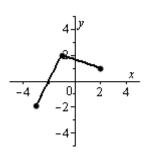
C)



D)



E)



16. Evaluate the function at the specified value of the independent variable and simplify.

$$f(y) = 2y + 7$$

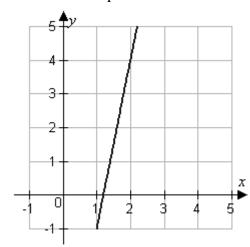
$$f(-1.4)$$

A)
$$-2.8y + 14$$

D)
$$-1.4y + 7$$

E)
$$-1.4y - 7$$

17. Estimate the slope of the line.



- B)
- C)
- D)
- 18. Use the functions $f(x) = \frac{1}{125}x 5$ and $g(x) = x^3$ to find $(f \circ g)^{-1}$.
 - A) $(f \circ g)^{-1} = \frac{x^3 + 5}{5}$
 - B) $(f \circ g)^{-1} = \frac{x^3 625}{125}$ C) $(f \circ g)^{-1} = \frac{\sqrt[3]{x+5}}{5}$

 - $D) \quad \left(f \circ g\right)^{-1} = 5x + 5$
 - E) $(f \circ g)^{-1} = 5\sqrt[3]{x+5}$

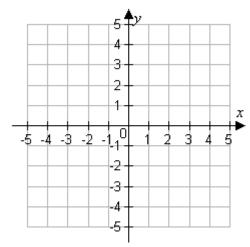
19. Find all real values of x such that f(x) = 0.

$$f(x) = \frac{7x - 5}{7}$$

- B) $\pm \frac{5}{49}$
- C) $\pm \frac{5}{7}$ D) $\frac{5}{7}$

- 20. Graph the function and determine the interval(s) for which $f(x) \ge 0$.

$$f(x) = -x^2 + 4x$$



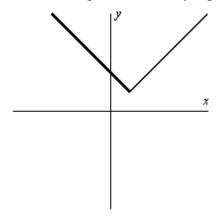
- A) $\left(-\infty,0\right] \cup \left[4,\infty\right)$
- C) (0,4)
- D) $(-\infty,0) \cup (4,\infty)$
- E) {4}

Answer Key

- 1. E
- 2. A
- 3. B
- 4. B
- 5. A
- 6. C
- 7. A
- 8. A
- 9. B
- 10. E
- 11. C
- 12. E
- 13. A
- 14. A
- 15. B
- 16. C
- 17. C
- 18. E
- 19. D
- 20. B

Name: _____ Date: _____

1. Determine an equation that may represented by the graph shown below.



A)
$$f(x) = |x-1|-1$$

B)
$$f(x) = -|x-1|+1$$

C)
$$f(x) = |x-1| + 1$$

D)
$$f(x) = |x+1| + 1$$

E)
$$f(x) = |x+1|-1$$

2. Find the inverse function of *f*.

$$f(x) = x^5 - 1$$

A)
$$f^{-1}(x) = -\sqrt[5]{x} - 1$$

B)
$$f^{-1}(x) = \sqrt[5]{x} - 1$$

C)
$$f^{-1}(x) = -\sqrt[5]{x-1}$$

D)
$$f^{-1}(x) = \sqrt[5]{x+1}$$

E)
$$f^{-1}(x) = \sqrt[5]{x} + 1$$

3. Find the domain of the function.

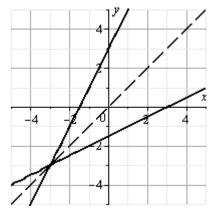
$$g(w) = \frac{4w}{w+9}$$

- A) all real numbers $w \neq -9$
- B) all real numbers $w \neq -9$, $w \neq 0$
- C) all real numbers

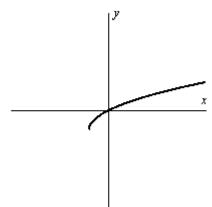
D)
$$w = -9, w = 0$$

E)
$$w = -9$$

4. Decide whether the two functions shown in the graph below appear to be inverse functions of each other.



- A) no
- B) yes
- C) not enough information
- 5. Determine an equation that may represented by the graph shown below.



- A) $f(x) = -1 + \sqrt{1+x}$
- $B) \quad f(x) = 1 \sqrt{1 x}$
- C) $f(x) = -1 \sqrt{1-x}$
- D) $f(x) = -1 + \sqrt{1-x}$
- E) $f(x) = -1 \sqrt{1+x}$

- 6. Which equation does not represent y as a function of x?
 - A) x = 6y 9
 - B) x = -5

 - C) y = x + 5D) $y = |-1 x^2|$ E) $y = \sqrt{-5 + 4x}$
- 7. Determine algebraically whether the following function is one-to-one.

$$f(x) = \frac{5x^2}{3x^2 + 6}$$
, where $x > 0$

A)
$$\frac{5a^2}{3a^2+6} = \frac{5b^2}{3b^2+6}$$

$$\frac{5a^2}{3a^2} + \frac{5a^2}{6} = \frac{5b^2}{3b^2} + \frac{5b^2}{6}$$

$$\frac{5}{3} + \frac{5a^2}{6} = \frac{5}{3} + \frac{5b^2}{6}$$

$$\frac{30+5a^2}{18} = \frac{30+5b^2}{18}$$
; not one-to-one

$$30 + 5a^2 = 30 + 5b^2$$

$$5a^2 = 5b^2$$
$$a^2 = b^2$$

$$a^2 = b^2$$

$$\pm a = \pm b$$

B)
$$\frac{5a^2}{3a^2+6} = \frac{5b^2}{3b^2+6}$$

$$\frac{5}{3+6} = \frac{5}{3+6}$$
; one-to-one

$$\frac{5}{6} = \frac{3}{6}$$

$$a = k$$

C)
$$\frac{5a^2}{3a^2+6} = \frac{5b^2}{3b^2+6}$$

$$\frac{5a^2}{3a^2} = \frac{5b^2}{3b^2}$$
; one-to-one

$$\frac{5}{3} = \frac{5}{3}$$

$$a = b$$

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D)
$$\frac{5a^2}{3a^2 + 6} = \frac{5b^2}{3b^2 + 6}$$

 $\frac{5a^2}{9a^2} = \frac{5b^2}{9b^2}$
 $\frac{5a}{9} = \frac{5b}{9}$; one-to-one
 $5a = 5b$
 $a = b$

E)
$$\frac{5a^2}{3a^2 + 6} = \frac{5b^2}{3b^2 + 6}$$

$$\frac{5a^2}{3a^2} + \frac{5a^2}{6} = \frac{5b^2}{3b^2} + \frac{5b^2}{6}$$

$$\frac{5}{3} + \frac{5a^2}{6} = \frac{5}{3} + \frac{5b^2}{6}$$

$$\frac{30 + 5a^2}{18} = \frac{30 + 5b^2}{18}$$
; one-to-one
$$30 + 5a^2 = 30 + 5b^2$$

$$5a^2 = 5b^2$$

$$a^2 = b^2$$

$$a = b$$

8. Find $f \circ g$.

$$f(x) = x + 3$$
 $g(x) = \frac{4}{x^2 - 9}$

A)
$$(f \circ g)(x) = \frac{4}{x^2}$$

B)
$$(f \circ g)(x) = \frac{4}{x^2 + 6x}$$

C)
$$(f \circ g)(x) = \frac{3x^2 + 1}{x^2 - 9}$$

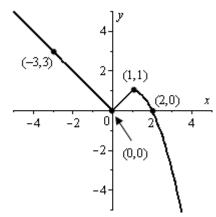
D)
$$(f \circ g)(x) = \frac{7}{x^2 - 9}$$

E)
$$(f \circ g)(x) = \frac{3x^2 - 23}{x^2 - 9}$$

9. Use function notation to write g in terms of $f(x) = \sqrt{x}$.

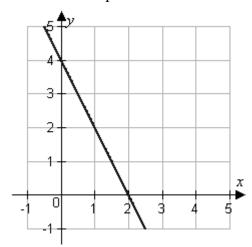
$$g(x) = -\frac{1}{3}\sqrt{x-8} + 7$$

- A) g(x) = -f(x-8) + 6
- B) $g(x) = -\frac{1}{3}f(x) 1$
- C) $g(x) = -\frac{1}{3}f(x-8) + 7$
- D) g(x) = f(x) + 7
- E) $g(x) = f(x-8) \frac{7}{3}$
- 10. Determine a piecewise-defined function for the graph shown below.



- A) $f(x) = \begin{cases} |x|, & x \le 1 \\ -(x-1)^2 + 1, & x > 1 \end{cases}$
- B) $f(x) = \begin{cases} |x|, & x \le 0 \\ -(x-1)^2 + 1, & x \le 0 \end{cases}$
- C) $f(x) = \begin{cases} |x|, & x \ge 1 \\ -x^2, & x \le 1 \end{cases}$
- D) $f(x) = \begin{cases} |x|, & x \ge 0 \\ -x^2, & x \le 1 \end{cases}$
- E) $f(x) = \begin{cases} |x|, & x \le 1 \\ -(x-1)^2, & x > 1 \end{cases}$

11. Estimate the slope of the line.



- A) $-\frac{1}{2}$
- B) 2
- C) -2
- D) $\frac{1}{2}$
- E) -3
- 12. Determine whether the function is even, odd, or neither.

$$f(x) = 4x^3 - 2x$$

- A) neither
- B) even
- C) odd
- 13. Find the slope and y-intercept of the equation of the line.

$$y = -2x + 3$$

- A) slope: $-\frac{1}{2}$; y-intercept: 3
- B) slope: $\frac{1}{3}$; y-intercept: -2
- C) slope: –2; *y*-intercept: 3
- D) slope: 3; y-intercept: -2
- E) slope: -2; y-intercept: -3

14. Determine whether lines L_1 and L_2 passing through the pairs of points are parallel, perpendicular, or neither.

$$L_1$$
: $(-1, 1), (-1, -6)$
 L_2 : $(3, -8), (24, -8)$

- A) parallel
- B) perpendicular
- C) neither
- 15. Show algebraically that the functions f and g shown below are inverse functions.

$$f(x) = \sqrt[3]{8x - 7}, \quad g(x) = \frac{x^3 + 7}{8}$$

$$A) \quad f(g(x)) = \sqrt[3]{8} \left(\frac{x^3 + 7}{8}\right) - 7$$

$$= \sqrt[3]{x^3 + 56 - 56}$$

$$= \sqrt[3]{x^3}$$

$$= x$$

$$B) \quad f(g(x)) = \sqrt[3]{8} \left(\frac{x^3 + 7}{8}\right) - 7$$

$$= \sqrt[3]{(x^3 + 7) - 7}$$

$$= \sqrt[3]{x^3 + 7 - 7}$$

$$= \sqrt[3]{x^3}$$

$$= x$$

$$g(f(x)) = \frac{(\sqrt[3]{8x - 7})^3 + 7}{8}$$

$$= \frac{8x}{8}$$

$$= x$$

$$g(f(x)) = \frac{(\sqrt[3]{8x - 7})^3 + 7}{8}$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{8x}{8}$$

$$= x$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{8x}{8}$$

$$= x$$

$$= x$$

$$= \frac{8x}{8}$$

$$= x$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{8x}{8}$$

$$= x$$

$$= \frac{8x}{8}$$

$$= x$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{8x}{8}$$

$$= x$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{8x - 7 + 7}{8}$$

$$= \frac{3\sqrt{x^3 + 7 - 7}}{8}$$

$$= \frac{8^3 x - 7 + 7}{8^3}$$

$$= \frac{8^3 x - 7 + 7}{8^3}$$

$$= \frac{8^3 x}{8^3}$$

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D)
$$f(g(x)) = \sqrt[3]{8\left(\frac{x^3+7}{8}\right)-7}$$
 $g(f(x)) = \frac{\left(\sqrt[3]{8x-7}\right)^3+7}{8}$
 $= \sqrt[3]{\left(8x^3+56\right)-56}$ $= \frac{8^3x-7^3+7^3}{8^3}$
 $= \sqrt[3]{8x^3+56-56}$ $= \frac{8^3x}{8^3}$
 $= x$ $= x$

E)
$$f(g(x)) = \sqrt[3]{8\left(\frac{x^3+7}{8}\right)-7}$$

 $= \sqrt[3]{x^3+\frac{7}{8}}-7$
 $= \sqrt[3]{8x-7} + \frac{7}{8}$
 $= \sqrt[3]{8x-7} + \frac{7}{8}$
 $= \frac{24x-21+21}{24}$
 $= \sqrt[3]{8x-7} + \frac{7}{8}$
 $= \frac{24x-21+21}{24}$
 $= \frac{24x}{24}$
 $= x$

16. Find all real values of x such that f(x) = 0.

$$f(x) = \frac{-2x+5}{5}$$

- A) $\frac{1}{2}$
- B) $\pm \frac{1}{2}$
- C) $\pm \frac{5}{2}$
- D) $\frac{5}{2}$
- E) $-\frac{5}{2}$

17. Compare the graph of the following function with the graph of f(x) = |x|.

$$y = \left| \frac{3}{4} x \right|$$

- A) vertical shift of $\frac{3}{4}$ units up
- B) horizontal stretch of $\frac{4}{3}$ units
- C) vertical shrink of $\frac{3}{4}$ units
- D) horizontal shrink of $\frac{3}{4}$ units vertical shift of $\frac{4}{3}$ units
- E) horizontal shrink of $\frac{3}{4}$ units
- 18. Find the domain of the function.

$$g(x) = \sqrt{25 - x^2}$$

- A) $-5 \le x \le 5$
- B) $x \le -5 \text{ or } x \ge 5$
- C) $x \ge 0$
- D) $x \le 5$
- E) all real numbers
- 19. Use the functions f(x) = x + 4 and g(x) = 5x 7 to find $(g \circ f)^{-1}$.

A)
$$(g \circ f)^{-1} = \frac{5x+11}{4}$$

B)
$$(g \circ f)^{-1} = 5x - 42$$

C)
$$(g \circ f)^{-1} = \frac{x - 13}{5}$$

D)
$$(g \circ f)^{-1} = \frac{-7x - 7}{5}$$

E)
$$(g \circ f)^{-1} = 5x + 13$$

20. Find the value(s) of x for which f(x) = g(x). $f(x) = x^2 - 11x - 36$ $g(x) = x^2 - 11x - 36$

$$f(x) = x^2 - 11x - 36$$

$$g(x) = -7x - 4$$

- A) $-36, -25, -\frac{4}{7}$ B) $-36, -11, -\frac{4}{7}$

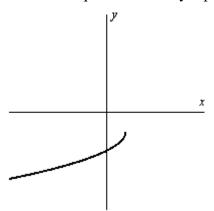
- C) 8, -4 D) -8, 4
- E) 47, $-\frac{4}{7}$

Answer Key

- 1. C
- 2. D
- 3. A
- 4. B
- 5. A
- 6. B
- 7. E
- 8. E
- 9. C
- 10. A
- 11. C
- 12. C
- 13. C
- 14. B
- 15. B
- 16. D
- 17. B
- 18. A
- 19. C
- 20. C

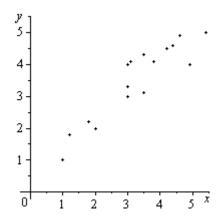
Name: _____ Date: _____

1. Determine an equation that may represented by the graph shown below.



- A) $f(x) = -1 \sqrt{1-x}$
- B) $f(x) = -1 + \sqrt{1-x}$
- C) $f(x) = -1 \sqrt{1+x}$
- D) $f(x) = -1 + \sqrt{1+x}$
- E) $f(x) = 1 \sqrt{1 x}$

2. The scatter plots of different data are shown below. Determine whether there is a positive correlation, negative correlation, or no discernible correlation between the variables.



- A) positive correlation
- B) negative correlation
- C) no discernible correlation

3. Does the table describe a function?

Input value	-6	-3	0	3	6
Output value	11	11	11	11	11

- A) yes
- B) no
- 4. Find the domain of the function.

$$g(w) = \frac{-7w}{w - 5}$$

- A) all real numbers $w \neq 5$
- B) all real numbers $w \neq 5$, $w \neq 0$
- C) all real numbers
- D) w = 5, w = 0
- E) w = 5
- 5. Determine the domain and range of the inverse function f^{-1} of the following function f.

$$f(x) = -|x+8|-3$$
, where $x > -8$

- A) Domain: $[-8,\infty)$; Range: $[-3,\infty)$
- B) Domain: $(-\infty, -3]$; Range: $[-8, \infty)$
- C) Domain: $\begin{bmatrix} -8, -3 \end{bmatrix}$; Range: $\begin{bmatrix} -8, \infty \end{bmatrix}$
- D) Domain: $(-\infty, -8]$; Range: $[3, \infty)$
- E) Domain: $(-\infty, \infty)$; Range: $(-\infty, \infty)$

6. Use function notation to write g in terms of $f(x) = x^3$.

$$g(x) = -\frac{1}{2}(x+9)^3$$

A)
$$g(x) = -\frac{1}{2} [f(x)]^3 + 9$$

B)
$$g(x) = -\frac{1}{2}[f(x) + 9]$$

C)
$$g(x) = -[f(x)]^3 + \frac{729}{2}$$

D)
$$g(x) = -\frac{1}{2} [f(x)]^3 + 729$$

E)
$$g(x) = -\frac{1}{2} [f(x+9)]$$

7. Evaluate the indicated function for $f(x) = x^2 - 1$ and g(x) = x - 6.

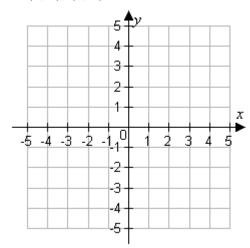
$$(fg)(-2)$$

- A) –24
- B) 40
- C) –2
- D) 12
- E) 24
- 8. If f is an even function, determine if g is even, odd, or neither.

$$g(x) = f(x+4)$$

- A) even
- B) odd
- C) cannot be determined
- D) neither

9. Plot the points and find the slope of the line passing through the pair of points. (1, 0), (5, 3)



- A) slope: $\frac{4}{3}$
- B) slope: $-\frac{4}{3}$
- C) slope: $\frac{1}{2}$
- D) slope: $\frac{3}{4}$
- E) slope: $-\frac{3}{4}$
- 10. Compare the graph of the following function with the graph of $f(x) = x^3$.

$$y = \left\lceil 5(x-2) \right\rceil^3$$

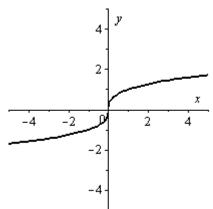
- A) vertical shift of 2 units down
- B) vertical shift of 2 units down horizontal shrink of $\frac{1}{5}$ units
- C) horizontal shift of 2 units to the right horizontal shrink of $\frac{1}{125}$ units
- D) horizontal shift of 2 units to the right horizontal stretch of $\frac{1}{5}$ units
- E) horizontal shift of 2 units to the right vertical shift of 5 units down

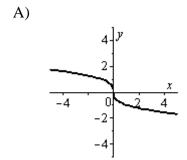
11. Find the slope-intercept form of the line passing through the points.

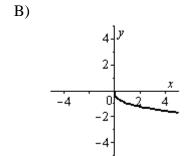
$$(-4, -2), (-1, 7)$$

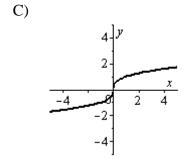
- A) y = 3x + 2
- B) y = 3x + 10
- C) $y = \frac{1}{3}x \frac{2}{3}$
- D) $y = -\frac{1}{3}x \frac{10}{3}$ E) y = -3x 14

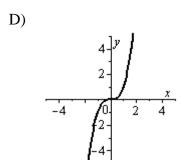
12. Match the graph of the function shown below with the graph of its inverse function

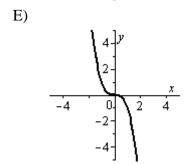






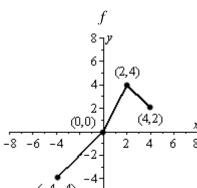


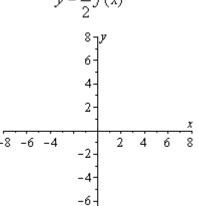




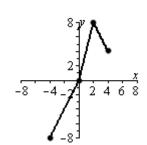
13. Use the graph of f to sketch the graph of the function indicated below.



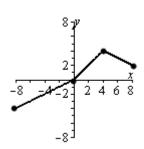




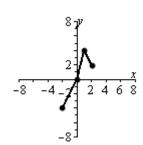
A)



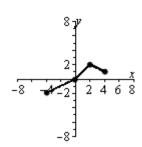
B)



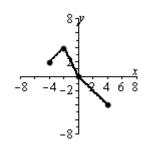
C)











14. Compare the graph of the following function with the graph of f(x) = |x|.

$$y = \left| \frac{7}{9} x \right|$$

- A) vertical shift of $\frac{7}{9}$ units up
- B) horizontal stretch of $\frac{9}{7}$ units
- C) vertical shrink of $\frac{7}{9}$ units
- D) horizontal shrink of $\frac{7}{9}$ units vertical shift of $\frac{9}{7}$ units
- E) horizontal shrink of $\frac{7}{9}$ units
- 15. Write the slope-intercept form of the equation of the line through the given point parallel to the given line.

point:
$$(3, -4)$$

line:
$$28x + 7y = -4$$

A)
$$y = -\frac{1}{28}x - \frac{109}{28}$$

B)
$$y = \frac{1}{4}x - \frac{19}{4}$$

C)
$$y = 28x + 80$$

D) $y = -4x + 8$

D)
$$y = -4x + 8$$

E)
$$y = -4x - 13$$

16. Does the table describe a function?

Input value	5	10	13	10	5
Output value	-13	-9	0	9	13

- A) yes
- B) no

17. Show algebraically that the functions f and g shown below are inverse functions.

$$f(x) = -\frac{5}{7}x - 3$$
, $g(x) = -\frac{7x + 21}{5}$

A)
$$f(g(x)) = -\frac{5}{7} \left(\frac{7x+21}{5}\right) - 3$$
 $g(f(x)) = -\frac{7\left(-\frac{5}{7}x-3\right)+21}{5}$
 $= \left(\frac{7x+21}{7}\right) - 3$ $= -\frac{(-5x-21)+21}{5}$
 $= (x+3)-3$ $= x+3-3$ $= x$ $= \frac{5x}{5}$
 $= x$

B)
$$f(g(x)) = -\frac{5}{7} \left(-\frac{7x+21}{5} \right) - 21$$
 $g(f(x)) = -\frac{7\left(-\frac{5}{7}x-3\right) + 21}{5}$
 $= \left(\frac{35x+21}{35} \right) - 21$ $= -\frac{(-5x-3)+21}{5}$
 $= (x+21)-21$ $= \frac{5x+3-21}{5}$
 $= x+21-21$ $= \frac{5x}{5}$

C)
$$f(g(x)) = -\frac{5}{7} \left(-\frac{7x+3}{5}\right) - 3$$
 $g(f(x)) = -\frac{7\left(-\frac{5}{7}x-3\right) + 21}{5}$
 $= \left(\frac{35x+3}{35}\right) - 3$ $= -\frac{(-5x-3)+3}{5}$
 $= (x+3)-3$ $= x+3-3$ $= x$

D)
$$f(g(x)) = -\frac{5}{7} \left(-\frac{7x+21}{5} \right) - 3$$
 $g(f(x)) = -\frac{7\left(-\frac{5}{7}x-3\right) + 21}{5}$
 $= \left(\frac{7x+21}{7} \right) - 3$ $= (x+3)-3$ $= x$ $= \frac{5x}{5}$
 $= x + 3 - 3$ $= (x+3)-3$ $= (x+3)-3$ $= (x+3)-3$ $= x$ $= (x+3)-3$ $= x + 3 - 3$ $= \frac{35x}{35}$

18. Find the domain of the function.

$$f(t) = \sqrt{64 - t^2}$$

- A) $-8 \le t \le 8$
- B) $t \le -8$ or $t \ge 8$
- C) $t \ge 0$
- D) $t \le 8$
- E) all real numbers

19. Find the inverse function of f.

$$f(x) = x^9 - 2$$

- A) $f^{-1}(x) = -\sqrt[9]{x} 2$
- B) $f^{-1}(x) = \sqrt[9]{x} 2$
- C) $f^{-1}(x) = -\sqrt[9]{x-2}$
- D) $f^{-1}(x) = \sqrt[9]{x+2}$
- E) $f^{-1}(x) = \sqrt[9]{x} + 2$
- 20. Find $f \circ g$.

$$f(x) = -4x + 3$$

$$g(x) = x + 7$$

- f(x) = -4x + 3 g(x) = x + 7A) $(f \circ g)(x) = -4x 25$
- B) $(f \circ g)(x) = -4x + 10$
- C) $(f \circ g)(x) = -4x^2 25x + 21$
- D) $(f \circ g)(x) = -5x 4$
- E) $(f \circ g)(x) = -5x + 10$

Answer Key

- 1. A
- 2. A
- 3. A
- 4. A
- 5. B
- 6. E
- 7. A
- 8. C
- 9. D
- 10. C
- 11. B
- 12. D
- 13. D
- 14. B
- 15. D
- 16. B
- 17. D
- 18. A
- 19. D
- 20. A

Name:	Date:	

1. Hooke's Law states that the force F required to compress or stretch a spring (within its elastic limits) is proportional to the distance d that the spring is compressed or stretched from its original length. That is, F = kd, where k is the measure of the stiffness of the spring and is called the *spring constant*. The table below shows the elongation d in centimeters of a spring when a force of F kilograms is applied.

Force, F	Elongation, d
20	1.4
40	2.5
60	4.0
80	5.3
100	6.6

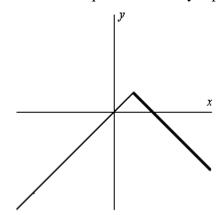
Find the equation of the line that seems to best fit the data. Use the model to estimate the elongation of the spring when a force of 55 kilograms is applied. Round your answer to one decimal place.

- A) 7.2 centimeters
- B) 5.4 centimeters
- C) 1.8 centimeters
- D) 3.6 centimeters
- E) 2.7 centimeters
- 2. If f is an even function, determine if g is even, odd, or neither.

$$g(x) = -f(x+3)$$

- A) even
- B) odd
- C) cannot be determined
- D) neither

- 3. Given $f(x) = \frac{10}{x^2 9}$ and g(x) = x + 3 determine the domain of $f \circ g$.
 - A) $\left(-\infty, -3\right) \cup \left(3, \infty\right)$
 - B) $(-\infty, -6) \cup (-6, 0) \cup (0, \infty)$
 - C) $\left(-\infty, -\frac{10}{3}\right) \cup \left(\frac{10}{3}, \infty\right)$
 - D) $\left(-\infty, -3\right) \cup \left(-3, 3\right) \cup \left(3, \infty\right)$
 - E) $\left(-\infty,\infty\right)$
- 4. Determine an equation that may represented by the graph shown below.



- A) f(x) = |x+1|+1
- B) f(x) = |x+1|-1
- C) f(x) = -|x-1|+1
- D) f(x) = |x-1|+1
- E) f(x) = |x-1|-1

5. Find all real values of x such that f(x) = 0.

$$f(x) = 49x^2 - 64$$

- A) $\pm \frac{7}{8}$
- B) $\pm \frac{8}{7}$
- C) $\pm \frac{64}{49}$
- D) $-\frac{64}{49}$
- E) $\frac{8}{7}$

6. Find
$$(f+g)(x)$$
.

$$f(x) = -8x^2 + 5x - 2$$

$$g(x) = 4x^2 + 7x + 4$$
A) $(f+g)(x) = -12x^4 - 2x^2 - 6$

$$g(x) = 4x + 7x + 4$$

A) $(f+g)(x) = -12x^4 - 2x^2$

B)
$$(f+g)(x) = -4x^4 + 12x^2 + 2$$

C)
$$(f+g)(x) = -12x^2 - 2x - 6$$

C)
$$(f+g)(x) = -12x^2 - 2x - 6$$

D) $(f+g)(x) = -4x^2 + 12x + 2$

E)
$$(f+g)(x) = 4x^2 - 12x - 2$$

7. Find $f \circ g$.

$$f(x) = x + 4$$

$$f(x) = x + 4$$
 $g(x) = \frac{3}{x^2 - 16}$

A)
$$(f \circ g)(x) = \frac{3}{x^2}$$

B)
$$(f \circ g)(x) = \frac{3}{x^2 + 8x}$$

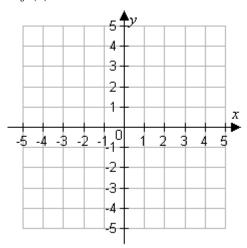
C)
$$(f \circ g)(x) = \frac{4x^2 - 1}{x^2 - 16}$$

D)
$$(f \circ g)(x) = \frac{7}{x^2 - 16}$$

E)
$$(f \circ g)(x) = \frac{4x^2 - 61}{x^2 - 16}$$

8. Graph the function and determine the interval(s) for which $f(x) \ge 0$.

$$f(x) = -x^2 + 4x$$



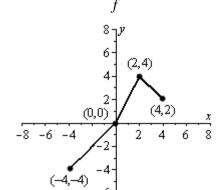
- A) $(-\infty,0] \cup [4,\infty)$
- B) [0,4]
- C) (0,4)
- D) $(-\infty,0) \cup (4,\infty)$
- E) {4}
- 9. Restrict the domain of the following function f so that the function is one-to-one and has an inverse function.

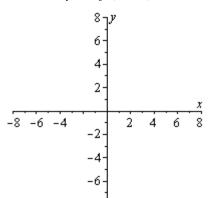
$$f(x) = -|x-4| + 2$$

- A) $\left[-4,\infty\right)$
- B) [2,4]
- C) $[4,\infty)$
- D) [-2,4]
- E) $\left(-\infty,2\right]$

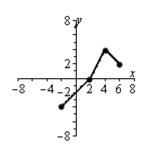
10. Use the graph of f to sketch the graph of the function indicated below.



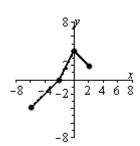




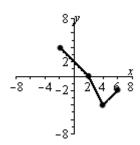
A)



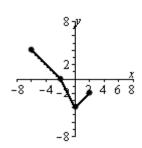
B)



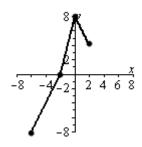
C)



D)



E)



11. Algebraically determine whether the function below is even, odd, or neither.

$$f(s) = 8s^{7/6}$$

- A) even
- B) odd
- C) cannot be determined
- D) neither

12. Compare the graph of the following function with the graph of $f(x) = \sqrt{x}$.

$$y = \sqrt{-x + 4}$$

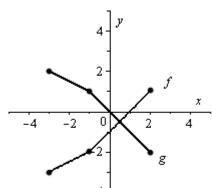
- A) First a vertical shift of 4 units up then a reflection in the y-axis.
- B) First a horizontal shift of 4 units to the left then a reflection in the y-axis.
- C) First a vertical shift of 4 units up then a reflection in the x-axis.
- D) First a horizontal shift of 4 units to the left, then a vertical shift of 4 units up and then a reflection in the *y*-axis.
- E) First a horizontal shift of 4 units to the left then a reflection in the x-axis.

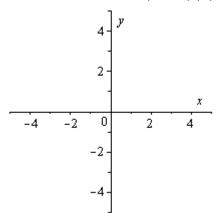
13. Find the domain of the function.

$$g(p) = \sqrt{4 - p^2}$$

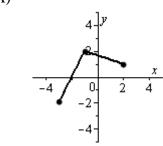
- A) $-2 \le p \le 2$
- B) $p \le -2$ or $p \ge 2$
- C) $p \ge 0$
- D) $p \le 2$
- E) all real numbers

14. Use the graphs of f and g, shown below, to graph h(x) = (f + g)(x).

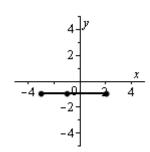




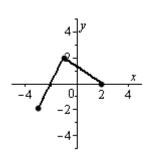
A)



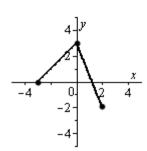
B)



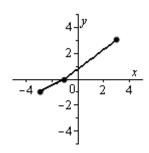
C)



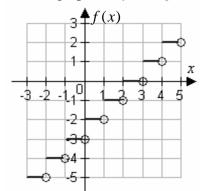
D)

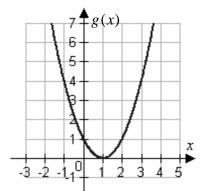


E)



15. Use the graphs of f and g to evaluate the function.





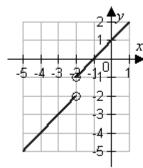
$$(f \circ g)(1)$$

- A) 9
- B) -1
- C) 0
- D) -4
- E) -2

16. Find the slope and y-intercept of the equation of the line.

$$y = -2x - 9$$

- A) slope: $-\frac{1}{2}$; y-intercept: -9
- B) slope: $-\frac{1}{9}$; y-intercept: -2
- C) slope: -2; y-intercept: -9
- D) slope: -9; y-intercept: -2
- E) slope: -2; y-intercept: 9
- 17. Use the graph of the function to find the domain and range of f.



A) domain: all real numbers

$$range: (-\infty,-2) \bigcup (-1,\infty)$$

B) domain: all real numbers

C) domain: $(-\infty, -2) \cup (-2, \infty)$

range:
$$(-\infty, -2) \cup (-1, \infty)$$

D) domain: $(-\infty, -2) \cup (-1, \infty)$

range:
$$(-\infty, -2) \cup (-2, \infty)$$

E) Domain: all real numbers

Range:
$$(-\infty, -2] \cup [-1, \infty)$$

18. Given that $f(x) = \sqrt[4]{x-4}$ and $g(x) = x^4 + 4$ determine the value of the following (if possible).

$$(f \circ g)(0)$$

- A) 0
- B) 2
- C) 4
- D) $x^4 16$
- E) not possible
- 19. Find the inverse function of f(x) = 8x + 3
 - A) $g(x) = \frac{x-3}{8}$
 - B) g(x) = 3x + 8
 - $C) \quad g(x) = \frac{x+3}{8}$

 - D) $g(x) = \frac{x}{3}$ E) $g(x) = \frac{1}{8}x 3$

20. Show algebraically that the functions f and g shown below are inverse functions.

$$f(x) = \frac{2}{2+x}, x \ge 0, \quad g(x) = \frac{2-2x}{x}, 0 < x \le 1$$

A)
$$f(g(x)) = \frac{2}{2 + \left(\frac{2 - 2x}{x}\right)}$$

$$= \frac{2}{2 + \left(\frac{1}{x}\right)}$$

$$= \frac{1}{\left(\frac{1}{x}\right)}$$

$$= 1 \cdot \frac{x}{1}$$

$$= x$$

$$g(f(x)) = \frac{2 - 2\left(\frac{2}{2 + x}\right)}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{0 - \left(\frac{2}{2 + x}\right)}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{-2}{2 + x}$$

$$= \left(\frac{-2}{2 + x}\right)\left(\frac{2 + x}{2}\right)$$

$$= \frac{2x + 2}{2 + x}$$

$$= x$$

B)
$$f(g(x)) = \frac{2}{2 + \left(\frac{2 - 2x}{x}\right)}$$

$$= \frac{1}{1 + \frac{2 - 2x}{x}}$$

$$= \frac{1}{\left(\frac{0}{x}\right)}$$

$$= x$$

$$g(f(x)) = \frac{2 - 2\left(\frac{2}{2 + x}\right)}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{2 - \left(\frac{4}{2 + x}\right)}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{4 + 2x - 4}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{2x}{\left(\frac{x}{2 + x}\right)}$$

$$= \frac{2x}{2 + x}$$

C)
$$f(g(x)) = \frac{2}{2 + \left(\frac{2 - 2x}{x}\right)}$$

$$= \frac{4}{\frac{2 - 2x}{x}}$$

$$= \frac{2}{\left(\frac{2x}{x}\right)}$$

$$= \frac{2}{\left(\frac{2x}{x}\right)}$$

$$= \frac{2 \cdot \frac{x}{2}}{\left(\frac{2x}{x}\right)}$$

$$= \frac{2 \cdot \frac{x}{2}}{\left(\frac{2x}{x}\right)}$$

$$= \frac{2 \cdot \frac{x}{2}}{\left(\frac{2x}{x}\right)}$$

$$= \frac{2 \cdot \frac{x}{2}}{\left(\frac{2x}{x}\right)}$$

$$= \frac{2 \cdot x}{2 + 2x}$$

$$= \frac{x}{2x}$$

D)
$$f(g(x)) = \frac{2}{2 + \left(\frac{2 - 2x}{x}\right)}$$

$$= \frac{2}{2x + 2 - 2x}$$

$$= \frac{2 - 2x}{x}$$

$$= \frac{2 - 2x}{\left(\frac{2}{x}\right)}$$

$$= \frac{\left(\frac{4}{2 + x}\right)}{\left(\frac{2}{2 + x}\right)}$$

$$= \left(\frac{4}{2 + x}\right)$$

$$= \left(\frac{4}{2 + x}\right)\left(\frac{2 + x}{2}\right)$$

$$= \frac{1 - x}{1}$$

$$= x$$

$$= \frac{2(2 + x)}{2 + x}$$

$$= \frac{2x}{2}$$

$$= x$$

E)
$$f(g(x)) = \frac{2}{2 + \left(\frac{2 - 2x}{x}\right)}$$

$$= \frac{2}{2x + 2 - 2x}$$

$$= \frac{2}{\left(\frac{2}{x}\right)}$$

$$= \frac{2 \cdot \frac{2}{\left(\frac{2}{x}\right)}}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{2 \cdot \frac{4}{2 + x}}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{4 + 2x - 4}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{2x}{\left(\frac{2}{2 + x}\right)}$$

$$= \frac{2x}{2}$$

Answer Key

- 1. D
- 2. C
- 3. B
- 4. C
- 5. B
- 6. D
- 7. E
- 8. B
- 9. C 10. E
- 11. D
- 12. B
- 13. A
- 14. B
- 15. E
- 16. C 17. C
- 18. A
- 19. A
- 20. E