### **Chapter 02: Quadratic and Other Special Functions**

 $x^2 - 3x + 6 = 4 - 4x^2$  in general form. 1. Write the equation

a. 
$$5x^2 + 3x + 4 = 0$$

b. 
$$-x^2-3x+4=0$$

c. 
$$5x^2-3x+2=0$$

d. 
$$x^2-3x-2=0$$

e. 
$$5x^2 + 3x - 4 = 0$$

ANSWER: С

2. Write the equation (z-5)(z-6)=8 in general form.

a. 
$$z^2 - 11z + 22 = 0$$

b. 
$$z^2 + 11z + 30 = 0$$

c. 
$$z^2 - 6z + 22 = 0$$

d. 
$$z^2 - 6z + 30 = 0$$

e. 
$$z^2 + 6z + 30 = 0$$

ANSWER: а

 $x^2 + 5x = x + 12$ 3. Solve the equation

$$x = -2, x = 6$$

b. 
$$x = 2, x = 6$$

c. 
$$x = -2$$
,  $x = -6$ 

d. 
$$x = 4$$
,  $x = -12$ 

e. 
$$x = 2, x = -6$$

ANSWER: е

4. Solve the equation  $9x^2 - 6x + 1 = 0$  by factoring.

a. 
$$x = -\frac{1}{3}$$

b. 
$$x = \frac{1}{3}$$

#### **Chapter 02: Quadratic and Other Special Functions**

$$x = 3$$

d. 
$$x = \frac{1}{6}$$

e. 
$$x = \frac{1}{3}, x = -\frac{1}{3}$$

ANSWER: b

5. Solve the equation by using the quadratic formula. Give real solutions only.

$$4x^2+x+3=0$$

a. 
$$x = \frac{1 \pm \sqrt{-47}}{8}$$

b. 
$$x = \frac{-1 \pm \sqrt{-47}}{8}$$

c. 
$$x = \frac{-1 \pm \sqrt{49}}{8}$$

d. no real solutions

$$x = \frac{-1 \pm \sqrt{-47}}{4}$$

ANSWER: d

6. Solve the equation by using the quadratic formula. Give real answers rounded to two decimal places.

$$6x^2 = 3x + 7$$

a. 
$$x = 1.36$$
,  $x = -0.86$ 

b. 
$$x = -1.36, x = -0.86$$

c. 
$$x = 15.00, x = 13.50$$

d. 
$$x = 1.72, x = -0.36$$

e. 
$$x = 1.69, x = -0.53$$

ANSWER: a

7. Find the exact real solutions to the equation, if they exist.

$$y^2 = 7$$

### **Chapter 02: Quadratic and Other Special Functions**

a. 
$$y = \pm 7$$

b. 
$$y = \sqrt{7}$$

c. 
$$y = 3.5$$

d. 
$$y = \pm \sqrt{7}$$

e. no real solutions

ANSWER: d

8. Find the exact real solutions to the equation, if they exist.

$$(x+7)^2 = 64$$

$$x = 1, x = -15$$

b 
$$x = \pm 8$$

c. 
$$x = 57$$

d. 
$$x = 71$$

$$e. x = 8$$

ANSWER: а

 $x^2 + 17x = 8x - 14$ , if they exist. 9. Find the exact real solutions of the equation

a. 
$$x=2$$
 and  $x=7$ 

b. 
$$x = -2$$
 and  $x = -7$   
c.  $x = 3$  and  $x = 8$ 

c. 
$$x = 3$$
  $x = 8$ 

d. 
$$x = 3$$
 and  $x = -7$ 

e. 
$$x = -3$$
 and  $x = -8$ 

ANSWER: b

 $\frac{5}{32}y^2 - \frac{11}{8}y + 1 = 0$ , if they exist. 10. Find the exact real solutions of the equation

a. 
$$y = -\frac{4}{5}$$
 and  $y = -8$ 

b. 
$$y = 4$$
 and  $y = 8$ 

c. 
$$y = -4$$
 and  $y = -8$ 

d. 
$$y = \frac{4}{5}$$
 and  $y = 8$ 

### **Chapter 02: Quadratic and Other Special Functions**

e. 
$$y = -8$$
 and  $y = 4$ 

ANSWER:

d

$$13x^2 = -26x - 2$$
, if they exist.

11. Find the exact real solutions of the equation

a. 
$$x = -1 + \frac{3\sqrt{13}}{13}$$
  $x = -1 - \frac{3\sqrt{13}}{13}$ 

b. 
$$x = -1 + \frac{\sqrt{143}}{13}$$
 and  $x = -1 - \frac{\sqrt{143}}{13}$ 

c. 
$$x = -1 + \frac{\sqrt{167}}{13}$$
 and  $x = -1 - \frac{\sqrt{167}}{13}$ 

d. 
$$x = -1 + \frac{\sqrt{143}}{2}$$
  $x = -1 - \frac{\sqrt{143}}{2}$ 

Real solutions do not exist.

ANSWER:

b

12. Solve the equation by using a graphing utility.

$$-14x + 168 - 7x^2 = 0$$

a. 
$$x = 4, x = -6$$

b. 
$$x = 4, x = -4$$

c. 
$$x = -56$$
,  $x = 42$ 

d. 
$$x = -4, x = 6$$

e. 
$$x = -6$$
,  $x = 84$ 

ANSWER:

а

$$2.4z^2 - 7.4z - 2.4 = 0$$

 $2.4z^2 - 7.4z - 2.4 = 0$  by using a graphing utility. Round your answers to two decimal 13. Solve the equation places.

a. 
$$z \approx 3.15$$
 and  $z \approx -0.07$ 

b. 
$$z \approx 3.51$$
 and  $z \approx -0.43$ 

c. 
$$z \approx 3.38$$
 and  $z \approx -0.30$ 

d. 
$$z \approx 5.85$$
 and  $z \approx -2.77$ 

e. 
$$z \approx 5.77$$
 and  $z \approx -2.69$ 

### ANSWER:

С

$$x + \frac{4}{x} = 5$$

14. Multiply both sides of the equation

by the LCD, and then solve the resulting quadratic equation.

a. 
$$x = 4, x = 1$$

b. 
$$x = 5, x = 1$$

c. 
$$x = 4, x = 5$$

d. 
$$x = 1, x = -1$$

$$x = 4, x = -1$$

ANSWER:

а

$$\frac{x}{x-1} = 2x + \frac{1}{x-1}$$

15. Solve the equation x-1 by first multiplying by the LCD, and then solving the resulting equation.

$$x=1$$

b. 
$$x = -1$$

$$x = -\frac{1}{2}$$

$$d. x = \frac{1}{2} x = 1$$

$$x = \frac{1}{2}$$

ANSWER:

d

16. Solve the equation below using quadratic methods.

$$(x+7)^2+7(x+7)+6=0$$

a. 
$$x = 13, x = 8$$

b. 
$$x = 7, x = 6$$

c. 
$$x = 1, x = 1$$

d. 
$$x = -13$$
,  $x = -8$ 

e. 
$$x = 7, x = 7$$

ANSWER:

d

17. If the profit from the sale of x units of a product is  $p = 85x - 150 - x^2$ , what level(s) of production will yield a profit of \$1,600?

- a. less 35 units of production.
- b. more than 50 units of production.
- c. 85 units of production.
- d. 15 units of production.
- e. 35 or 50 units of production.

ANSWER: e

18. If a ball is thrown upward at 80 feet per second from the top of a building that is 100 feet high, the height of the ball can be modeled by , where t is the number of seconds after the ball is thrown. How long after it is thrown is the height 100 feet?

a. 
$$t=5$$
 seconds

b. 
$$t = 40$$
 seconds

c. 
$$t=1$$
 seconds

d. 
$$t = 80$$
 seconds

e. 
$$t = 6.04$$
 seconds

ANSWER:

19. The amount of airborne particulate pollution p from a power plant depends on the wind speed s, among other things, with the relationship between p and s approximated by  $p = 16 - 0.01s^2$ . Find the value of s that will make p = 0.

a. 
$$s = 400$$

b. 
$$s = 50$$

c. 
$$s = 40$$

ANSWER:

20. The sensitivity S to a drug is related to the dosage size by , where x is the dosage size in milliliters. Determine all dosages that yield 0 sensitivity.

a. 
$$x=0$$
 milliliters,  $x=5$  milliliters

b. 
$$x = 0$$
 milliliters,  $x = 50$  milliliters

c. 
$$x = 0$$
 milliliters,  $x = -50$  milliliters

d. 
$$x = -50$$
 milliliters,  $x = 50$  milliliters

e. 
$$x = 0$$
 milliliters

ANSWER:

21. The time t, in seconds, that it takes a 2005 Corvette to accelerate to x mph can be described  $t = 0.001[0.723x^2 + 15.417x + 607.732]$ 

by . How fast is the Corvette going after 9.08 seconds? Give your answer to the nearest tenth.

- a. 97.1 mph
- b. 98.1 mph
- c. 100.1 mph
- d. 118.9 mph
- e. 119.4 mph

ANSWER: b

22. Suppose that the percent of total personal income that is used to pay personal taxes is given by  $v = 0.034x^2 - 0.044x + 12.642$ 

, where *x* is the number of years past 1990 (*Source*: Bureau of Economic Analysis, U.S. Department of Commerce). Find the year or years when the percent of total personal income used to pay personal taxes is 20 percent.

- a. 2015
- b. 2005
- c. 2004
- d. 2010
- e. 2050

ANSWER: b

23. A fissure in the earth appeared after an earthquake. To measure its vertical depth, a stone was dropped into it, and the sound of the stone's impact was heard 3.3 seconds later. The distance (in feet) the stone fell is given by  $s = 12t_1^2$ , and the distance (in feet) the sound traveled is given by  $s = 1.092t_2$ . In these equations, the distances traveled by the sound and the stone are the same, but their times are not. Using the fact that the total time is 3.3 seconds, find the depth of the fissure. Round your answer to two decimal places.

- a. 94.19 feet
- b. 91.00 feet
- c. 121.98 feet
- d. 126.38 feet
- e. 126.48 feet

ANSWER: c

b

### **Chapter 02: Quadratic and Other Special Functions**

 $y = 11.768x^2 - 142.214x + 493$  24. An equation that models the number of users of the Internet is million users where x is the number of years past 1990 (*Source: CyberAtlas*, 1999). If the pattern indicated by the model remains valid, when does this model predict there will be 1,100 million users?

- a. 2004
- b. 2021
- c. 2014
- d. 2007
- e. 2005

ANSWER:

е

25. The model for body-heat loss depends on the coefficient of convection K, which depends on wind speed V according to the equation where V is in miles per hour. Find the positive coefficient of convection when the wind speed is 42 mph. Round your answer to the nearest integer.

- a. **K**≈ 18
- b.  $K \approx 28$
- c.  $K \approx 3$
- d. K≈6
- e. *K*≈26

ANSWER: b

26. Find the vertex of the graph of the equation  $y = 0.0625x^2 + x$ 

- a. (8, -4)
- b. (8, 4)
- c. (-4, -8)
- d. (-8, -4)
- e. (0, 16)

ANSWER:

27. Determine if the vertex of the graph of the equation is a maximum or minumim point.

$$y = \frac{1}{8}x^2 + 4$$

- a. vertex is at a maximum point
- b. vertex is at a minimum point
- c. has no vertex

ANSWER: b

28. Find the vertex of the graph of the equation  $y=3x^2-4x$ . Round your answer to two decimal places.

- a. (0.67, -1.33)
- b. (3.00, -4.00)
- c. (0, 1.33)
- d. (-1.33, 0.67)
- e. (1.33, -1.33)

ANSWER: a

29. Determine what value of x gives the optimal value of the function, and determine the optimal (maximum or minimum) value. Round your answers to two decimal places.

$$y = 2x^2 - 3x$$

- a. optimal value of x: 0, optimal value: 1.00
- b. optimal value of x: -1.13, optimal value: 0.75
- c. optimal value of x: 1.50, optimal value: -1.50
- d. optimal value of x: -0.75, optimal value: -1.13
- e. optimal value of x: 0.75, optimal value: -1.13

ANSWER: e

30. Determine whether the function's vertex is a maximum point or a minimum point and find the coordinates of this point.

$$y = x^2 + 4x + 14$$

- a. vertex: (-2, 10), a minimum point
- b. vertex: (2, -18), a maximum point
- c. vertex: (2, -18), a minimum point
- d. vertex: (-2, 10), a maximum point
- e. vertex: (-18, 2), a maximum point

ANSWER:

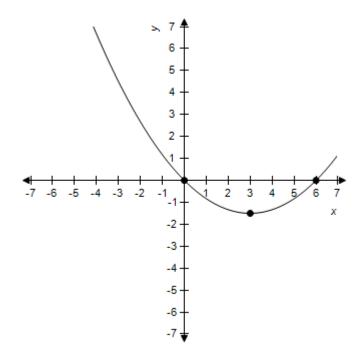
31. Sketch the graph of the following function.

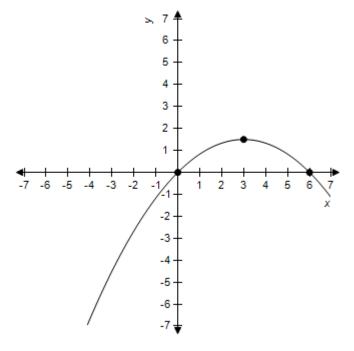
b

# **Chapter 02: Quadratic and Other Special Functions**

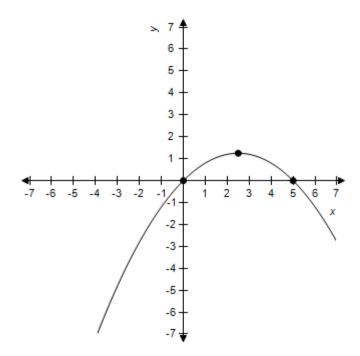
$$y = x - \frac{1}{6}x^2$$

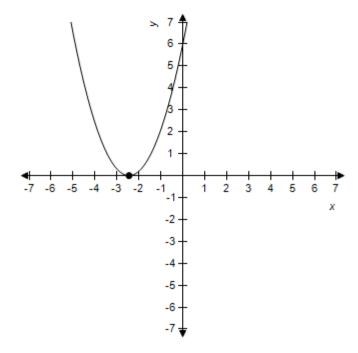
a





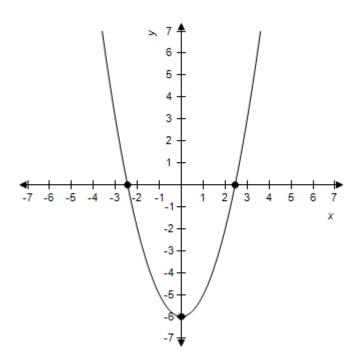
c d





### **Chapter 02: Quadratic and Other Special Functions**

e



ANSWER: b

32. Find the zeros, if any exist. Round your answers to two decimal places.

$$y = x^2 + 10x + 17$$

- zeros at -2.17 and -7.83 a.
- zeros at 0 and 10.00 b.
- c. zeros at 11.00 and -21.00
- d. no zeros
- e. zeros at 0 and 27.00

ANSWER:

а

33. Determine whether the vertex of the graph of the following function is a maximum point or a minimum point. Also find the coordinates of the vertex.

$$\frac{1}{6}x^2 + 3x - y - 7 = 0$$

- vertex: (-9, -20.5), a maximum point
- vertex: (-9, -20.5), a minimum point

b

e:

### **Chapter 02: Quadratic and Other Special Functions**

- vertex: (9, -20.5), a minimum point
- vertex: (18, 101), a minimum point d.
- vertex: (-20.5, 9), a maximum point

ANSWER:

34. Find the x-intercepts, if any exist. Round your answers to two decimal places.

$$\frac{1}{6}x^2 + 3x - y - 7 = 0$$

- x-intercepts: x = -9.00, x = -20.50x-intercepts: x = -2.09, x = 20.09x-intercepts: x = 2.09, x = -20.09b.
- c.
- *x*-intercepts: x = 18.00 x = 101.00d.
- no x-intercepts e.

ANSWER: С

35. How is the graph of  $y=x^2$  shifted to obtain the graph of the function  $y=(x-3)^2+6$ ?

- shifted 3 units to the left and 6 units up a.
- shifted 3 units to the right and 6 units down b.
- shifted 9 units to the left and 6 units up
- shifted 6 units to the right and 6 units down d.
- shifted 3 units to the right and 6 units up e.

ANSWER: е

36. Use a graphing utility to find the vertex of the function. Round your answer to two decimal places.

$$y = \frac{1}{20}x^2 - x - \frac{27}{20}$$

- vertex: (10.00, -6.35) a.
- vertex: origin b.
- vertex: (10.00, 16.35) c.
- vertex: (10.00, 13.65) d.
- vertex: (-10.00, -6.35) e.

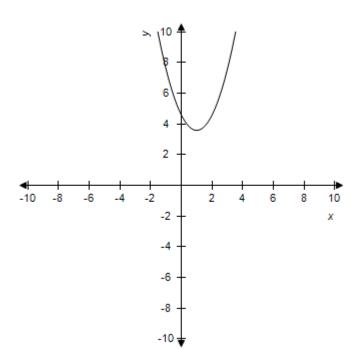
ANSWER: а

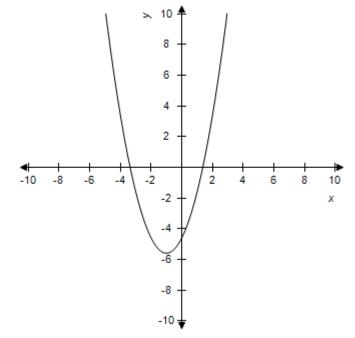
37. Sketch the graph of the following function by using graphing calculator.

$$y = \frac{1}{4}x^2 + 3x + 11$$

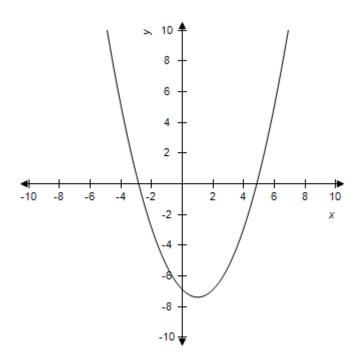
a

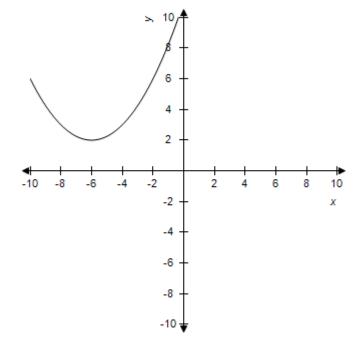
b



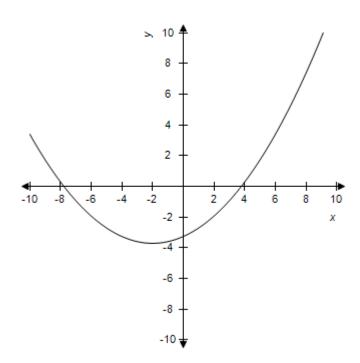


d





e



ANSWER:

38. Find the average rate of change of the function between the given values of x.

d

### **Chapter 02: Quadratic and Other Special Functions**

$$y = -5x - x^2$$
 between  $x = -6$  and  $x = 1$ .

a.

7

b.

6

c.

0

d. e. -6 12

ANSWER:

С

39. Find the vertex and then determine the range of the function.

$$y = 66 + 0.2x - 0.01x^2$$

a. all values greater than or equal to 67

b. all values less than or equal to 63

c. all values greater than or equal to 10

d. all values less than or equal to 85

e. all values less than or equal to 67

ANSWER:

е

40. Use a graphing utility to approximate the solutions to f(x) = 0. Round your answers to two decimal places.

$$f(x) = 3x^2 - 24x + 19$$

a. 
$$x = 21.33, x = 2.67$$

b. 
$$x = -0.89$$
,  $x = -7.11$ 

c. 
$$x = 7.11, x = 0.89$$

d. 
$$x = 4.00$$
,  $x = -29.00$ 

e. 
$$x = -7.11, x = 0.89$$

ANSWER:

С

41. Factor the function  $f(x) = 2x^2 - 21x + 49$ 

a. 
$$f(x) = (x-7)(x-7)$$

b. 
$$f(x) = -21(x-7)(2x-7)$$

c. 
$$f(x) = (x-7)(2x-7)$$

d. 
$$f(x) = (x+7)\left[x-\frac{7}{2}\right]$$

e. 
$$f(x) = (7x-1)(2x-7)$$

ANSWER:

С

42. Solve f(x) = 0 for the function  $f(x) = 3x^2 - 16x + 16$ 

a. 
$$x = \frac{4}{3}$$
,  $x = -16$ 

b. 
$$x = 4, x = -\frac{4}{3}$$

c. 
$$x = 4, x = \frac{3}{4}$$

d. 
$$x = 4, x = \frac{4}{3}$$

no real solutions e.

ANSWER:

d

 $P = 20x - 0.2x^2 - 97$  dollars. What level of production 43. The daily profit from the sale of a product is given by maximizes profit?

- production level of 100 units a.
- b. production level of 10 units
- production level of 5 units c.
- production level of 50 units d.
- production level of 95 units e.

ANSWER:

d

 $P = 16x - 0.2x^2 - 100$ 44. The daily profit from the sale of a product is given by dollars. What is the maximum possible profit? Round intermediate calculations and final answer to the nearest dollar.

ANSWER:

С

 $P = 82x - 0.3x^2 - 180$ 

45. The daily profit from the sale of a product is given by dollars. What is the maximum possible profit? Round intermediate calculations and final answer to the nearest dollar.

- a. \$5,423
- b. \$16,685
- c. \$11,013
- d. \$137
- e. \$271

ANSWER:

46. The yield in bushels from a grove of orange trees is given by Y = x(1,000 - x), where x is the number of orange trees per acre. How many trees will maximize the yield?

- a. 1,000 trees
- b. 2,000 trees
- c. 550 trees
- d. 1.050 trees
- e. 500 trees

ANSWER: e

47. The sensitivity S to a drug is related to the dosage x in milligrams by

determine what dosage gives maximum sensitivity.

S =  $9/0x - x^2$ Use a graphing utility to determine what dosage gives maximum sensitivity.

- a. 97
- b. 235,225
- c. 970, 0
- d. 970
- e. 485

ANSWER: e

48. A ball thrown vertically into the air has its height above ground given by  $s = 121t - 16t^2$ , where t is in

48. A ball thrown vertically into the air has its height above ground given by t, where t is ir seconds and t is in feet. Find the maximum height of the ball.

- a. 242 feet
- b. 121 feet
- c. 8 feet
- d. 16 feet
- e. 229 feet

ANSWER: e

### **Chapter 02: Quadratic and Other Special Functions**

49. The owner of a skating rink rents the rink for parties at \$696 if 58 or fewer skaters attend, so that the cost per person is \$12 if 58 attend. For each 5 skaters above 58, she reduces the price per skater by \$0.50. Which table gives the revenue generated if 58, 68, and 78 skaters attend?

a

u.		_	
	Price	No. of skaters	Total Revenue
	12	58	\$780
	11	68	\$748
	10	78	\$696

b.

Price	No. of skaters	Total Revenue
12	58	\$696
13	68	\$748
14	78	\$780

c.

Price	No. of skaters	Total Revenue
12	58	\$696
11	68	\$748
10	78	\$780

d.

_	Price	No. of skaters	Total Revenue
	12	58	\$696
	13	68	\$884
	14	78	\$1092

e.

Price	No. of skaters	Total Revenue
12	58	\$696
11.5	68	\$782
11	78	\$858

ANSWER:

50. When a stone is thrown upward, it follows a parabolic path given by a form of the equation  $x = ax^2 + bx + c$ . If y = 0 represents ground level, find the equation of a stone that is thrown from ground level at x = 0 and lands on the ground 130 units away if the stone reaches a maximum height of 130 units.

a. 
$$y = -\frac{1}{65}x^2 + 2x$$

b. 
$$y = -\frac{2}{65}x^2 + 4x$$

c. 
$$y = 4x^2 - \frac{2}{65}x$$

d. 
$$y = -2x^2 - \frac{1}{65}x$$

e. 
$$v = 2(x^2 + 65x)$$

ANSWER:

51. In 1995, America's 45 million Social Security recipients received a 2.6% cost-of-living increase, the second smallest increase in nearly 20 years, a reflection of lower inflation. The percent increase might be described by  $p(t) = -0.4375t^2 + 8.2t - 34.3625$ 

, where t is the number of years past 1980. In what year does the model predict the highest cost of living percent increase?

- a. 1990
- b. 2009
- c. 1987
- d. 1989
- none of the above e.

ANSWER:

d

52. Sketch the first quadrant portions of the following functions and estimate the market equilibrium point.

b

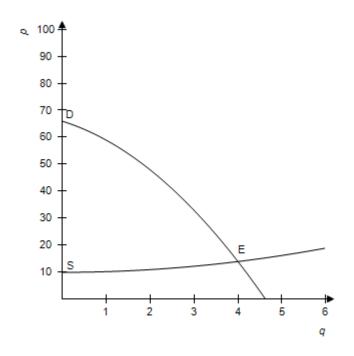
$$p = \frac{1}{2}q^2 + 10$$

Supply:

$$p = 94 - 3q - 4q^2$$

Demand:

a

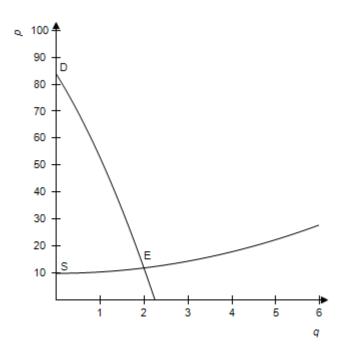


E:(4, 14)

E:(4, 18)

 $\mathbf{c}$  d

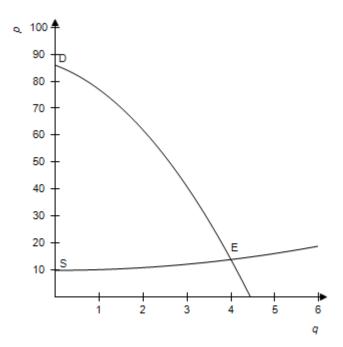
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E:(2, 12)

E:(2, 12)

e .



Dat

e:

#### **Chapter 02: Quadratic and Other Special Functions**

E:(4, 14)

ANSWER: b

 $p = \frac{1}{2}q^2 + 20$ 

53. A supply function has the equation is  $p = 86 - 6q - 3q^2$ , and the demand function is decribed by the equation

. Algebraically determine the equilibrium point for the supply and demand functions. Round your answer to two decimal places.

- a. E(3.57, -5.28)
- b. E(-5.28, 26.37)
- c.  $E(\frac{1}{2}, 86)$
- d. E(3.57, 26.37)
- e. E(3.57, 6.37)

ANSWER:

54. If the supply function for a commodity is  $p = q^2 + 8q + 16$  and the demand function is , find the equilibrium quantity and equilibrium price. Round your final answer to two decimal places.

- a. E(10.00, 65.00)
- b. E(-10.50, 106.00)
- c. E(10.00, 106.00)
- d. E(10.00, 81.00)
- e. E(10.00, 196.00)

ANSWER: e

55. If the supply and demand functions for a commodity are given by  $^{6p-q}=60$  and  $^{(p+2)q}=4830$ , respectively, find the price that will result in market equilibrium.

- a. 41
- b. 150
- c. 33
- d. 31
- e. 25

ANSWER: c

56. If the supply and demand functions for a commodity are given by p-q=10 and q(2p-10)=1200, what is the equilibrium price and what is the corresponding number of units supplied and demanded? Round your

### **Chapter 02: Quadratic and Other Special Functions**

answer to two decimal places.

ANSWER:

57. The supply function for a product is 2p-q-10=0, while the demand function for the same product is

(p+10)(q+30) = 6,300Find the market equilibrium point E(q, p). Round your final answer to two decimal places.

ANSWER:

d

а

58. The supply function for a product is  $^{2p-q-10=0}$ , while the demand function for the same product is . If a \$22 tax is placed on production of the item, then the supplier passes this tax on by adding \$22 to his selling price. Find the new equilibrium point E(q, p) for this product when the tax is passed

on. (The new supply function is given by .) Round your final answer to two decimal places.

ANSWER:

R(x) = 130x

d

 $C(x) = 1,650 + 45x + x^2$ 59. The total costs for a company are given by , and the total revenues are given by Find the break-even points.

- Break-even values are at x = 30 and x = 55 units.
  - Break-even values are at  $x = \infty$  units.

### **Chapter 02: Quadratic and Other Special Functions**

- c. Break-even values are at  $x = -\infty$  units.
- d. Break-even values are at x = 15 and x = 27.5 units.
- e. Break-even values are at x = 55 units.

ANSWER:

60. If a firm has the following cost and revenue functions, find the break-even points.

$$C(x) = 9000 + 25x + \frac{1}{2}x^{2},$$

$$R(x) = \left[255 - \frac{1}{2}x\right]x$$

- a. Break-even values are at x = 40 and x = 180 units.
- b. Break-even values are at x = 50 and x = 170 units.
- c. Break-even values are at x = 40 and x = 170 units.
- d. Break-even values are at x = 180 and x = 170 units.
- e. Break-even values are at x = 50 and x = 180 units.

ANSWER: e

 $C(x) = 15,000 + 35x + 0.1x^2$   $R(x) = 385x - 0.9x^2$  61. If a company has total costs and total revenues given by find the break-even points. Round your answers to two decimal places.

- a. Break-even values are at x = 300.00 and x = 175.00 units.
- b. Break-even values are at x = 300.00 and x = 50.00 units.
- c. Break-even values are at x = 424.26 units.
- d. Break-even values are at x = 175.00 units.
- e. Break-even values are at x = 175.00 and x = 424.26 units.

ANSWER: b

62. If total costs are C(x) = 4.400 + 1.500x and total revenues are  $R(x) = 1.650x - x^2$ , find the break-even points.

- a. Break-even values are at x = 40 and x = 20 units.
- b. Break-even values are at x = 40 and x = 110 units.
- c. Break-even values are at x = 20 and x = 110 units.
- d. Break-even values are at x = 40 and x = 90 units.

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**Chapter 02: Quadratic and Other Special Functions** 

Break-even values are at x = 20 and x = 90 units.

ANSWER:

b

 $P(x) = -13x + 0.1x^2 + 172.5$ , and that production is restricted to fewer than 75 63. Given the profit function, units, find the break-even point(s). Round your answer to two decimal places.

- Break-even value is at x = 14.00 units. a.
- Break-even value is at x = 13.37 units. b.
- Break-even value is at x = 75.00 units. c.
- Break-even value is at x = 115.00 units. d.
- Break-even value is at x = 15.00 units.

ANSWER:

е

 $R(x) = 360x - 0.8x^2$ 

. Round your answer to the nearest 64. Find the maximum revenue for the revenue function cent.

- \$40,500.00 a.
- \$121,500.00 b.
- \$30,375.00 c.
- d. \$111,375.00
- e. \$122,500.00

ANSWER:

а

65. If, in a monopoly market, the demand for a product is p = 180 - 0.75x, and the revenue function is R = px, where x is the number of units sold, what price will maximize revenue? Round your answer to the nearest cent.

- Price that will maximize revenue is p = \$90.00
- Price that will maximize revenue is p = \$247.50
- Price that will maximize revenue is p = \$270.00
- Price that will maximize revenue is p = \$120.00
- Price that will maximize revenue is p = \$60.00.

ANSWER:

а

 $P(x) = 120x - x^2 - 1100$ 

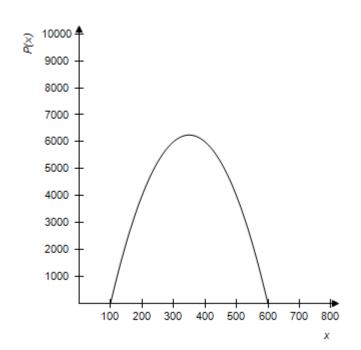
. Find the level of production that 66. The profit function for a certain commodity is yields maximum profit, and find the maximum profit.

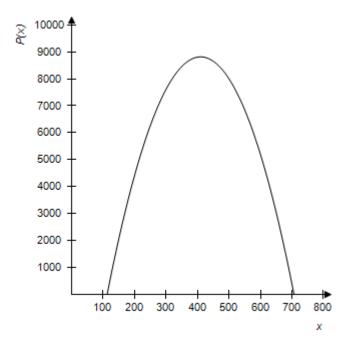
- a. Production levels of 120 yields a maximum profit of \$1,100.
- b. Production levels of 120 yields a maximum profit of \$2,500.
- c. Production levels of 60 yields a maximum profit of \$6,040.
- d. Production levels of 60 yields a maximum profit of \$3,600.
- e. Production levels of 60 yields a maximum profit of \$2,500.

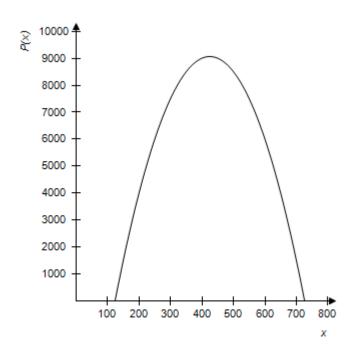
ANSWER: e

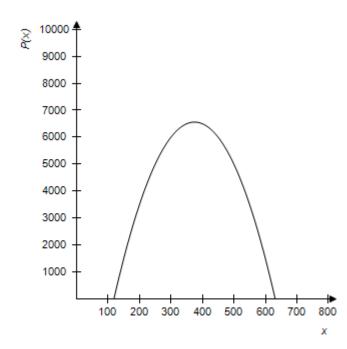
 $P(x) = 80x - 0.1x^2 - 7000$  67. Use a graphing calculator to graph the profit function

a b

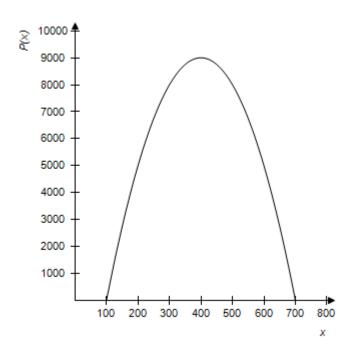








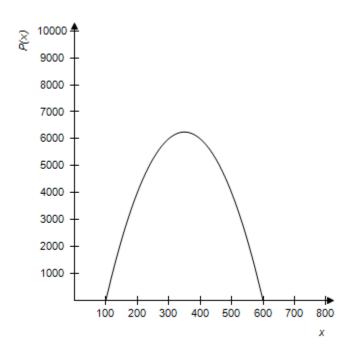
e .



ANSWER:

$$P(x) = 70x - 0.1x^2 - 6000$$

68. The graph of the profit function is given as follows. Consider the average rate of change of the profit from a to 350 where a lies to the left of 350. Does the average rate of change of the profit get closer to 0 or farther from 0 as a gets closer to 350?



closer to 0 a.

farther from 0 b.

ANSWER:

а

69. Form the profit function for the cost and revenue functions, where the total costs and total revenues are  $R(x) = 390x - 0.9x^2$ and  $C(x) = 15,100 + 35x + 0.1x^2$ given by

a. 
$$P(x) = -0.8x^2 + 355x + 15,100$$

b. 
$$P(x) = -x^2 + 355x - 15,100$$

c. 
$$P(x) = -x^2 + 425x - 15.100$$

d. 
$$P(x) = -x^2 + 355x + 15,100$$

e. 
$$P(x) = -0.8x^2 + 425x - 15,100$$

ANSWER: b

70. Suppose a company has fixed costs of \$26,000 and variable costs of  $\frac{2}{5}x + 222$  dollars per unit, where x is the  $1300 - \frac{3}{5}x$ 

total number of units produced. Suppose further that the selling price of its product is unit. Find the break-even points. Round your answer to the nearest cent.

- a. Break-even values are at x = 1,053.32 and x = 24.68.
- b. Break-even values are at x = 1,078.00 and x = 0.
- c. Break-even values are at x = 21.16 and x = 1,228.84
- d. Break-even values are at x = 1.053.32 and x = 26.000.00
- e. Break-even values are at x = 555.00 and x = 2,166.67.

ANSWER:

71. Suppose a company has fixed costs of \$27,000 and variable costs of  $\frac{2}{5}x + 222$  dollars per unit, where x is  $\frac{1,275 - \frac{3}{5}x}{5}$ 

the total number of units produced. Suppose further that the selling price of its product is dollars per unit. Find the maximum revenue. Round your answer to the nearest cent.

- a. Maximum revenue is \$1,026.70.
- b. Maximum revenue is \$27,000.00.
- c. Maximum revenue is \$26,862.50.
- d. Maximum revenue is \$677,343.75.
- e. Maximum revenue is \$612.50.

ANSWER: d

72. Assume that sales revenues for Continental Divide Mining can be described by

 $R(t) = -0.051t^2 + 0.876t + 0.179$ , where t is the number of years past 1992. Use the function to determine the year in which maximum revenue occurs.

- a. Maximum revenue occurred during 2001.
- b. Maximum revenue occurred during 1992.
- c. Maximum revenue occurred during 2000.
- d. Maximum revenue occurred during 2009.
- e. Maximum revenue occurred during 1991.

ANSWER:

73. Assume that sales revenues, in millions, for Continental Divide Mining can be described by  $R(t) = -0.041t^2 + 0.776t + 0.179$ 

 $R(t) = -0.041t^2 + 0.776t + 0.179$ 

, where t is the number of years past 1992. Use the function to find the maximum revenue. Round your answers to three decimal places.

- a. Maximum revenue is \$9.463 million.
- b. Maximum revenue is \$5.971 million.
- c. Maximum revenue is \$3.672 million.
- d. Maximum revenue is \$3.851 million.
- e. Maximum revenue is \$16.986 million.

ANSWER:

74. Assume that costs and expenses for Continental Divide Mining can be described by

$$C(t) = -0.012t^2 + 0.561t + 0.731$$
 and the sales revenue can be described by

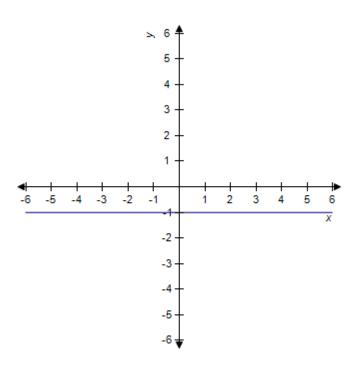
, where t is the number of years since the beginning of 1992. Find the year in which maximum profit occurs.

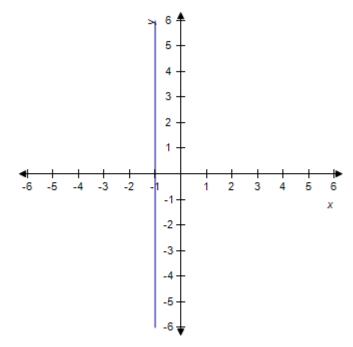
- a. 2014
- b. 1993
- c. 2003
- d. 2004
- e. 1994

ANSWER: c

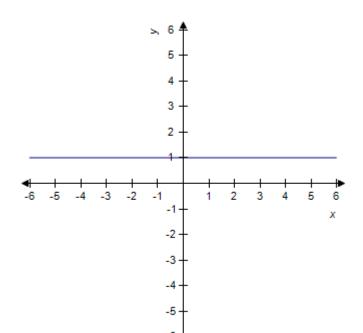
75. Sketch the graph of the function f(x) = 1.

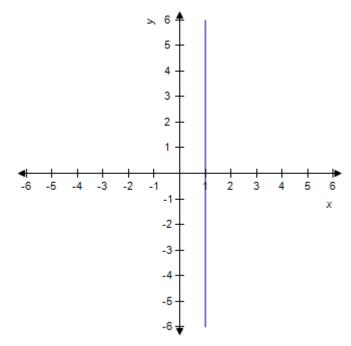
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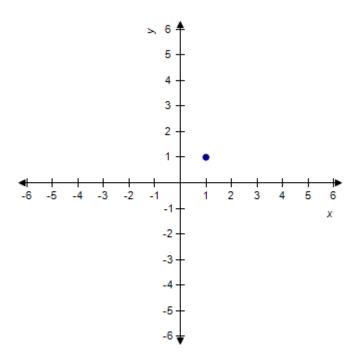




c d



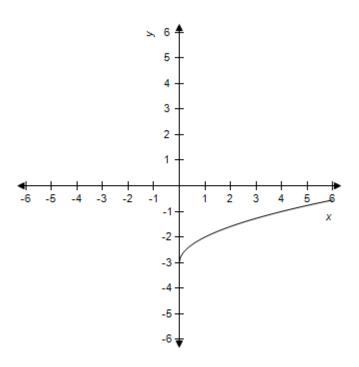


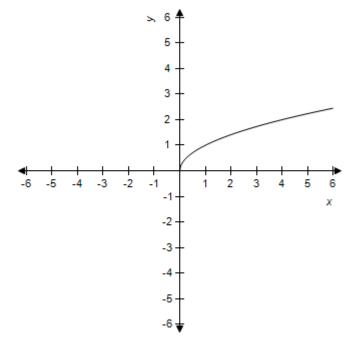


ANSWER:

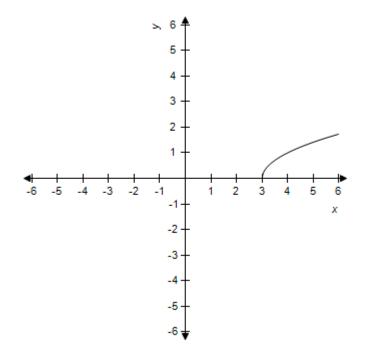
76. Sketch the graph of the function  $y = \sqrt{x} - 3$ 

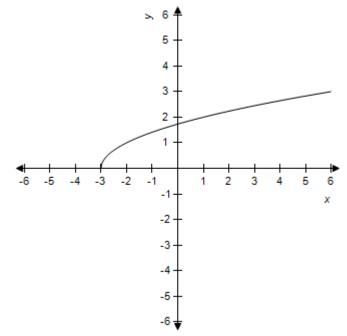
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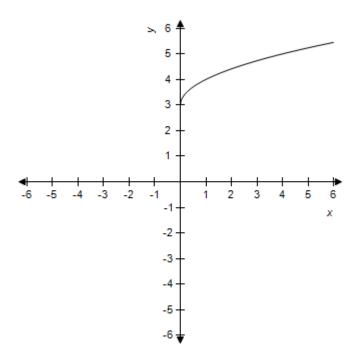




c d





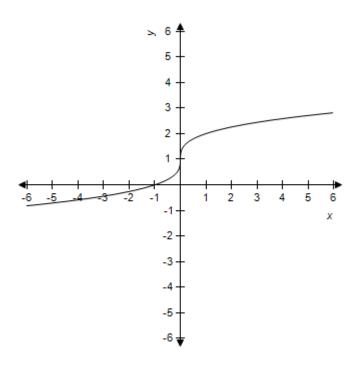


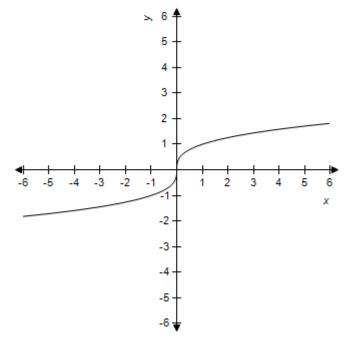
ANSWER:

77. Sketch the graph of the function  $y = \sqrt[3]{x} - 1$ .

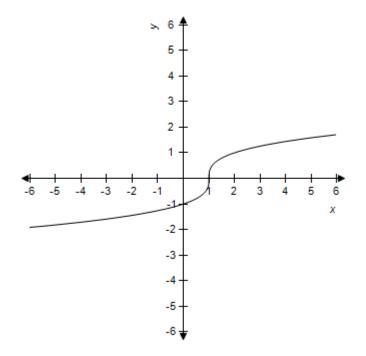
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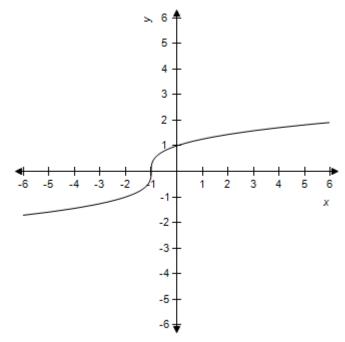
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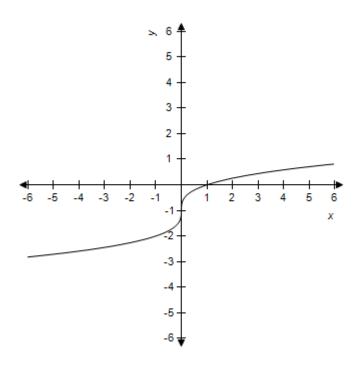




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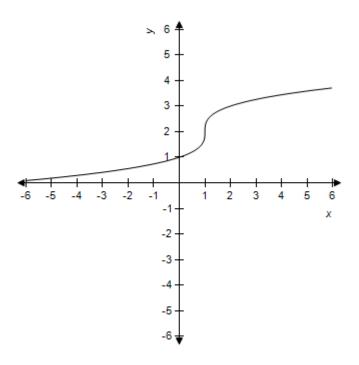


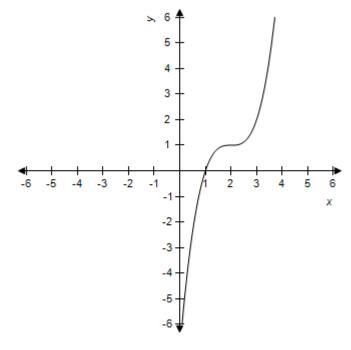
ANSWER: e

78. Sketch the graph of the function below.

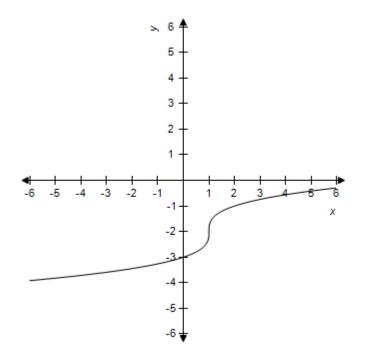
$$y = (x-2)^3 + 1$$

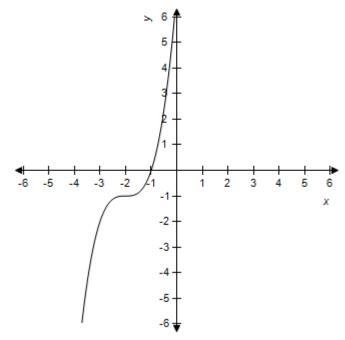
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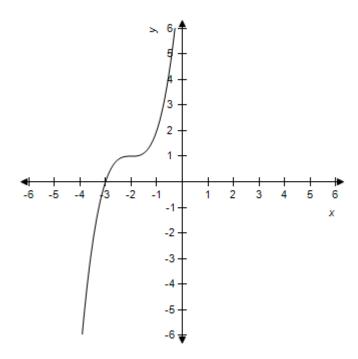


c d





e

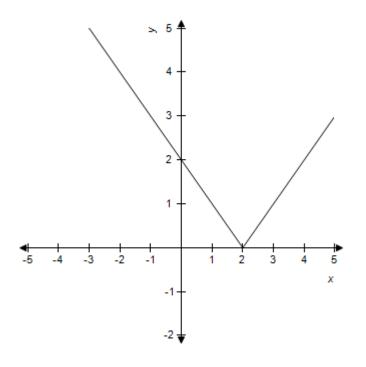


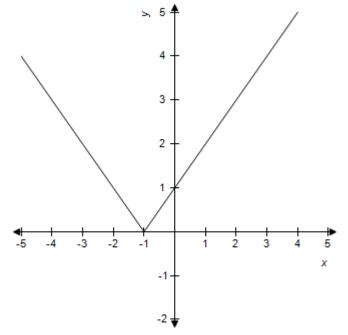
ANSWER: b

79. Sketch the graph of the function y = |x+2|.

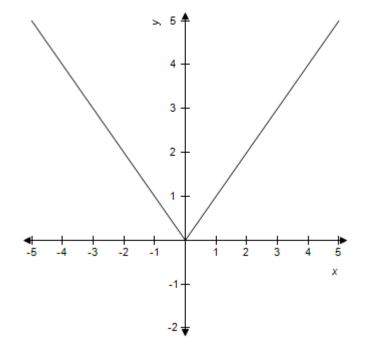
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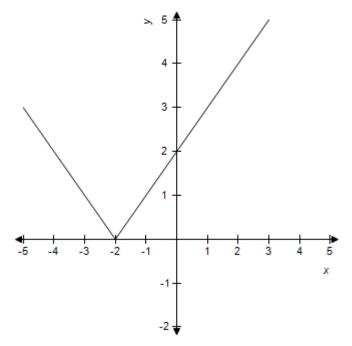
**Chapter 02: Quadratic and Other Special Functions** 

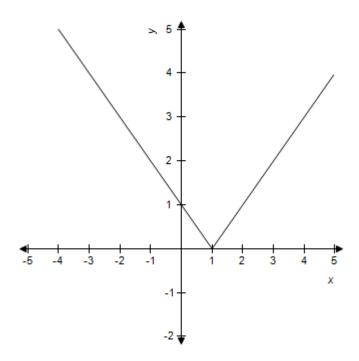




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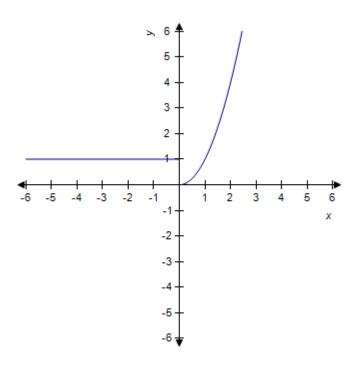


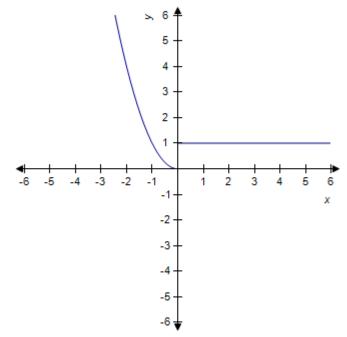
ANSWER:

 $f(x) = \begin{cases} x^2 & \text{if } x < 0 \\ 1 & \text{if } x > 0 \end{cases}$ 

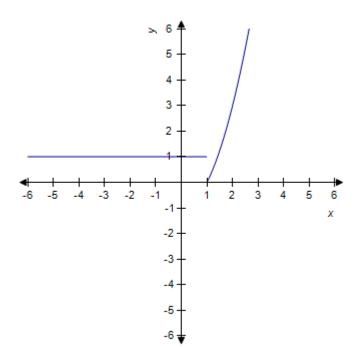
80. Sketch the graph of the function

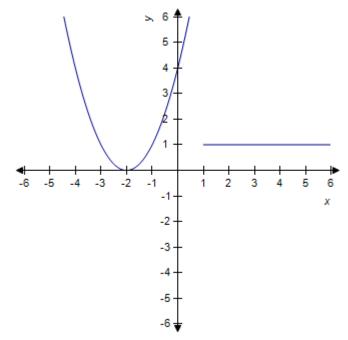
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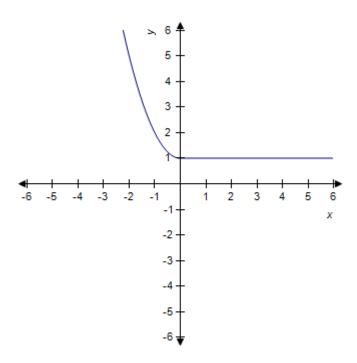


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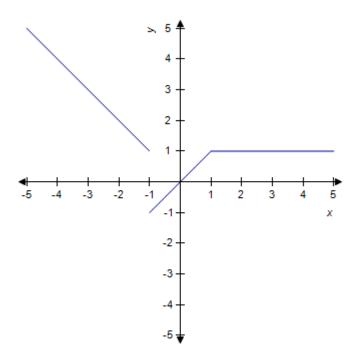


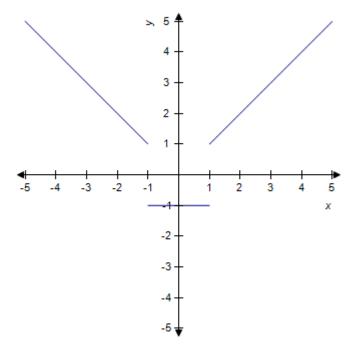
ANSWER: b

$$f(x) = \begin{cases} -1, & \text{if } x \le -1 \\ x, & \text{if } -1 < x < 1 \\ -x, & \text{if } x \ge 1 \end{cases}$$

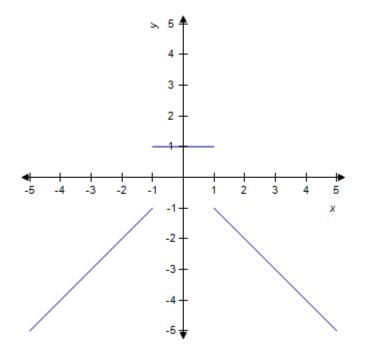
81. Sketch the graph of the function

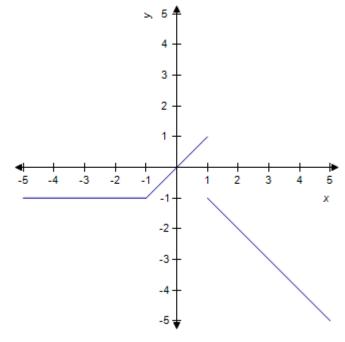
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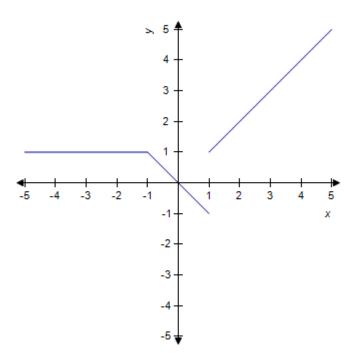


 $\mathbf{c}$  d





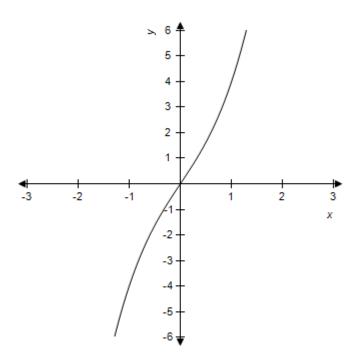
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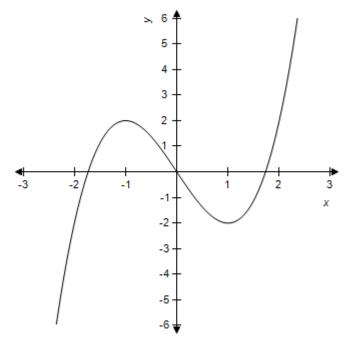


ANSWER:

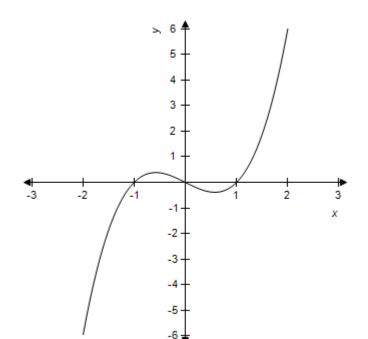
82. By recognizing shapes and features of polynomial functions, sketch the graph of the function  $y = x^3 - x$ . Use a graphing utility to confirm your graph.

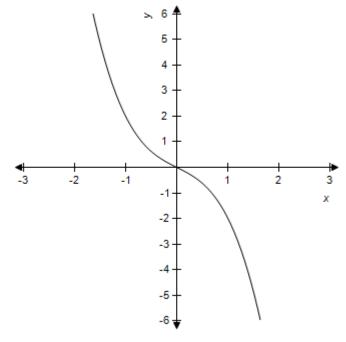
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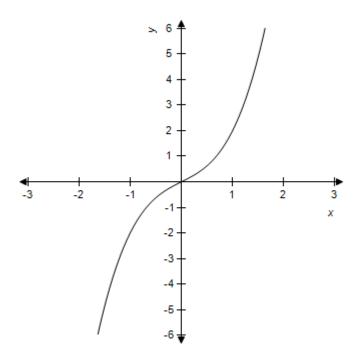


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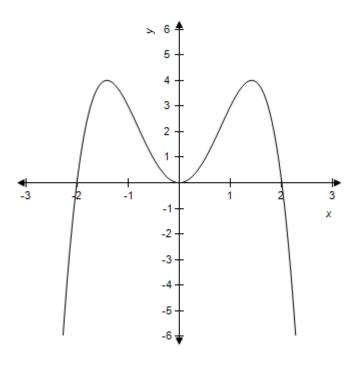
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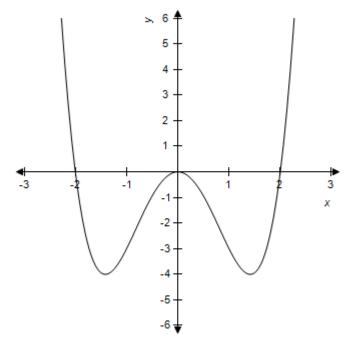


ANSWER: c

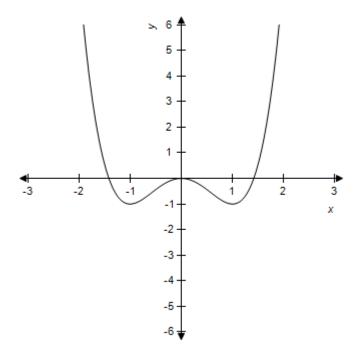
83. By recognizing shapes and features of polynomial functions, sketch the graph of the function Use a graphing utility to confirm your graph.

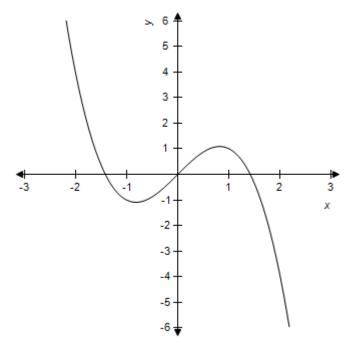
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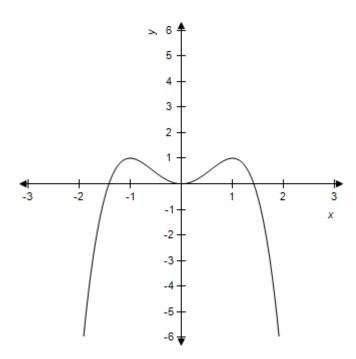




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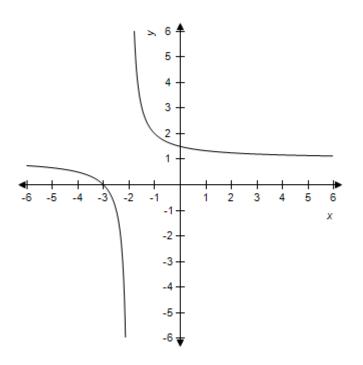


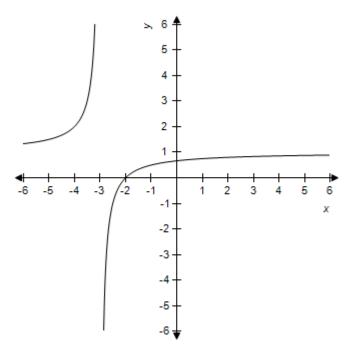
ANSWER: e

 $y = \frac{x+3}{x+2}$ 

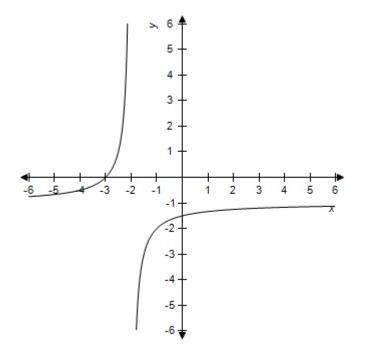
84. By recognizing shapes and features of rational functions, sketch the graph of the function x+2. Use a graphing utility to confirm your graph.

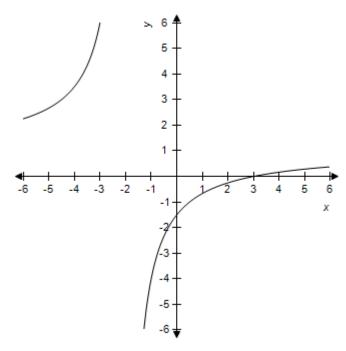
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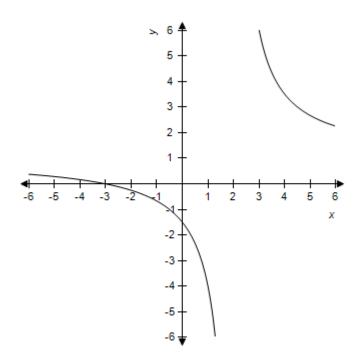




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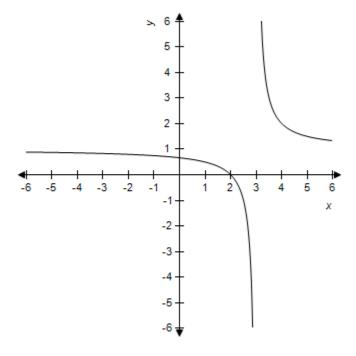






ANSWER:

85. Find the rational function whose graph is given.



### **Chapter 02: Quadratic and Other Special Functions**

a. 
$$y = \frac{x-3}{x+2}$$

b. 
$$y = \frac{x+3}{x-2}$$

$$y = \frac{x+2}{x-3}$$

$$y = \frac{x-2}{x-3}$$

$$y = \frac{x+2}{x+3}$$

ANSWER:

86. If  $f(x) = 8x^{5/2}$ , find f(100) and f(0.36). Round your answers to two decimal places.

a. 
$$f(100) = 800,000.00 \text{ and } f(0.36) = 0.62$$

b. 
$$f(100) = 800,512.00$$
 and  $f(0.36) = 0.42$ 

c. 
$$f(100) = 799,980.00$$
 and  $f(0.36) = 1.02$ 

d. 
$$f(100) = 799,750.00$$
 and  $f(0.36) = 0.12$ 

e. 
$$f(100) = 800,080.00$$
 and  $f(0.36) = 1.36$ 

ANSWER: a

If  $k(x) = \begin{cases} -4 & \text{if } x < 0 \\ x+2 & \text{if } 0 \le x < 1 \text{, find } k(-2), k(0), \text{ and } k(3). \\ 6-x & \text{if } x \ge 1 \end{cases}$ 

a. 
$$k(-2) = -2$$
,  $k(0) = -4$ ,  $k(3) = 3$ 

b. 
$$k(-2) = -4$$
,  $k(0) = -4$ ,  $k(3) = -9$ 

c. 
$$k(-2) = -4$$
,  $k(0) = 2$ ,  $k(3) = 3$ 

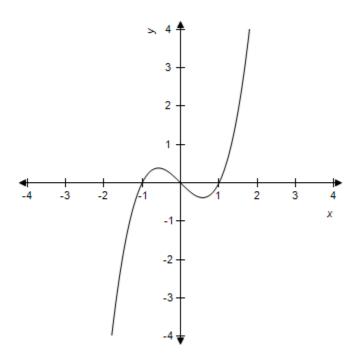
d. 
$$k(-2) = -2, k(0) = 2, k(3) = 6$$

e. 
$$k(-2) = -2$$
,  $k(0) = 2$ ,  $k(3) = 5$ 

ANSWER: c

88. Determine whether the given graph is the graph of a polynomial function, a rational function (but not a polynomial), or a piecewise defined function. Use the graph to estimate the turning points. Round your answers to two decimal places.

## **Chapter 02: Quadratic and Other Special Functions**



a. polynomial function turning points: x = 0.58 and x = -0.58

b. rational function turning points: x = 0.58 and x = -0.58

c. polynomial function turning points: x = -1.00, x = 0.00, and x = 1.00

d. rational function turning points: x = -1.00, x = 0.00, and x = 1.00

e. piecewise function turning points: x = 0.38 and x = -0.38

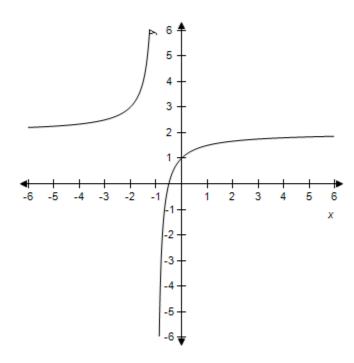
ANSWER:

а

89. Determine whether the given graph is the graph of a polynomial function, a rational function (but not a polynomial), or a piecewise defined function. Use the graph to estimate the turning points and any asymptotes.

Name Class

## **Chapter 02: Quadratic and Other Special Functions**



- a. polynomial function x = -0.5 turning points: x = -1 vertical asymptote: y = 2
- b. rational function turning points: none vertical asymptote: x=-1horizontal asymptote: y=2
- c. rational function turning points: none vertical asymptote: x = 2horizontal asymptote: y = -1
- d. piecewise function turning points: x = -0.5vertical asymptote: x = 2horizontal asymptote: y = -1
- e. polynomial function turning points: none vertical asymptote: x = 2horizontal asymptote: y = -1

Dat

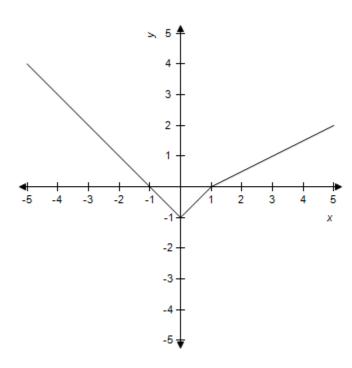
e:

## **Chapter 02: Quadratic and Other Special Functions**

ANSWER:

b

90. Determine whether the given graph is the graph of a polynomial function, a rational function (but not a polynomial), or a piecewise defined function. Use the graph to estimate the turning points.



- a. piecewise function turning points: x = -1 and x = 1
- b. polynomial function turning points: x = -1 and x = 1
- c. rational function turning points: x = -1
- d. polynomial function turning points: x = 0
- e. piecewise function turning points: x = 0

ANSWER:

е

91. An open-top box is constructed from a square piece of cardboard with sides of length 10 ft. The volume of  $V = x(10-2x)^2$  ft<sup>3</sup> such a box is given by , where x is the height of the box. Find the volume of the box if its height is 2 ft.

### **Chapter 02: Quadratic and Other Special Functions**

a. 
$$70.5 \text{ ft}^3$$

b. 
$$71.5 \text{ ft}^3$$

c. 
$$72 \text{ ft}^3$$

$$d.$$
 74 ft<sup>3</sup>

e. 
$$76.5 \text{ ft}^3$$

ANSWER:

- 92. The amount of money invested in a certain mutual funds, measured in millions of dollars, for the years 1995  $f(x) = 98.25x^{0.95}$  to 1999 was found to be modeled by million dollars, where x is the number of years past 1990. Will the graph of this function bend upward or will it bend downward? How much money is predicted to be in the fund in the year 2009? Round your answer to two decimal places.
  - a. the function's graph bends upward; the function predicts 134,947.08 million dollars in 2009
  - b. the function's graph bends downward; the function predicts 134,947.08 million dollars in 2009
  - c. the function's graph bends upward; the function predicts 68,279.14 million dollars in 2009
  - d. the function's graph bends downward; the function predicts 1,611.20 million dollars in 2009
- e. the function's graph bends upward; the function predicts 1,611.20 million dollars in 2009 ANSWER:
- 93. Suppose that the cost C (in dollars) of removing p percent of the particulate pollution from the smokestacks  $C(p) = \frac{7.450p}{100-p}$  of an industrial plant is estimated by . What is the domain of this function? What will it cost to remove 99.0% of the particulate pollution? Round your answer to the nearest cent.
  - a. domain:  $0 \le p < 99.0$

b. domain: 
$$0 \le p < 100$$
 cost: \$737,550.00

c. domain: all 
$$p$$
 except  $p = 100$  cost: \$737,550.00

d. domain: 
$$0 \le p < 100$$

e. domain: all 
$$p$$
 except  $p = 100$  cost: \$74.49

ANSWER: b

$$f(x) = \begin{cases} 36.00 & \text{if } 0 \le x \le 20 \\ 36.00 + 0.4(x - 20) & \text{if } x > 20 \end{cases}$$

94. The monthly charge for water in a small town is given by , where x is water usage in hundreds of gallons and f(x) is cost in dollars. Find the monthly charge for 1900 gallons and

#### **Chapter 02: Quadratic and Other Special Functions**

for 2600 gallons. Round your answers to the nearest cent.

- a. charge for 1900 gallons is \$36.00 charge for 2600 gallons is \$38.40
- b. charge for 1900 gallons is \$788.00 charge for 2600 gallons is \$1068.00
- c. charge for 1900 gallons is \$36.00 charge for 2600 gallons is \$46.40
- d. charge for 1900 gallons is \$38.40 charge for 2600 gallons is \$46.40
- e. charge for 1900 gallons is \$36.00 charge for 2600 gallons is \$74.40

ANSWER:

а

95. A shipping company's charges for delivery of a package is a function of the package's weight. The following table describes the company's shipping rates.

Weight Increment	Rate
First pound or fraction of a pound	\$0.45
Each additional pound or fraction of a pound	\$0.85

Convert this table to a piecewise defined function that represents shipping costs for packages weighing between 0 and 4 pounds using x as the weight in pounds and C as the cost in dollars. Find the postage for a 0.75-pound package. Round your answer to the nearest cent.

a. 
$$C(x) = \begin{cases} 0.45 & \text{if } 0 < x \le 1 \\ 0.90 & \text{if } 1 < x \le 2 \\ 1.35 & \text{if } 2 < x \le 3 \\ 1.80 & \text{if } 3 < x \le 4 \end{cases}$$

cost for a 0.75 lb package: \$0.45

b. 
$$C(x) = \begin{cases} 0.45 & \text{if } 0 < x \le 1 \\ 0.85 & \text{if } 1 < x \le 2 \\ 1.70 & \text{if } 2 < x \le 3 \\ 2.55 & \text{if } 3 < x \le 4 \end{cases}$$

cost for a 0.75 lb package: \$0.23

c. 
$$C(x) = \begin{cases} 0.45 & \text{if } 0 < x \le 1 \\ 0.45 + 0.85x & \text{if } 1 < x \le 4 \end{cases}$$
  
cost for a 0.75 lb package: \$1.09

## **Chapter 02: Quadratic and Other Special Functions**

d. 
$$C(x) = \begin{cases} 0.45 & \text{if } 0 < x \le 1 \\ 1.30 & \text{if } 1 < x \le 2 \\ 2.15 & \text{if } 2 < x \le 3 \\ 3.00 & \text{if } 3 < x \le 4 \end{cases}$$

cost for a 0.75 lb package: \$0.45

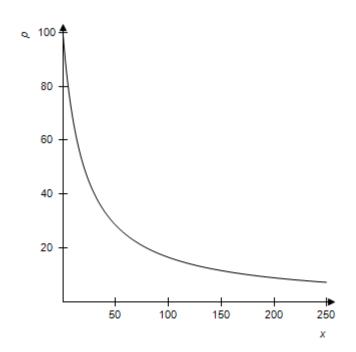
e. 
$$C(x) = \begin{cases} 0.45 & \text{if } 0 < x \le 1 \\ 0.45 + 0.85x & \text{if } 1 < x \le 2 \\ 0.45 + 1.70x & \text{if } 2 < x \le 3 \\ 0.45 + 2.55x & \text{if } 3 < x \le 4 \end{cases}$$

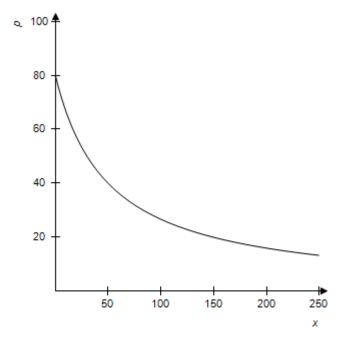
cost for a 0.75 lb package: \$0.45

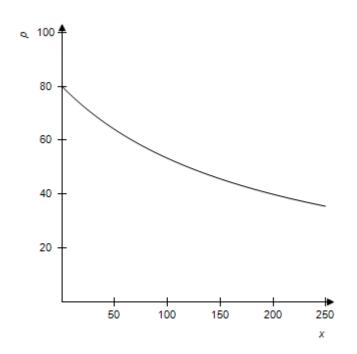
ANSWER:

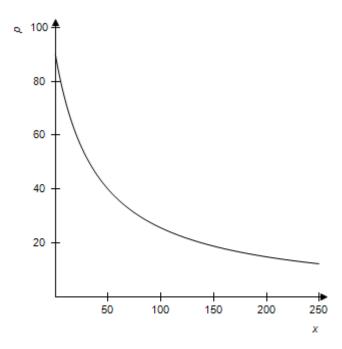
 $p = \frac{800}{10 + 0.05x}$ 96. The demand function for a product is given by price in dollars. Graph this demand function for  $0 \le x \le 250$ , with x on the horizontal axis.

a b

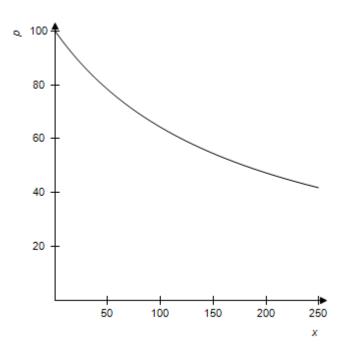








e



ANSWER:

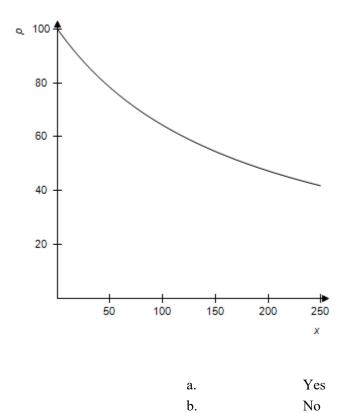
С

900

e:

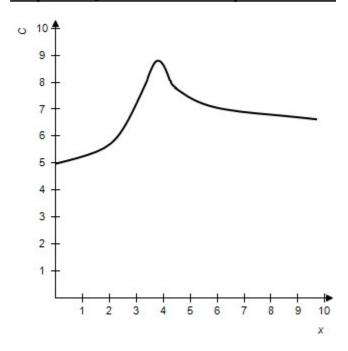
## **Chapter 02: Quadratic and Other Special Functions**

97. The demand function for a product is given by  $p = \frac{1}{9 + 0.05x}$ , where x is the number of units and p is the price in dollars. The graph of this demand function for  $0 \le x \le 250$ , with x on the horizontal axis is given below. Does the demand function ever reach 0?



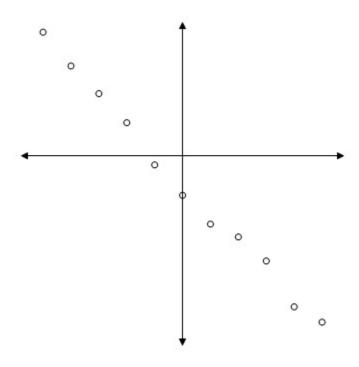
ANSWER: No

98. The given graph shows the cost *C*, in thousands of dollars, of a production run for a product when *x* machines are used. Estimate the company's fixed cost of production to the nearest thousand dollars, and determine the number of machines that will result in maximum cost for the company.



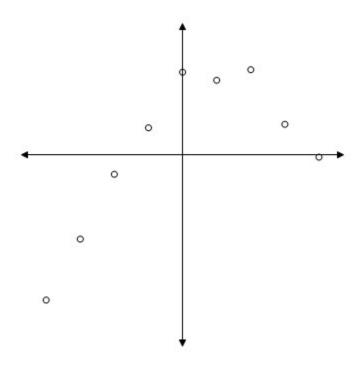
- a. fixed production cost: \$6,000 maximum cost when 4 machines used
- b. fixed production cost: \$9,000 maximum cost when 4 machines used
- c. fixed production cost: \$5,000 maximum cost when 4 machines used
- d. fixed production cost: \$6,000 maximum cost when 6 machines used
- e. fixed production cost: \$5,000 maximum cost when 6 machines used

ANSWER: c



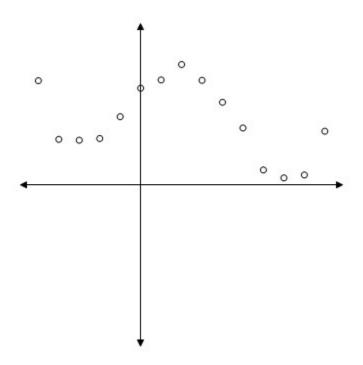
- a. linear
- b. power
- c. quadratic
- d. cubic
- e. quartic

ANSWER:



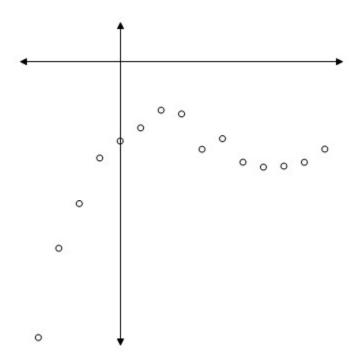
- a. linear
- b. power
- c. quadratic
- d. cubic
- e. quartic

ANSWER: c



- a. linear
- b. power
- c. quadratic
- d. cubic
- e. quartic

ANSWER: e



- a. linear
- b. power
- c. quadratic
- d. cubic
- e. quartic

ANSWER:

103. Find the equation of the linear function that is the best fit for the given data. Round your final values to two decimal places.

X	y
0	3.5
1	5.6
2	7.1
3	9.6
4	11.5

- a. y = 2.71x + 4.92
- b. y = 2.08x + 2.81
- c. y = 2.97x + 0.94
- d. y = 1.63x + 7.03

## **Chapter 02: Quadratic and Other Special Functions**

e. 
$$y = 1.00x + 5.99$$

ANSWER: b

104. Graph the linear function that models the data given in the table below.

$$x$$
  $-1$   $y$   $-1.5$ 

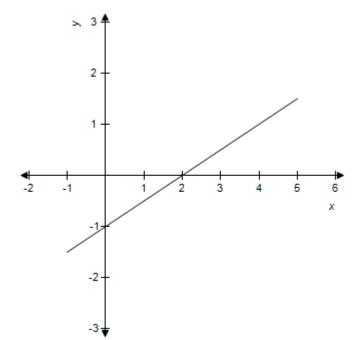
$$0 \\ -1.0$$

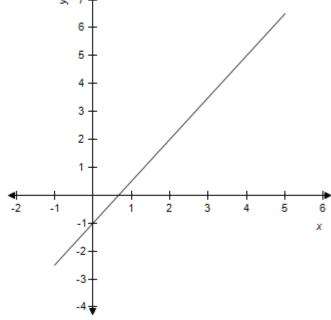
a



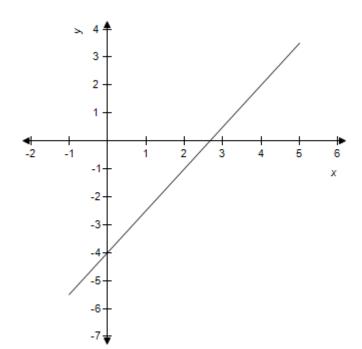
b

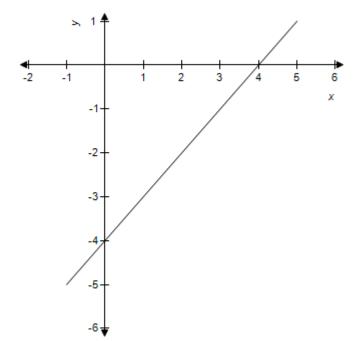




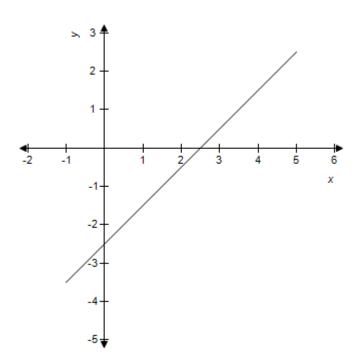


c





e



ANSWER: a

# **Chapter 02: Quadratic and Other Special Functions**

two decimal places.

x	у
-2	-7.03
-1	-2.25
0	0.31
1	0.65
2	-0.43
3	-3.63
4	-9.15

a. 
$$y = -0.71x^2 + 3.20x - 0.46$$

b. 
$$y = -0.61x^2 + 2.13x - 1.38$$

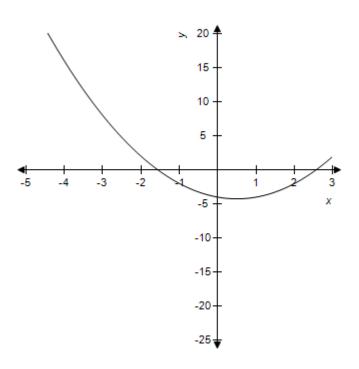
c. 
$$y = -0.34x^2 + 2.40x - 0.23$$

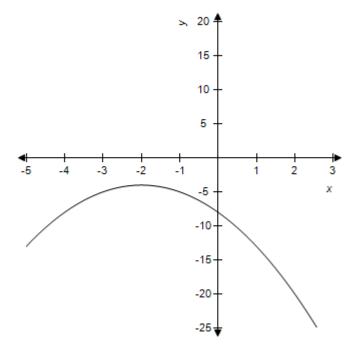
d. 
$$y = -1.14x^2 + 0.80x - 0.52$$

e. 
$$y = -0.96x^2 + 1.60x - 0.69$$

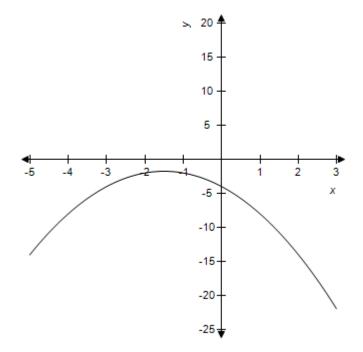
ANSWER: e

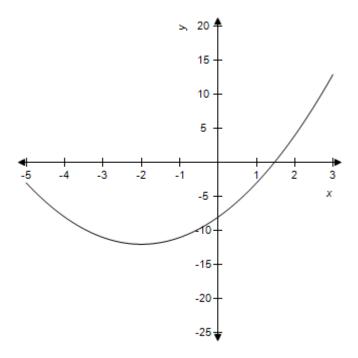
106. Graph the quadratic function that models the data given in the table below.

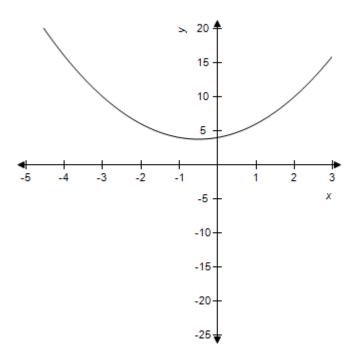




c d







ANSWER: b

107. Find the equation of the cubic function that is the best fit for the given data. Round your final values to two decimal places.

x	y
-4	-127.9
-3	-58.1
-2	-19.1
-1	-1.8
0	3.2
1	4.3
2	11.0

a. 
$$y = 1.84x^3 - 2.09x^2 + 1.51x + 2.53$$

b. 
$$y = 1.53x^3 - 1.74x^2 + 1.26x + 2.41$$

c. 
$$y = 1.22x^3 - 1.91x^2 + 2.02x + 2.29$$

d. 
$$y = 1.68x^3 - 1.39x^2 + 0.76x + 2.46$$

e. 
$$y = 1.38x^3 - 1.57x^2 + 1.89x + 2.36$$

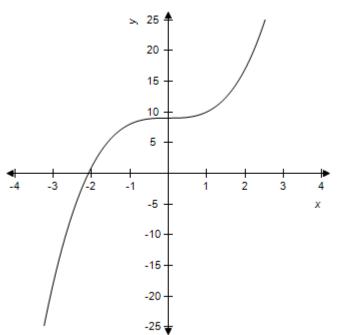
## **Chapter 02: Quadratic and Other Special Functions**

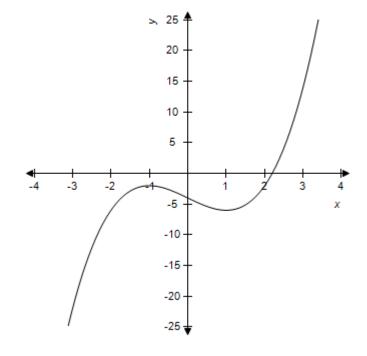
108. Graph the cubic function that models the data given in the table below.

-3  $\boldsymbol{x}$ 14 у

a

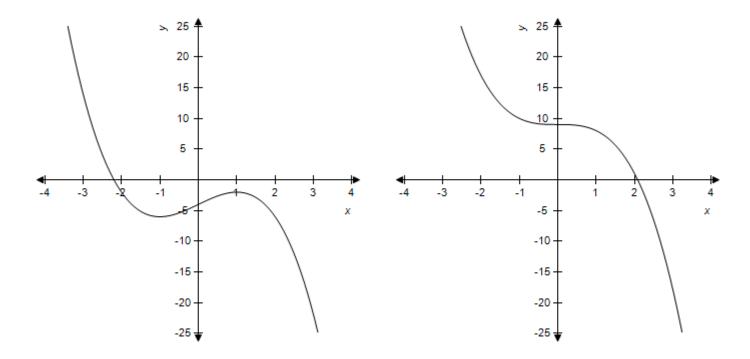
b



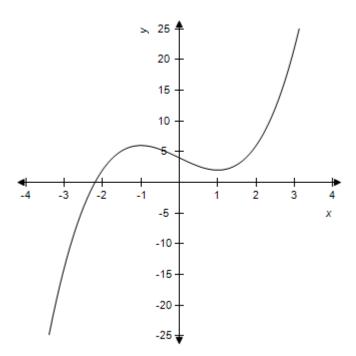


c

d



e



ANSWER:

С

109. Find the equation of the quartic function that is the best fit for the given data. Round your final values to Page 70

## **Chapter 02: Quadratic and Other Special Functions**

two decimal places.

X	y
1	4.2
2	-4.3
3	-34.1
4	-97.7
5	-210.0
6	-385.9
7	-642.8

a. 
$$y = -0.05x^4 - 1.61x^3 + 0.44x^2 + 2.21x + 3.20$$

b. 
$$y = -2.15x^4 + 1.30x^3 + 2.25x^2 + 5.00x + 2.16$$

c. 
$$y = -1.76x^4 + 0.86x^3 + 1.21x^2 + 2.14x + 0.72$$

d. 
$$y = -2.93x^4 + 1.40x^3 + 2.60x^2 + 4.64x + 1.87$$

e. 
$$y = -1.37x^4 + 0.97x^3 + 1.56x^2 + 2.50x + 1.01$$

ANSWER:

а

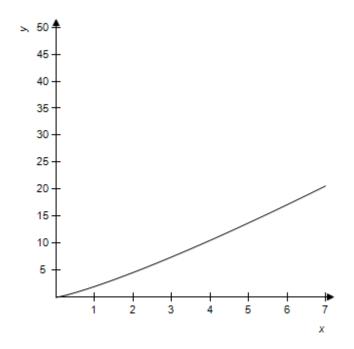
110. Graph the power function that models the data given in the table below.

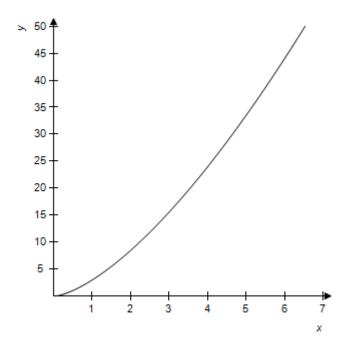
 $\begin{array}{ccc} x & 1 \\ y & 3.0000 \end{array}$ 

2 8.4853 3 15.5885 4 24.0000 5 33.5410 6 44.0908

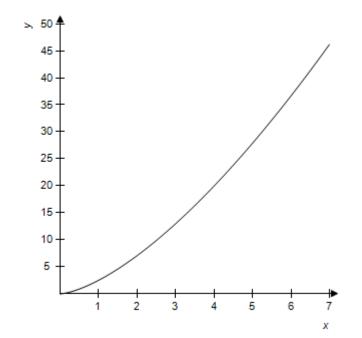
a

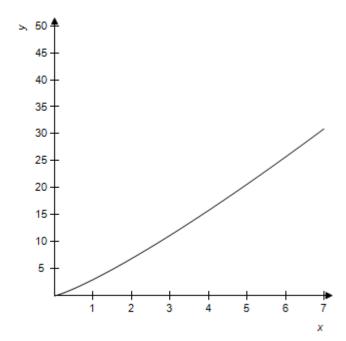
b

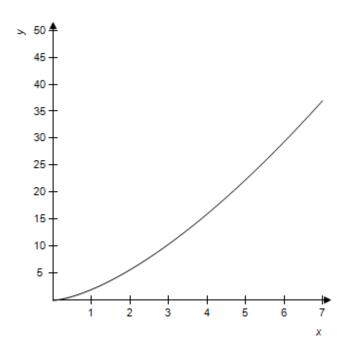




c d







ANSWER: b

111. Determine what type of function best models the data given below, and find the equation that is the best fit for the data. Round your final values to four decimal places.

x	y
0	1.50
1	7.33
2	13.41
3	19.32
4	25.33
5	31.44
6	37.37

a. linear: 
$$y = 5.9911x + 5.9911$$

b. 
$$y = 0.0101x^2 + 5.9304x + 1.4633$$

c. 
$$y = 8.4069x^{0.7838}$$

d. 
$$y = -0.0044x^3 + 0.0501x^2 + 5.8415x + 1.4898$$

e. 
$$y = -0.0005x^4 + 0.0010x^3 + 0.0299x^2 + 5.8645x + 1.4874$$

#### **Chapter 02: Quadratic and Other Special Functions**

ANSWER:

112. Determine what type of function best models the data given below, and find the equation that is the best fit for the data. Round your final values to four decimal places.

x	y
0	7.8
1	40.1
2	59.7
3	66.3
4	59.7
5	40.4
6	7.7

a. 
$$\lim_{x \to 1} y = 0.0107x + 40.2107$$

b. 
$$y = -6.4988x^2 + 39.0036x + 7.7167$$

c. 
$$y = 25.4285x^{0.2823}$$

d. 
$$y = -0.0111x^3 - 6.3988x^2 + 38.7813x + 7.7833$$

e. 
$$y = 0.0008x^4 - 0.0202x^3 - 6.3652x^2 + 38.7430x + 7.7872$$
 quartic;

ANSWER: b

113. The table shows the average earnings of year-round, full-time workers by gender and educational attainment in a certain country. Let *x* represent earnings for males and *y* represent earnings for females, and find a linear model that expresses women's annual earnings as a function of men's. Interpret the slope of the linear model. Round your final values to three decimal places.

Educational Attainment	Average Annual Earnings	
	Males	Females
Less than 9th grade	\$12,035	\$10,745
Some high school	\$13,010	\$11,470
High school graduate	\$18,085	\$16,200
Some college	\$20,135	\$13,120
Associate's degree	\$26,295	\$22,210
Bachelor's degree or more	\$45,070	\$35,135

a. y = 1.292x-1,008.175

slope: females earn \$1,292 for each \$1,000 males earn

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$$b. y = 1.292x - 1.008.175$$

slope: the average difference in yearly male and female earnings is \$1,292

$$v = 0.748x + 1.353.436$$

slope: females earn \$748 for each \$1,000 males earn

$$d_{x} v = 0.748x + 1,353.436$$

slope: the average difference in yearly male and female earnings is \$748

$$v = 0.748x + 1.353.436$$

slope: the average of male and female earnings increases by an average of \$748 for each level of educational attainment

ANSWER: c

114. The table gives the median household income (in 2005 year) for two cities in various years. Let *x* represent the median household income for citizens of city A and *y* represent the corresponding median household income for citizens of city B. Find a linear model that expresses the median household income for citizens in city B as a function of the median household income for citizens of city B. Interpret the slope of the linear model. Round numerical values in your answer to three decimal places.

# Median Household Income (2005 year)

Year	City A	City B
1985	\$21,900	\$19,600
1990	\$23,800	\$21,500
1995	\$25,700	\$24,500
2000	\$27,400	\$27,200
2005	\$31,000	\$31,100

a. 
$$y = 0.761x + 7.100.386$$

slope: median household income is growing at the same rate for city A as it is for city B.

v = 0.761x + 7.100.386

slope: median household income is growing at the same rate for city A as it is for city B.

c. y = 0.761x - 7.100.386

slope: median household income is growing at the same rate for city A as it is for city B.

y = 1.305x - 9.088.705

slope: median household income is growing faster for city A than it is for city B.

e. y = 1.305x - 9.088.705

slope: median household income is growing slower for city A than it is for city B.

ANSWER:

d

115. Suppose the IQ scores (rounded to the nearest 10) for a group of people are summarized in the table below. Find the quadratic function that best fits the data, using x as the IQ score and y as the number of people in the group with that IQ score. Use a graphing utility to estimate the IQ score of the maximum number of individuals according to the model. Round your final answer to 2 decimal places.

IQ Score	<b>Number of People</b>
70	53
80	78
90	91
100	87
110	75
120	47
130	17

a. 
$$y = -0.06x^2 + 11.15x - 436.43$$

The model predicts that the maximum number of people have an IQ score of approximately 94.

b. 
$$y = -0.06x^2 + 11.15x - 436.43$$

The model predicts that the maximum number of people have an IQ score of approximately 90.

c. 
$$y = -0.07x^2 + 10.82x - 458.25$$

The model predicts that the maximum number of people have an IQ score of approximately 90.

d. 
$$y = -0.07x^2 + 10.82x - 458.25$$

The model predicts that the maximum number of people have an IQ score of approximately 94.

e. 
$$v = -0.07x^2 + 12.26x - 458.25$$

The model predicts that the maximum number of people have an IQ score of approximately 90. *ANSWER:* 

116. Suppose that the following table gives the number of near-collisions on the runways of the nation's airports. With x=0 representing 1990, find a quadratic function that models the data in the chart. Round numerical values in your answer to four decimal places. Depending on the technology you use, your answer may be slightly different than the correct answer shown.

Runway near-hits in USA
300
312
320
325
340
365
378
420
455
481

### **Chapter 02: Quadratic and Other Special Functions**

2000

498

a. 
$$v = 1.5979x^2 + 4.9210x + 300.7413$$

b. 
$$y = 1.5979x^2 - 4.9210x + 300.7413$$

c. 
$$v = 3.8991x^2 + 4.9210x + 300.7427$$

d. 
$$v = 2.8335x^2 + 10.0440x + 303.8647$$

e. 
$$y = 2.8335x^2 - 10.0440x + 303.8647$$

ANSWER:

а

117. The table that follows gives the population of a city. Find the power function that best fits the data, with *x* equal to the number of years past 1950. According to the model, will the city's population be greater than 1,400 by the year 2010? Round your final answer to three decimal places.

Year	Population
1960	648
1970	890
1980	1,110
1990	1,153
2000	1,176

a. 
$$y = 5.613x^{0.389}$$

The model predicts that the population will not be greater than 1,400.

b. 
$$y = 273.895x^{0.389}$$

The model predicts that the population will not be greater than 1,400.

c. 
$$y = 5.613x^{0.611}$$

The model predicts that the population will be greater than 1,400.

d. 
$$y = 273.895x^{0.611}$$

The model predicts that the population will be greater than 1,400.

e. 
$$v = 648x^{0.5}$$

The model predicts that the population will not be greater than 1,400.

ANSWER:

b

118. Suppose that the following table shows the number of millions of people in the United States who lived below the poverty level for selected years. Find a cubic model that approximately fits the data, using *x* as the number of years after 1960. Round numerical values in your answer to four decimal places. Depending on the technology you use, your answer may be slightly different than the correct answer shown.

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	Poverty Level (millions)
1960	87.3
1970	28.4
1975	25.6
1980	43.2
1989	97.6
1990	103.9
1992	100.8
1996	120.4
2000	140.6
2002	138.4

a. 
$$y = -0.0122x^3 + 0.8905x^2 - 13.6747x + 87.5062$$

b. 
$$y = 0.0102x^3 - 0.7905x^2 + 15.1707x + 89.8364$$

c. 
$$y = -0.0102x^3 + 0.7905x^2 - 15.1707x + 89.8364$$

d. 
$$y = -0.0078x^3 + 0.6359x^2 - 11.7207x + 87.5050$$

e. 
$$v = 0.0078x^3 - 0.6359x^2 + 11.7207x + 87.5050$$

ANSWER:

119. The table below shows the national expenditures for health care in a certain country for selected years. Find a power model and a linear model for the data where *x* is the number of years after 1950. Which of the models seems to be the best to use if you are interested in finding the health care costs near the year 1990? Round numerical values in your answers to three decimal places.

Year	National Expenditures for Health Care (in billions)		
1960	\$20.3		
1970	\$71.0		
1980	\$249.3		
1990	\$693.3		
2000	\$1,423.1		

a. 
$$y = 0.034x^{2.666}$$

$$y = 34.279x - 536.970$$

The power model gives more accurate results near the year 1990.

b. 
$$y = 0.034x^{2.666}$$

$$y = 34.279x - 536.970$$

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The linear model gives more accurate results near the year 1990.

c. 
$$y = 20.300x^{1.334}$$

$$y = 34.279x - 67,381.020$$

The power model gives more accurate results near the year 1990.

d. 
$$y = 20.300x^{1.334}$$

$$y = 34.279x - 67,381.020$$

The linear model gives more accurate results near the year 1990.

e. 
$$v = 693.300x^{1.334}$$

$$v = 34.279x + 693.300$$

The power model gives more accurate results near the year 1990.

ANSWER: a

120. Suppose the following table gives the U.S. population, in millions, for selected years, with projections to 2050. Find a linear model that approximately fits the data, with *x* equal to the number of years past 1960. Round numerical values in your answer to three decimal places. Depending on the technology you use, your answer may be slightly different than the correct answer shown.

Year	1960	1970	1980	1990	2000	2025	2050
U.S.	178.671	217.758	230.762	249.948	284.878	299.793	408.625
Populations							
(millions)							

a. 
$$y = 2.288x + 183.843$$

b. 
$$y = 3.072x + 185.299$$

c. 
$$y = 2.288x - 183.843$$

d. 
$$y = 3.072x - 185.299$$

e. 
$$y = 3.745x - 182.387$$

ANSWER: a

121. The table gives the percent of the population of a certain city that was foreign born in the given year. Find a cubic function that best fits the data where *x* is the number of years after 1900 and *y* is equal to the percent. By trial and error, estimate the year the model predicts that the foreign-born population will be 100%. Round numerical values in your answer to three decimal places.

Year	Percent		
	Foreign Born		
1900	10.94		
1910	16.64		
1920	8.05		
1930	7.30		

Name Class Dat : e:

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1940	9.24
1950	15.77

a.  $y = 0.0007x^3 - 0.0466x^2 + 0.5918x + 11.7987$ 

foreign born population will be 100% in 1965.

b.  $y = 0.0007x^3 - 4.2134x^2 + 8,094.4651x - 5,183,264.2767$ 

foreign born population will be 100% in 1975.

c.  $y = 0.0007x^3 - 0.0466x^2 + 0.5918x + 11.7987$ 

foreign born population will be 100% in 1975.

d.  $y = 0.0007x^3 - 4.2134x^2 + 8.094.4651x - 5.183.264.2767$ 

foreign born population will be 100% in 1965.

e.  $y = 0.0007x^3 - 0.0466x^2 + 0.5918x + 11.7987$ 

foreign born population will be 100% in 1985.

ANSWER:

С